Observational constraints on the spin of the most massive black holes from radio observations

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ABSTRACT

We use recent progress in simulating the production of magnetohydrodynamic jets around black holes to derive the cosmic spin history of the most massive black holes. Our work focusses on black holes with masses $\gtrsim 10^8 \, M_\odot$. Under the assumption that the efficiency of jet production is a function of spin $\hat{a}$, as given by the simulations, we can approximately reproduce the observed ‘radio loudness’ of quasars and the local radio luminosity function.

Using the X-ray luminosity function and the local mass function of supermassive black holes, SMBHs, we can reproduce the individual radio luminosity functions of radio sources showing high- and low-excitation narrow emission lines. We find that the data favour spin distributions that are bimodal, with one component around spin zero and the other close to maximal spin. The ‘typical’ spin is therefore really the expectation value, lying between the two peaks. In the low-excitation galaxies, the two components have similar amplitudes, meaning approximately half of the sources have very high spins, and the other have very low spins. For the high-excitation galaxies, the amplitude of the high-spin peak is typically much smaller than that of the low-spin peak, so that most of the sources have low spins. However, a small population of near maximally spinning high-accretion rate objects is inferred. A bimodality should be seen in the radio loudness of quasars, although there are a variety of physical and selection effects that may obfuscate this feature.

We predict that the low-excitation galaxies are dominated by SMBHs with masses $\gtrsim 10^8 \, M_\odot$, down to radio luminosity densities $\sim 10^{21} \, \text{W Hz}^{-1} \, \text{sr}^{-1}$ at 1.4 GHz. Under reasonable assumptions, our model is also able to predict the radio luminosity function at $z=1$, and predicts it to be dominated by radio sources with high-excitation narrow emission lines above luminosity densities $\gtrsim 10^{26} \, \text{W Hz}^{-1} \, \text{sr}^{-1}$ at 1.4 GHz, and this is in full agreement with the observations.

From our parametrisation of the spin distributions of the high- and low-accretion rate SMBHs, we derive an estimate of the spin history of SMBHs, which shows a weak evolution between $z=1$ and 0. A larger fraction of low-redshift SMBHs have high spins compared to high-redshift SMBHs. Using the best fitting jet efficiencies there is marginal evidence for evolution in spin: the mean spin increases slightly from $\langle \hat{a} \rangle \sim 0.25$ at $z=1$ to $\langle \hat{a} \rangle \sim 0.35$ at $z=0$, and the fraction of SMBHs with $\hat{a} \gtrsim 0.5$ increases from $0.16 \pm 0.03$ at $z=1$ to $0.24 \pm 0.09$ at $z=0$. Our inferred spin history of SMBHs is in excellent agreement with constraints from the mean radiative efficiency of quasars, as well as the results from recent simulations of growing SMBHs. We discuss the implications in terms of accretion and SMBH mergers. We also discuss other work related to the spin of SMBHs as well as work discussing the spin of galactic black holes and their jet powers.

Key words: galaxies : active galaxies : jets–galaxies: nuclei – quasars: general –black hole physics – cosmology: miscellaneous
1 INTRODUCTION

Astrophysical black holes are described by two parameters, mass and spin, which define the structure of space-time around the black hole. Distant observers can infer black hole properties from the dynamics of material orbiting the black hole or more indirectly when matter is being accreted, from the radiation and jets produced.

Active galactic nuclei (AGN) are believed to be powered by accretion onto supermassive black holes (SMBHs, e.g. Lurid-Bell 1969; Rees 1984). Matter accreted onto the SMBH radiates via thermal and non-thermal processes, dominating the observed spectral energy distribution (SED) between X-ray energies and far-infrared wavelengths (see e.g. Krolik 1999). Multiwavelength observations can therefore be used to measure the bolometric luminosity of the AGN, although in practice reasonable estimates of this quantity can be obtained from observations in a single band (e.g. Elvis et al. 1994; Hopkins et al. 2007).

