Liquidity, Interest Rates and House Prices in the Euro area: A DSGE Analysis

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Abstract

In this paper, we propose a two-country monetary union DSGE model with housing, in order to study how different shocks contributed to the increase in housing prices and credit in the EMU prior to the crisis. One of the countries is calibrated to represent the core group in the Euro area while the other one corresponds to the periphery. First, we explore how a liquidity shock (or a decrease in the interest rate) affects house prices and the real economy through the asset price and the collateral channel. Then, we analyze how a house price shock in the periphery and a technology shock in the core countries are transmitted to the both economies. We find that a combination of an increase in liquidity in the Euro area coming from the common monetary policy, together with asymmetric house price and technology shocks, can explain the increase in house prices in the Euro area and the stronger credit growth in the peripheral economies in the pre-crisis period.

Keywords: Liquidity, interest rates, monetary policy, house prices, collateral effects, asymmetric shocks, asset prices.

JEL Classification: E32, E44, E58

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"[...] developments in the monetary aggregates and credit play an important role in the development of asset price boom episodes. Although the issue of empirical causality between asset prices on the one hand and money and credit developments on the other is a complicated one, the potential role of credit and money in driving asset prices is straightforward.". Speech by Jean-Claude Trichet, President of the ECB. 8 June 2005, Singapore.

1 Introduction

The launch of the European Economic and Monetary Union (EMU) in 1999 built up large imbalances in housing markets between European countries. In particular, we can distinguish two groups of countries: the peripheral countries (Greece, Ireland, Italy, Portugal, and Spain, known as GIIPS) and the rest.¹ One of these imbalances was set in the real sector when residential property prices of new and existing houses and flats increased 80% in the periphery from 1999 to 2007, while in the core the increase was less than 20%. Moreover, real gross fixed capital formation in dwellings doubled in the periphery and stated the same in the core between both years. Additionally, mortgage loans grew moderately in the core but they boomed in the periphery (Brzoza-Brzezina, Kolasa and Makarski, 2014).

Several scholars have pointed the possibility that the main drivers of the asymmetric evolution of the housing prices between the two areas could be of different nature. The first driver may remain in the financial sector: a fall in interest rates following their euro area accession and the easy access to cross-border borrowing after the launch EMU (see for instance ECB, 2003; Honohan and Leddin 2006; Blanchard, 2007; or Andrés et al., 2013). Secondly, it could be possible that a house price bubble was developed in the periphery. Finally, a third possibility might be in the real economy: shocks to productivity with asymmetric distribution between core and periphery (Andrés et al., 2013).

With respect to the first driver, it is important to note that in the Euro area, monetary policy is common for all the countries and it is conducted by the European Central Bank (ECB). The ECB implemented, since the introduction of the Euro till 2006, an expansionary monetary policy which increased liquidity in the Euro area (See Figure A1 in the Appendix). This fact was reflected in decreasing the interest rate to unprecedented lows. The fall was even more dramatic if the pre-EMU interest rates are taken into account.² Furthermore, due to the significant differences between the core and periphery

¹See Quint and Rabanal (2014) for more details on this division.
²For instance, the average Spanish government interest rate (interest payments/sovereign debt stock) fell from around 9% in the late 1990s to below 4% by 2010.
economies, the common monetary policy could have an asymmetric impact. The domestic demand growth was extremely strong at the periphery but very weak at the core. Therefore, monetary policy was too loose for the periphery and too tight for the rest. The increase in liquidity, the reduction of the interest rate, and its asymmetric impact caused different effects on the housing prices and credit in the core and the periphery through the transmission channels of monetary policy.

Secondly, many of the peripheral countries experimented strong increases in housing demand, not determined by economic fundamentals, which can be interpreted as housing bubbles or asymmetric house price shocks.

The third driver, an asymmetric productivity shock, could also affect differently the house prices of the core and the periphery. The productivity in the core evolved better than in the periphery. Even though the peripheral productivity was not improving as much as in the core, those countries benefitted from the lower common interest rates stemming from low inflation in the more productive region. This created a demand shock that affected credit and house prices in the periphery.

In order to explore the three previous drivers, we develop a model with two countries inside a monetary union. We identify these countries as core and periphery, respectively. In each country, there are two sectors, construction and consumption, and two infinite-horizon households, savers and borrowers. The model constitutes a two-country version of the seminal paper of Iacoviello (2005), that introduces a financial accelerator that works through the housing sector. This is done in the spirit of Iacoviello and Smets (2006) and Aspachs and Rabanal (2010). However, it introduces cross-country housing-market heterogeneity as in Rubio (2014). The model is then adapted to represent the core and the periphery in the Euro area, as in Brzoza-Brzezina et al (2014) and Quint and Rabanal (2014), who, differently to us, use their framework to study how to implement macroprudential policies in these two regions. In our paper, we use this model to analyze the influence of interest rate falls (increase in liquidity), and productivity shocks, on the asymmetric evolution of housing prices in the core and the periphery. Additionally, we study the impact of a shock in house prices that some scholars, such as in’t Veld et al. (2012), have pointed as source of changes in fundamentals.

Results from our simulations show that the increase in liquidity can explain higher house prices, through an asset price channel. Furthermore, collateral effects coming from higher house prices, contributed to the credit boom in the Euro area, being the effects more remarkable in the periphery, given that these countries were more leveraged. We also consider a house price shock in the periphery, to

\[3\text{See Figure A2 in the Appendix.}\]
account for a housing bubble in this area. We see that a stronger housing demand preference in these economies increases credit by a large amount, through the collateral constraint of borrowers. Finally, we observe that higher productivity in the core makes the common interest rate decrease and this causes a demand shock in the periphery, making credit and house prices increase through the credit channel.

Summarizing, our analysis shows that the combination of an increase in liquidity in the Euro area coming from the common monetary policy, together with asymmetric house price and technology shocks, contributed to the increase in house prices in the Euro area and the stronger credit growth in the peripheral economies in the pre-crisis period.

The paper is organized as follows. Section 1.2 presents some discussion on the related literature and the contribution of the paper. Section 2 sets up the model. Section 3 simulates the model. Section 4 concludes.

1.1 Related Literature and Contribution

There are a number of empirical studies that study the interrelations between monetary policy, liquidity and other shocks with house prices and credit. For instance, Taltavull and White (2012, 2015) use a VECM to examine the influence of several economic variables, including liquidity on house prices for the UK and Spain. Crowe et al. (2011) study the relationship between monetary policy conditions and house price changes based on a panel vector autoregression. Adrian and Shin (2009) and De Nicolo et al. (2010) analyze to which extent monetary policy affects the leverage in the financial sector. Our paper provides a theoretical counterpart to this studies to disentangle the mechanisms behind those results through a DSGE model.

On the other hand, there is also plenty of evidence that housing and credit markets did not behave in the same way across European countries. Guerrieri and Esposito (2012) provide evidence of these imbalances. They notice that the demand boom in the peripheral countries, led to losses of competitiveness and asset price inflation, notably in the housing market. Hansen (2010) and Marin (2010) suggest that Germany and the core countries reduced their labour costs, following the launch of the Euro and increased their productivity. Furthermore, as Stockhammer (2011) shows the core economies were export-led while the peripheral were credit-led. In the periphery, credit-financed consumption growth and residential investment became the key source of demand growth and run substantial current account deficits. Besides, the core did not experience an equally strong rise in household debt and consumption and increasingly relied on exports as the main growth engine. Also, as pointed out by Quint and Rabanal
(2014), the leverage in the housing sector was much higher in the periphery than in the core countries. The increase in household debt in percentage of GDP from 2000 to 2008 was more than 32% in Spain, 61% in Ireland, 21% in Portugal and 18% in Italy; while in core countries was much lower, in Austria was 7% and in Germany 11%.  

Our paper also sheds some light, from a theoretical perspective, on the effects of these imbalances. We calibrate the model to be representative of the core and the peripheral group and characterize asymmetric house price shocks (in the periphery) and asymmetric productivity shocks (in the core), to account for this evidence and find the mechanisms that explain them. We approximate the more leveraged countries by a higher LTV, which makes the collateral constraint more important and the financial accelerator effects stronger. In this way, the model is able to capture this difference between the two areas. Furthermore, since it is a two country model within a monetary union, the analysis is also able to illustrate the asymmetric technology and house price shocks between these two regions and the common monetary policy. Therefore, the structure of the model is suitable to answer the research question that we propose.

We introduce several channels in the setting through which shocks are transmitted. Throughout the paper, we consider liquidity shocks and changes in the interest rate as equivalent. As Woodford (2003) and Michis (2014) show, interest rates are influenced mainly by the money supply (i.e., the liquidity effect). Then, a change in the interest rate or in the liquidity can affect real estate prices via different channels. The first channel is the credit channel (Mishkin, 2007). Lower interest rates make it cheaper to obtain a mortgage and thus, there is an increase in the housing demand and an increase in the housing prices. This channel is present in our model through borrower’s debt repayments. The second channel is the so-called asset inflation channel (Belke et al, 2008). In this case, lower interest rates imply higher asset prices, including housing prices. In our model, housing prices move inversely with interest rates. Another channel that we explore here is the impact of house prices in the economy. Our model captures the positive wealth effect in case that the real estate price increases, since borrowers use houses as collateral to obtain loans. A higher price will let them increase their purchases, including houses. Therefore, we have here a financial accelerator effect (See Aoki et al, 2004 or Iacoviello, 2005).

Therefore, in our paper, we analyze the influence of interest rate falls (increase in liquidity), and productivity shocks, on the asymmetric evolution of housing prices in the core and the periphery. Additionally, we also study the impact of a shock in house prices.

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4 See Stockhammer (2011)
2 Model Setup

We consider an infinite-horizon, two-country, two-sector economy inside a monetary union. The home country (Core) is denoted by COR and the rest of the union (the periphery) by PER. Households consume, work, and demand real estate. Each country produces one differentiated intermediate good, but households consume goods from both countries. For simplicity, housing is a non-traded good. We assume that labor is immobile across the countries. Firms follow a standard Calvo problem. In this economy, both final and intermediate goods are produced. Prices are sticky in the intermediate-goods sector. There is a construction sector that produces houses. We introduce transaction-facilitating money by the device of including real balances as an argument of each household’s utility function. Monetary policy is conducted by a single central bank that responds to a weighted average of inflation in both countries. We allow for housing-market heterogeneity across the countries.