Accretion onto SMBHs can also produce jets. The bulk of the jet power is used to fill and expand a cocoon of low-density relativistic magnetised plasma that pushes back the intergalactic medium (IGM, see e.g. Longair et al. 1973; Scheuer 1974; Begelman et al. 1984). These lobes are sources of synchrotron radiation emitted at radio wavelengths. However, the power is radiated at a much lower rate than is supplied to the lobes via the jets, at least while the jets are active, so that energy is stored in the lobes. Making assumptions about the contents of the lobes (charged particles and magnetic fields), and how the energy density is distributed between them, as well as assumptions on the typical jet advance speeds and IGM density profiles, the jet power can be estimated from the low-frequency monochromatic radio luminosity (e.g. Miller et al. 1993; Willott et al. 1997).

Observations of AGN require an extra ‘hidden variable’ to explain the variations in radio luminosity, reflecting variations in jet power. For a given radiative power, AGN can show radio luminosities that vary by more than two orders of magnitude (e.g. Kellermann et al. 1989; Miller et al. 1993; Willott et al. 1999). The jets can be steady, transient or abnormally powerful jets can be driven by low we mean an Eddington rate\(\dot{E}<0.1\), or during high accretion rates (\(\lambda\sim0.3\), e.g. GRS 1915+105, see e.g. Fender et al. 2004). The jets can be steady, transient or absent at \(\lambda\sim0.01\), depending on the accretion state. This is consistent with steady jets requiring geometrically-thick accretion flows, either ADAFs (advection-dominated accretion flows Narayan & Yi 1995) or slim discs (Abramowicz et al. 1998). However, these differences in the accretion flow are observable at X-ray energies, while as explained in the preceding paragraphs, the radio-loudness of AGN requires an extra variable parameter that is not readily observable.

Finally, we note that comparison of individual spin measurements for GBHs find no correlation between radio loudness and individual spin estimates (Fender et al. 2010). We discuss these results in detail later in this paper, in Section 4.1 and argue that they are not robust enough to invalidate the spin paradigm.

In this work we begin by spelling out our assumptions in Section 2, where we also introduce the different jet efficiencies, drawn from the literature, that we will use. The most important assumption is that the efficiency with which jets are produced is an increasing function of spin. In Section 3 we test the spin paradigm and show that under our assumptions we can explain the observed range in ‘radio-loudness’ of quasars.

In Section 1, we model the contribution to the local\(\dot{E}\) of jet power and accretion rate, however they do show that an extremely efficient mechanism must be powering the jets.

In theory, spinning black holes can reach nominal jet efficiencies greater than one, since as well as drawing energy from the accreted mass, the jet draws energy from the rotation of the black hole. Hence, spin is an attractive candidate to explain the radio loudness of AGN (e.g. Blandford & Znajek 1977; Rees 1984; Psnulv & Coroniti 1990; Scheuer 1992; Wilson & Colbert 1993; Koide et al. 2002; Sikora et al. 2005). It is attractive because, in principle, it is capable of high efficiencies and in addition it provides a physical explanation for a hidden variable. This is usually referred to as the ‘spin paradigm’.

The jets are most likely powered by differential rotation of poloidal magnetic fields in the accretion disc or near the black hole. Theoretically, the spin of the black hole is therefore a promising candidate since frame dragging around spinning black holes would provide particularly strong magnetic fields and particularly fast rotation (e.g. Blandford & Znajek 1977; Prsulv & Coroniti 1990; Meier 2000; Koide et al. 2002).

However, whether the jets are really tapping the rotational energy of the black hole is still a matter of debate. Some authors argue that the power extracted in this way is at most comparable to the power generated by the inner regions of the accretion disc (Ghosh & Abramowicz 1997; Livio et al. 1994). Others argue that in the case of geometrically thick accretion discs, powerful jets can be driven by the black hole spin (e.g. Meier 2001).