2.1 The Consumer’s Problem

There are two types of consumers in each country: borrowers and savers. Borrowers are constrained individuals who need to collateralize their debt repayment, that is, interest payments in the next period cannot exceed a proportion of the expected future value of the current house stock. As in Iacoviello (2005), I assume that constrained consumers are more impatient than unconstrained ones.\footnote{This assumption ensures that the borrowing constraint is binding in the steady state and that the economy is endogenously split into borrowers and savers.}

2.1.1 Unconstrained Consumers (Savers)

Unconstrained consumers in COR maximize as follows:

$$\max \, E_0 \sum_{t=0}^{\infty} \beta^t \left( \ln C_t + j \ln H_t + \chi \ln m_t - \left( \frac{L_t^u}{\eta} \right)^n \right),$$

Here, $E_0$ is the expectation operator, $\beta \in (0,1)$ is the discount factor, and $C_t$, $H_t$, $m_t$, and $L_t$ are consumption at $t$, the stock of housing, real money balances and hours worked, respectively.\footnote{It is assumed that housing services are proportional to the housing stock.} $j$ represents the weight of housing in the utility function. $1/(\eta - 1)$ is the aggregate labor-supply elasticity.

Consumption is a bundle of domestically and foreign-produced goods, defined as: $C_t = (C_{COR})^n (C_{PER})^{1-n}$, where $n$ is the size of COR. Unconstrained consumers provide labor to both the consumption and construction sector, so that $L_t = \left( (L_{ct})^{1-v} + (L_{ht})^{1-v} \right)^{1/(1-v)}$. 
The budget constraint for COR is as follows:

\[ P_{\text{COR}} C_{\text{COR}} + P_{\text{PER}} C_{\text{PER}} + Q_{\text{COR}} (H_t - H_{t-1}) + R_{\text{COR}t-1} B_{2t-1} + R_{t-1} D_{t-1} + \frac{\psi}{2} D_t^2 + M_{t-1} \leq \]

\[ W_{ct} L_{ct} + W_{ht} L_{ht} + B_t + D_t + M_{t-1} + P_{\text{COR}} F_t + P_{\text{COR}} T_t, \]

where \( P_{\text{COR}} \) and \( P_{\text{PER}} \) are the prices of the goods produced in Countries COR and PER, respectively, \( Q_{\text{COR}} \) is the housing price in COR, and \( W_{ct} \) and \( W_{ht} \) are the consumption and housing sector wages for unconstrained consumers. \( B_t \) represents domestic bonds denominated in the common currency. \( R_{\text{COR}t} \) is the nominal interest rate in COR. Positive bond holdings signify borrowing, and negative signify savings. However, as we will see, unconstrained consumers will choose not to borrow at all: they are the savers in this economy. \( D_t \) are foreign-bond holdings by savers in COR.\(^7\) \( M_t \) are nominal money balances. \( R_t \) is the nominal rate of foreign bonds, which are denominated in euros. As is common in the literature, to ensure stationarity of net foreign assets we introduced a small quadratic cost of deviating from zero foreign borrowing, \( \frac{\psi}{2} D_t^2 \).\(^8\) Savers obtain interest on their savings. \( F_t \) are lump-sum profits received from the firms. \( T_t \) are lump-sum government transfers.

Dividing by \( P_{\text{COR}} \), we can rewrite the budget constraint in terms of goods in COR:

\[ \frac{C_{\text{COR}}}{P_{\text{COR}}} + \frac{P_{\text{PER}}}{P_{\text{COR}}} C_{\text{PER}} + q_{\text{COR}} (H_t - H_{t-1}) + \frac{R_{\text{COR}t-1} b_{2t-1}}{\pi_{\text{COR}}} + \frac{R_{t-1} d_{t-1}}{P_{\text{COR}}} + \frac{\psi}{2} d_t^2 + \frac{m_{t-1}}{\pi_{\text{COR}}} \leq \]

\[ w_{ct} L_{ct} + w_{ht} L_{ht} + b_t + d_t + m_{t-1} + F_t + T_t, \]

where \( \pi_{\text{COR}} \) denotes inflation for the goods produced in COR, defined as \( P_{\text{COR}t} / P_{\text{COR}t-1} \). \( q_{\text{COR}} \) is defined as \( Q_{\text{COR}} / P_{\text{COR}} \).

Maximizing (1) subject to (3), we obtain the first-order conditions for the unconstrained group:

\[ \frac{C_{\text{COR}}}{P_{\text{PER}}} = \frac{n P_{\text{PER}}}{(1 - n) P_{\text{COR}}} \]

\[ \frac{1}{C_{\text{COR}}} = \beta E_t \left( \frac{R_{\text{COR}}}{\pi_{\text{COR}t+1} C_{\text{COR}t+1}} \right), \]

\(^7\)Savers have access to international financial markets.