In galactic black holes (GBHs), the presence of steady jets occurs typically during low accretion rates (where by low we mean an Eddington rate\(\dot{E}<0.01\), or during high accretion rates (\(\lambda\sim0.3\), e.g. GRS 1915+105, see e.g. Fender et al. 2004). The jets can be steady, transient or absent at \(\lambda\sim0.01\), depending on the accretion state. This is consistent with steady jets requiring geometrically-thick accretion flows, either ADAFs (advection-dominated accretion flows Narayan & Yi 1993) or slim discs (Abramowicz et al. 1998). However, these differences in the accretion flow are observable at X-ray energies, while as explained in the preceding paragraphs, the radio-loudness of AGN requires an extra variable parameter that is not readily observable.

In Section 2, we also introduce the different jet efficiencies, drawn from the literature, that we will use. The most important assumption is that the efficiency with which jets are produced is an increasing function of spin. In Section 3 we test the spin paradigm and show that under our assumptions we can explain the observed range in ‘radio-loudness’ of quasars.

In Section 1, we model the contribution to the local

\[\dot{E} = \frac{m \delta B}{m_{\text{IGM}}} \quad (\text{Punsly et al. 2007; McNaulara et al. 2011; Fernandes et al. 2010})\]. These results still carry considerable uncertainty in their estimates of jet power and accretion rate, however they do show that an extremely efficient mechanism must be powering the jets.
radio luminosity function (LF) of HEGs and LEGs as being composed of high-accretion rate objects (quasars or QSOs) and low-accretion rate ones (ADAFs). We allow these populations to have several different spin distributions, parametrised by three different models. Fitting to the data, and using a bayesian model selection scheme, in Section 5 we derive the spin distribution of SMBHs of mass $m_a \geq 10^8 M_\odot$ in the local Universe, and make a prediction for the $z=1$ radio LF. In Section 6, we present an estimate of the cosmic spin history of the most massive black holes from our modellng of the radio LF. Section 7 compares and discusses our inference about the spins of black holes to other results in the literature, using different methods. It includes a discussion about the lack of correlation between spin measurements and radio loudness found in GBHs. Finally, in Section 8 we discuss the implications of our result in terms of SMBH growth through accretion and mergers.

We adopt a ΛCDM cosmology with the following parameters: $h = H_0/(100 \text{ km s}^{-1} \text{ Mpc}^{-1}) = 0.7$, $\Omega_m = 0.3$, $\Omega_\Lambda = 0.7$.

2 ASSUMPTIONS

2.1 Radiative efficiency

We assume that the bolometric luminosity (due to radiation), $L_{\text{bol}}$ is given by:

$$L_{\text{bol}} = c \dot{n} c^2$$

where $\dot{n}$ is the accretion rate and $c$ the speed of light. The term $\epsilon$ is the radiative efficiency. In the classical disc picture of Novikov & Thorne (1973), hereafter NT73, $\epsilon$ is given by (one minus) the binding energy per unit mass of the ISCO, which is itself a function of the black hole spin.

Some simulations have shown that the radiative efficiency estimated by NT73 to slightly underestimate the radiative efficiency for low spins (Beckwith et al. 2008, Noble et al. 2009). On the other hand, other simulations suggest that the radiative efficiency is very close to that predicted by the NT73 model (McKinney & Gammie 2004, Shafee et al. 2008, Penna et al. 2010).

Figure 1 compares the radiative efficiency as a function of spin from the NT73 model to the results of simulations by different groups. In some cases, the results from the simulations have higher efficiencies than the NT73 model, in others they have lower efficiencies. Overall, and given the range of results from the simulations, the NT73 model is not obviously wrong.

For our work we require analytic expressions for $\epsilon(\dot{a})$ and the jet efficiency $\eta(\dot{a})$, and we will use the NT73 approximation for $\epsilon(\dot{a})$. Figure 1 suggests this is an acceptable approximation. This paper is concerned with variations in jet powers that span orders of magnitudes, and the ~2 uncertainty in $\epsilon$ has only a small effect on our results. Indeed the uncertainties in the jet efficiencies discussed in Section 2.2 are far larger than this.