\(^8\)See Iacoviello and Smets (2006) for a similar specification of the budget constraint.
\[ \frac{1 - \psi_{d,t}}{C_{CORT}} = \beta E_t \left( \frac{R_t}{\pi_{CORT+1} C_{CORT+1}} \right), \]  
\tag{6}

\[ \frac{n}{C_{CORT}} = \beta E_t \left( \frac{n}{\pi_{CORT+1} C_{CORT+1}} \right) + \frac{\chi}{m_t}, \]  
\tag{7}

\[ w_{ct} = (L_t)^{\eta-1} (L_{ct})^{-\nu} \left[ (L_{ct})^{1-\nu} + (L_{ht})^{1-\nu} \right]^{\frac{\nu}{1-\nu}} \frac{C_{CORT}}{n}, \]  
\tag{8}

\[ w_{ht} = (L_t)^{\eta-1} (L_{ht})^{-\nu} \left[ (L_{ct})^{1-\nu} + (L_{ht})^{1-\nu} \right]^{\frac{\nu}{1-\nu}} \frac{C_{CORT}}{n}, \]  
\tag{9}

\[ \frac{j}{H_t} = \frac{n}{C_{CORT}} q_{CORT} - \beta E_t \frac{n}{C_{CORT+1}} q_{CORT+1}. \]  
\tag{10}

Equation (4) equates the marginal rate of substitution between goods to the relative price, and it reflects the fact that countries are trading. Equation (5) is the Euler equation for consumption, which states that consumers would like to smooth consumption over time. That is, at the margin, consumers should be indifferent between consuming one extra unit of consumption today or saving it to the future. Equation (6) is the first-order condition for net foreign assets, and its intuition is equivalent to the previous Euler equation. Equation (7) represents money demand, that is an Euler equation for money.\(^9\) Equations (8) and (9) are the labor-supply conditions for both sectors. These equations are standard. Equation (10) is the Euler equation for housing and states that, at the margin, the benefits from consuming housing today have to be equal to the costs. That is, if consumers consume one unit of housing today, they enjoy the utility it derives and they can sell it in the future. However, they incur in a cost today in terms of consumption.

Combining (5) and (6) we obtain a non-arbitrage condition between home and foreign bonds:\(^{10}\)

\[ R_{CORT} = \frac{R_t}{(1 - \psi_{d,t})}. \]  
\tag{11}

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\(^9\)The Euler condition for money is a typical expression for the price of an asset. If consumers give up consumption today and decide to hold money forever from then on, they will enjoy the stream of utility services which will be eroded from the rise in prices.

\(^{10}\)The log-linearized version of this equation could be interpreted as the uncovered interest-rate parity.
Since all consumption goods are traded and there are no barriers to trade, we assume in this paper that the law of one price holds:

\[ P_{\text{COR}} = P_{\text{COR}}^*, \]  

(12)

where variables with a star denote foreign variables.

### 2.1.2 Constrained Consumers (Borrowers)

Constrained consumers are more impatient than unconstrained ones, that is \( \tilde{\beta} < \beta \). Constrained consumers face a collateral constraint: the expected debt repayment in the next period cannot exceed a proportion of the expectation of tomorrow’s value of today’s stock of housing:

\[ E_t \frac{R_{\text{COR}}}{\pi_{\text{COR}}+1} b_t' \leq k_{\text{COR}} E_t q_{\text{COR},t+1} H_t', \]  

(13)

where equation (13) represents the collateral constraint for the borrower. \( k_{\text{COR}} \) can be interpreted as the loan-to-value ratio in COR.

Borrowers maximize their lifetime utility function:

\[
\max E_0 \sum_{t=0}^{\infty} \beta^t \left( \ln C_t' + j \ln H_t' + \chi \ln m_t' - \frac{(L_t')^{\eta}}{\eta} \right),
\]

(14)

where \( C_t' = \left( C_{\text{COR}}' \right)^n \left( C_{\text{PERI}}' \right)^{1-n} \), \( L_t' = \left[ \left( L_{ct}' \right)^{1-\nu} + \left( L_{ht}' \right)^{1-\nu} \right]^{\frac{1}{1-\nu}} \), subject to the budget constraint (in terms of the consumption good in COR):

\[
C_{\text{CORI}}' + \frac{P_{\text{PERI}}}{P_{\text{CORI}}} C_{\text{PERI}}' + q_{\text{CORI}} (H_t' - H_{t-1}') + \frac{R_{\text{CORI}}}{\pi_{\text{CORI}}} b_{t-1}' + \frac{m_{t-1}'}{\pi_{\text{CORI}}} \leq w_{ct}' L_{ct}' + w_{ht}' L_{ht}' + b_t' + m_t',
\]

(15)

and subject to the collateral constraint (13).

The first-order conditions for these consumers are as follows:

\[
\frac{C_{\text{CORI}}'}{C_{\text{PERI}}'} = \frac{n P_{\text{PERI}}}{(1-n) P_{\text{CORI}}}
\]

(16)
\[
\frac{n}{C_{CORt}'} = \tilde{\beta} E_t \left( \frac{n R_{CORt}}{\pi_{CORt+1} C_{CORt+1}'} \right) + \lambda_t R_{CORt}, \tag{17}
\]

\[
\frac{n}{C_{CORt}'} = \tilde{\beta} E_t \left( \frac{n}{\pi_{CORt+1} C_{CORt+1}'} \right) + \frac{\chi}{m_t}, \tag{18}
\]

\[
w_{ct}' = \left( L_t' \right)^{\eta-1} \left( L_{ct}' \right)^{-\nu} \left[ \left( L_{ct}' \right)^{1-\nu} + \left( L_{ht}' \right)^{1-\nu} \right] \frac{\nu}{1-\nu} \frac{C_{CORt}'}{n}, \tag{19}
\]

\[
w_{ht}' = \left( L_t' \right)^{\eta-1} \left( L_{ht}' \right)^{-\nu} \left[ \left( L_{ct}' \right)^{1-\nu} + \left( L_{ht}' \right)^{1-\nu} \right] \frac{\nu}{1-\nu} \frac{C_{CORt}'}{n}, \tag{20}
\]

\[
\frac{j}{H_t} = \frac{n}{C_{CORt}'} q_{CORt} - \tilde{\beta} E_t \frac{n}{C_{CORt+1}'} q_{CORt+1} - \lambda_t k_{CORt} E_t q_{CORt+1} \pi_{CORt+1}. \tag{21}
\]

These first-order conditions can be interpreted in a similar way to the ones of the savers. However, they differ from those of unconstrained individuals in some aspects. In the case of constrained consumers, the Lagrange multiplier on the borrowing constraint \((\lambda_t)\) appears in equations (17) and (21) to reflect the fact that housing has an extra collateral effect on these consumers. As in Iacoviello (2005), the borrowing constraint is always binding, so that constrained individuals borrow the maximum amount they are allowed, and their saving is zero.\(^\text{11}\)

The problem for consumers is analogous in PER.

### 2.2 Firms

#### 2.2.1 Final-Consumption Goods Producers

In COR, there is a continuum of final-goods producers that aggregate intermediate goods according to the production function:

\[
Y_{CORt}^k = \left[ \int_0^1 Y_{CORt}^k (z)^{\frac{r-1}{r}} dz \right]^{\frac{r}{r-1}}, \tag{22}
\]

\(^\text{11}\)From the Euler equations for consumption of the unconstrained consumers, we know that \(R_{COR} = 1/\beta\), where variables without a time subscript denote steady-state variables. If we combine this result with the Euler equation for consumption for the constrained individual, we have \(\lambda = n \left( \beta - \tilde{\beta} \right) / C_{COR} > 0\). Given that \(\beta > \tilde{\beta}\), the borrowing constraint holds with equality in steady state. Since the model is log-linearized around the steady state and low uncertainty is assumed, this result can be generalized to off-steady-state dynamics.
where \( \varepsilon > 1 \) is the elasticity of substitution among intermediate goods.

The total demand of intermediate-good \( z \) is given by \( Y_{CORt} (z) = \left( \frac{P_{CORt}(z)}{P_{CORt}} \right)^{-\varepsilon} Y_{CORt} \), and the price index is \( P_{CORt} = \left[ \int_0^1 P_{CORt} (z)^{1-\varepsilon} dz \right]^{\frac{1}{\varepsilon-1}} \).

### 2.2.2 Intermediate-Goods and House Producers

The intermediate-goods consumption market is monopolistically competitive. Following Iacoviello (2005), intermediate goods are produced according to the following production function:

\[
Y_{CORt} (z) = \xi_t \left( L_{ct} (z) \right)^\gamma \left( L'_{ct} (z) \right)^{(1-\gamma)},
\]  

(23)

where \( \xi_t \) represents technology. We assume that \( \log \xi_t = \rho_t \log \xi_{t-1} + u_{\xi t} \), where \( \rho_t \) is the autoregressive coefficient and \( u_{\xi t} \) is a normally distributed shock to technology. \( \gamma \in [0, 1] \) measures the relative size of each group in terms of labor.

Symmetry across firms allows avoiding index \( z \) and re-writing equation (23) as:

\[
Y_{CORt} = \xi_t \left( L_{ct} \right)^\gamma \left( L'_{ct} \right)^{(1-\gamma)},
\]  

(24)

The production function for housing investment is as follows:

\[
I_{CORt} = \xi_t \left( L_{ht} \right)^\gamma \left( L'_{ht} \right)^{(1-\gamma)},
\]  

(25)

Producers maximize profits:

\[
\max_{L_{ct},L_{ht},L'_{ct},L'_{ht}} \frac{Y_{CORt}}{X_t} + q_{CORt} I_{CORt} - w_{ct} L_{ct} - w_{ht} L_{ht} - w'_{ct} L'_{ct} - w'_{ht} L'_{ht}.
\]  

(26)

The first-order conditions for labor demand are the following:

\[
w_{ct} = \frac{1}{X_t} \gamma \frac{Y_{CORt}}{L_{ct}},
\]  

(27)

\[
w'_{ct} = \frac{1}{X_t} (1-\gamma) \frac{Y_{CORt}}{L'_{ct}},
\]  

(28)

\[
w_{ht} = \gamma q_{CORt} I_{CORt} \frac{L'_{ht}}{L_{ht}},
\]  

(29)
\[ w_{ht}' = (1 - \gamma) \frac{q_{CORt}I_{CORt}}{L_{ht}}, \]  
(30)

where \( X_t \) is the markup, or the inverse of marginal cost.

The price-setting problem for the intermediate-goods producers is a standard Calvo-Yun case. An intermediate-goods producer sells goods at price \( P_{CORt}(z) \), and \( 1 - \theta \) is the probability of being able to change the sale price in every period. The optimal reset price \( P^{OPT}_{CORt}(z) \) solves the following:

\[
\sum_{k=0}^{\infty} (\theta/\beta)^k E_t \left\{ \Lambda_{t,k} \left[ \frac{P^{OPT}_{CORt}(z)}{P_{CORt+k}} - \frac{\varepsilon}{(\varepsilon - 1)} \frac{Y^{OPT}_{CORt+k}(z)}{X_{t+k}} \right] \right\} = 0. \tag{31}
\]

The aggregate price level is given as follows:

\[
P_{CORt} = \left[ \theta P^{1-\varepsilon}_{CORt-1} + (1 - \theta) (P^{OPT}_{CORt})^{1-\varepsilon} \right]^{1/(1-\varepsilon)}. \tag{32}
\]

Using (31) and (32) and log-linearizing, we can obtain the standard forward-looking Phillips curve.\textsuperscript{12}

The firm problem is similar in PER.

2.3 Aggregate Variables and Market Clearing

Economy-wide aggregates in Country COR are \( C_t \equiv C_t + C_t' \), \( L_t \equiv L_t + L_t' \). Domestic housing market clearing requires \( I_{CORt} \equiv (H_t - H_{t-1}) + (H_t' - H_{t-1}') \).

The market clearing condition for the final good in Country COR is \( nY_{CORt} = nC_{CORt} + (1 - n) C^*_t + n \frac{\psi}{2} d^2_t \). Domestic financial markets clear: \( b_t = b_t' \). The world bond market clearing condition is \( nd_t + (1 - n) \frac{P_{PERt}}{P_{CORt}} d^*_t = 0 \), where \( d_t \) denotes the foreign bonds in real terms. The net foreign asset position follows \( d_t = \frac{R_{t+1}}{(1 - \psi a_t) q_{CORt}} d_{t-1} + Y_{CORt} - C_{CORt} - \frac{P_{PERt}}{P_{CORt}} C_{PERt} \). Everything is similar in PER.

2.4 Monetary Policy

In order to close the model, we need to specify a way to introduce monetary policy. The central bank uses the money supply as an instrument to affect the economy, so that injecting or draining liquidity into the system is transmitted through credit and housing markets until it affects real variables. However, if we combine the saver’s Euler equation for consumption (equation 5) with their money demand (equation 7), we observe the following:

\textsuperscript{12} This Phillips curve is consistent with other two-country models with financial accelerator. See for instance Gilchrist et al (2002) or Iacoviello and Smets (2006).
\[ m_t = \frac{\lambda C_{\text{CORt}}}{n} \left( \frac{R_{\text{CORt}}}{R_{\text{CORt}} - 1} \right) \]

That is, for given values of consumption and prices and taking into account equation (11), there is a one-to-one mapping between the money supply and the interest rate set by the central bank. Therefore, monetary policy can be represented by an interest rate rule. In this way, a decrease in the target interest rate is equivalent to an increase in liquidity and vice versa. With this approach, although there would be a transaction-oriented demand for real money balances implied by the optimization problem of the agents, when policy is based on an interest rate policy rule, the money demand function would serve only to indicate the quantity of money needed to support the interest rate rule. Thus, throughout the paper we will assume that interest rate shocks are analogous to liquidity shocks.\textsuperscript{13}

\subsection*{2.4.1 Interest Rate Rule}

We consider a Taylor rule with interest-rate smoothing for interest-rate setting by a single central bank,\textsuperscript{14}

\[ R_t = (R_{t-1})^{\rho_R} \left( \left[ (\pi_{\text{CORt}})^n (\pi_{\text{PERt}})^{(1-n)} \right]^{(1+\phi_{\pi})} R \right)^{1-\rho_R} \varepsilon_{R,t}, \]  \hspace{1cm} (33)

0 \leq \rho_R \leq 1 is the parameter associated with interest-rate inertia. \((1 + \phi_{\pi})\) measures the sensitivity of interest rates to current inflation. \(\varepsilon_{R,t}\) is a white noise shock process with zero mean and variance \(\sigma^2_{\varepsilon_R}\). This rule is consistent with the primary objective of the ECB being price stability.

\section*{3 Dynamics}

In this section, we simulate the model to illustrate how monetary policy affects housing prices and the rest of economic variables in the core and the periphery. In particular, we want to explore how an increase in liquidity has affected housing markets and the real economy in both economies. We also illustrate the effects of house price shocks and technology shocks in the periphery and the core economies, respectively.

\textsuperscript{13}Since Woodford (2003), the standard practice is to consider a cash-less economy, expressing policy behavior in terms of interest rate rules.

\textsuperscript{14}This type of rule is also used in other monetary-union models. See Iacoviello and Smets (2006) or Aspachs and Rabanal (2008). Furthermore, as shown in Iacoviello (2005) and Rubio and Carrasco-Gallego (2013), a rule that only responds to inflation enhances the financial accelerator.
3.1 Parameter Values

Parameters are calibrated to reflect the core economy and the periphery. Some of the parameters are standard and are common for both economies and some others will be specifically calibrated for each area.\textsuperscript{15}

Discount factors are set to be common in both economies, following the standard values in the literature. The discount factor for savers, $\beta$, is set to 0.99 so that the annual interest rate is 4\% in steady state. The discount factor for borrowers, $\tilde{\beta}$, is set to 0.98.\textsuperscript{16} The steady-state weight of housing in the utility function, $j$, is set to 0.12. This parameter pins down the ratio of housing wealth to GDP.\textsuperscript{17} We set $\eta = 2$, implying a value of the labor supply elasticity of 1.\textsuperscript{18} Following Horvath (2000) and Iacoviello and Neri (2010), we set the inverse elasticity of substitution across hours in the two sectors to one. For the loan-to-value ratio we consider a steady-state value of 0.70 and 0.80, for COR and PER, respectively, in order to reflect a low and a high leveraged country.\textsuperscript{19} The labor-income share of unconstrained consumers, $\gamma$, is set to 0.7.\textsuperscript{20} We pick a value of 6 for $\epsilon$, the elasticity of substitution among intermediate goods. This value implies a steady-state markup of 1.2. The probability of not changing prices, $\theta$, is set to 0.75, implying that prices change every four quarters on average. For the Taylor Rule parameters, we use $\rho = 0.8$, $\phi_\pi = 0.5$. The first value reflects a realistic degree of interest-rate smoothing.\textsuperscript{21} $\phi_\pi$ is consistent with the original parameters proposed by Taylor in 1993. The size of the peripheral group is considered to be 40\%.\textsuperscript{22} A technology shock is a 1\% positive technology with 0.9 persistence.\textsuperscript{23}
3.2 Impulse Responses

3.2.1 Interest rate/liquidity shock

This shock represents the increase in liquidity that occurred when the Euro area was established. The ECB and other central banks, previous to the crisis, implemented unprecedented loose monetary policies. The increase in liquidity situated interest rates at very low levels. From October 2000 to November 2005 the ECB decreased the interest rate from 4.75% to 2%, as it is shown in Figure A1. In this section, we proxy this ECB policy as a negative interest-rate shock.

As expected, in Figure 1, we observe that an increase in liquidity has an immediate effect in house

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15 For robustness, we have provided some alternative simulations which can be found in the Appendix. We have set simulations for a two country model with countries that are equal in size but have different proportion of borrowers and different LTVs. We have done this for both monetary and technology shocks. See figures A3-A6 in the Appendix.

16 Lawrance (1991) estimate discount factors for poor consumers at between 0.95 and 0.98 at quarterly frequency.

17 Following Aspachs and Rabanal (2008), we use 1.40, value that reflects the ratio of housing wealth to GDP across most industrialized countries as a proxy for the Euro area.

18 Microeconomic estimates usually suggest values in the range of 0 and 0.5 (for males). Domeij and Flodén (2006) show that in the presence of borrowing constraints this estimate could have a downward bias of 50%.

19 These values approximately reflect the prevalent loan-to-values in Germany and Spain, representing respectively the core and the periphery.

20 This value is in the range of the estimates of Iacoviello (2005) and Iacoviello and Neri (2010) for the US, and Campbell and Mankiw (1991) for the US, Canada, France, and Sweden. Therefore, we take it as valid for most of the countries of the Euro area.


22 We follow Quint and Rabanal (2014).

23 This high persistence value for technology shocks is consistent with what is commonly reported in the literature. Smets and Wouters (2002) estimated a value of 0.822 for this parameter in Europe; Iacoviello and Neri (2010) estimated it as 0.93 for the US.
prices. As stated before, there are several channels that can potentially link liquidity with house prices. Through the asset-price channel, since the increase in liquidity lowers the interest rate, asset prices should increase due to a substitution effect from money to other assets. House prices are an asset price and therefore they should move inversely with the interest rate. Figure 1 shows that this is precisely what happens; following the decrease in the interest rate, house prices start to rise. We also see that loose credit conditions in the Euro area lead to an increase in borrowing, especially in the periphery. There are two reasons why this occurs. First, lower interest rates make it cheaper to obtain a mortgage and thus, the common lower interest rates makes credit increase in both the core and the periphery. A second reason which represents a strong mechanism in this model is wealth effects. Borrowers need housing collateral in order to obtain loans. The value of this collateral is thus linked to house prices since houses will be more or less valuable depending on house price movements. As we have seen, the increase in liquidity makes house prices go up and therefore the value of the collateral to increase as well. This produces a wealth effect because borrowers are wealthier now, since they can obtain more credit either to purchase more houses or more consumption goods. This collateral channel is the so-called financial accelerator effect since changes due to non-financial reasons, such as liquidity in this case, are amplified through the financial market. We also see that the fact that the LTV is higher in the periphery makes these households be more sensitive to changes in the interest rate, due to a stronger financial accelerator effect. The increase in liquidity causes a common demand shock in both areas but it exacerbates the credit boom in the periphery. Mortgaged houses, although they increase in both areas, increase by more in the peripheral economies. This increase in housing demand should also have an effect on house prices. However, as we see in the graph, house prices do not increase by more in the periphery than in the core countries. Thus, given that the increase in house prices is very similar in the two economies, we can conclude that the channel that is prevalent here is the asset price channel, which is common for both the core and the periphery. In terms of consumption, demand increases in both groups of countries due to lower interest rates and the collateral effects, but by more in the periphery.

3.2.2 House price shock in PER

In order to explain the higher house price growth in the peripheral economies, we assume that the periphery suffered a housing demand shock that was translated to higher house prices. Brzoza-Brzezina et al. (2014) present evidence that residential property prices of new and existing houses and flats in the periphery raised to 80% between 1999 and 2007, while in the core the increase was less than 20%. They
also show that real gross fixed capital formation in dwellings multiplied by two in the periphery and stated the same in the core in that period. Furthermore, they display that mortgage loans boomed in the periphery while they grew moderately in the core. Besides, Mayer and Gareis (2013) find that in the EMU from 1997 to 2008 housing preference and technology shocks were the main drivers of fluctuations in house prices and residential investment. They show that the majority of the variation of housing preference shocks can be explicated by demand factors. There is a general consensus about the fact that some periphery countries suffered a bubble on house prices during the first years of the 21st century. Therefore, in order to explain the higher house price growth in the peripheral economies, we first analyze the situation in which the periphery suffers a housing demand shock that is translated to higher house prices. In the next section we will consider a technology shock.

Figure 2 illustrates an increase in the preference for houses in the periphery produces a raise in housing prices in this area. Since the value of the collateral is higher in the peripheral economies but not in the core countries, borrowing increases only in the periphery, creating a credit boom in this region. Houses, in the periphery, since they serve as a collateral, have an intrinsic value that consumption goods do not have. Therefore, in the periphery, households substitute away consumption goods by mortgaged houses. This is why we observe a strong increase in mortgaged houses, financed by the increase in credit and a slight decrease in consumption. The common interest rate slightly falls in the monetary

\[ \text{See for instance McQuinn and O’Reilly (2006), Malzubris (2008) or Conefrey and Gerald (2010).} \]
union and, although it has no effects on borrowing in the core economies, there is a little increase in consumption. Here, we see that higher house prices also affects the interest rate and thus liquidity. The effect is bidirectional. If we compare this shock with the previous one, we see that in order to explain the different behavior of house prices in the core and the periphery that we empirically observed, we cannot only rely on liquidity shocks. The liquidity shock produces an upward effect in house prices that is mainly driven by the asset-price channel and therefore, given the common monetary policy in the Euro area, it does not generate a different behavior in house prices across economies. We need to introduce asymmetric house price (housing demand) shocks in order to explain the higher hike in house prices in this periphery, as compared to the core.

3.2.3 Technology shock in COR

As it was pointed out before, technology shocks were one of the main drivers of fluctuations in house prices and residential investment in EMU countries. However, they did not occur evenly between the core and the peripheral countries. In Figure A2 in the Appendix, we show the growth in multifactor productivity for the core and the periphery. We observe that the growth in productivity was higher in the pre-crisis period in the core region than in the periphery. For instance, the difference in productivity growth between the two areas was 0.2 percentage points in 2001 and it increased up to 1.4 percentage points in 2006. Then, productivity differentials between the core and the periphery after the launch of
the Euro may have contributed to the credit boom in the peripheral economies previous to the crisis.

In Figure 3, we illustrate an asymmetric shock that happens only in the core countries, to proxy for this evidence. The core countries experiment a productivity shock that increases output and decreases inflation. Lower inflation rates in the core countries, which have a higher weight in the Taylor rule, make the systematic component of the policy rule respond by lowering interest rates. The decrease in the interest rate, in the context of the monetary union, is common to the periphery as well. The periphery does not benefit from a productivity shock but it is transmitted to these countries in the form of lower interest rates, loosening credit conditions. Thus, a supply shock in the core Euro area becomes a demand shock in the periphery, due to lower interest rates. Therefore, consumption in the periphery also increases, as in the core but at the expense of higher inflation and a credit boom that is stronger than in the core countries.

4 Concluding Remarks

In this paper, we build a two-country, two-sector DSGE model with housing and collateral constraints in order to illustrate how the common monetary policy and asymmetric shocks to technology and housing preferences contributed to the increase in house prices and credit in the Euro area previous to the crisis. We characterize the two economies as the core and the periphery, in order to compare the effects of different shocks among these different groups of countries.

Using this framework, we illustrate that the increase in liquidity that emerged from the launch of the Euro made house prices increase through an asset price inflation. Lower interest rates following the increase in liquidity and collateral effects stemming from higher house prices contributed to the credit boom in the Euro area, being the effects more remarkable in the periphery, given that these countries were more leveraged.

Furthermore, we also analyze how asymmetric shocks helped determine the imbalances in housing and credit markets in the Euro area. First, we consider a house price shock in the periphery. We see that a stronger housing demand preference in these economies has as a consequence a strong increase in credit, through the collateral constraint of borrowers. Second, we study the effects of an asymmetric technology shock in the core economies. We observe that higher productivity in the core makes the common interest rate decrease; this supply shock in the core is transmitted to the periphery as a demand shock through lower interest rates, making credit and house prices increase.
In conclusion, a combination of an increase in liquidity in the Euro area coming from the common monetary policy, together with asymmetric house price and technology shocks, contributed to the increase in house prices in the Euro area and the stronger credit growth in the peripheral economies.

Appendix

Additional Tables and Figures

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<th>Table A1: Parameter Values</th>
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Figure A1: European Central Bank Benchmark Rate. Source: www.tradingeconomics.com, European Central Bank

Figure A2: Multifactor productivity average growth rate (2001-2007). Source: OECD Statistics, Growth in multifactor productivity. Authors’ calculations. Core: Austria, Belgium, Finland, France, Germany, and Netherlands. Periphery: Ireland, Italy, Portugal, and Spain.
Figure A3: Impulse Responses to a Monetary Policy Shock. Same size countries. Country A, gamma = 0.2. Country B, gamma = 0.8

Figure A4: Impulse Responses to a Technology Shock. Same size countries. Country A, gamma = 0.2. Country B, gamma = 0.8
Figure A5: Impulse Responses to a Monetary Policy Shock. Same size countries. Country A, LTV = 0.1. Country B, LTV = 0.9

Figure A6: Impulse Responses to a Technology Shock. Same size countries. Country A, LTV = 0.1. Country B, LTV = 0.9
References