We are also neglecting the fraction of energy advected into the hole (in excess of the energy of the ISCO). This is a reasonable assumption for SMBHs with Eddington rates in the range $10^{-2} \leq \lambda \leq 1$. Accretion rates with higher or lower Eddington ratios will tend to have a large fraction of the energy advected into the hole (Narayan & Yi 1995, Beloborodov 1998). Throughout this paper we will only require to use the radiative efficiency for quasars, not for ADAFs. Quasars have typically $0.1 \leq \lambda \leq 1.0$ (McLure & Dunlop 2004), and hence neglecting the advected energy is a reasonable approximation.

2.2 Jet efficiencies

We assume the power available for the production of jets can be approximated by:

$$Q_{\text{jet}} = \eta(\dot{a})\dot{n} c^2$$

where $Q_{\text{jet}}$ is the jet power, while $\eta$ is the jet efficiency and we make the assumption that it is only a function of spin.

Our definition of the jet efficiency is the same as that of Merloni & Heinz (2008) and Shankar et al. (2008). The main conceptual difference is that we assign it to black hole spin and use the theoretical results from the literature. We note that our method is different to that of Daly (2009), since that work assumes the jet power to depend on black hole spin and mass, rather than spin and accretion rate.

It is beyond the scope of this work to discuss in detail the physics of jet formation around spinning black holes. We use recent jet efficiencies from the literature, and refer the reader to that work for the details and assumptions (we list these in the following paragraph and in Table 1). However, we do outline some of the key aspects and limitations of these efficiencies and how they can affect the results of our work.

The models we will be using are from Tchekhovskoy et al. (2010) hereafter T10 (we will actually use two separate results: T10A and T10B), Benson & Balbus (2009, BB09), Nemmen et al. (2007, N07), Hawley & Krolik (2006, HK06) and McKinney (2003, M05). In figures and tables they will be listed in reverse chronological order. Their dependence on the spin $\dot{a}$ is shown in Figure 2.

Assuming an efficiency which is solely a function of spin is undoubtedly a simplification which sweeps many issues
under the carpet. One such issue is the possible dependence of accretion rate with spin, which we assume is small enough to have no significant effect (note that the efficiencies from simulations, M05 and HK06, will have this effect included).

Additionally, variations in the magnetic field geometry can lead to similar accretion flows producing very different jets (M05 [Beckwith et al. 2008a]), another effect that we are not able to take into account here, other than by considering a variety of different jet efficiencies.

Another effect that has been neglected is the effect the thickness of the accretion disc will have on the jet power, which has been discussed in detail in the literature (e.g. Ghosh & Abramowicz 1997; Livio et al. 1999; Meier 2001, T10).

On the one hand, it has been argued that thicker discs can sustain stronger poloidal magnetic fields and hence lead to more powerful jets (e.g. Livio et al. 1999; Meier 2001). On the other hand M05 and T10 argue that thick discs cover a large fraction of the area of the black hole, so that the
energy outflowing from this area will go to the accretion disc and not into the jet. For this reason, M05 makes a difference between “total” and “jet” powers. T10 assume the magnetic flux through the black hole is constant, not higher than M05, despite having a similar disk thickness, a magnetic pressure that is typically (but not always) lower than the jet. For this reason, the accretion rates from their simulations have maximum spins a = 0.99, therefore covering a wide range of disc thickness. In this paper we will concern ourselves mainly with two types of AGN: those at very low Eddington ratios (ADAFs) and those at very high ones (quasars). The jet efficiencies used here are derived from accretion flows with typical aspect ratios h/r ≃ 0.17–0.33. Assuming a viscosity parameter α = 0.3. These aspect ratios are taken from De Villiers et al. (2003). 2. Using an efficiency derived for accretion flows with negligible cooling. While this appears as a major shortcoming for black holes with high Eddington rates, we believe it is still a useful approximation. The higher accretion rates are already considered in the m term. The worry is then if the jet efficiency is appropriate for an accretion flow with a high λ. As mentioned earlier, the aspect ratio is believed to be an important factor in determining the jet power. The jet efficiencies used here are derived from accretion flows with typical aspect ratios 0.17 ≤ h/r ≤ 0.9, therefore covering a wide range of disc thickness. In this paper we will concern ourselves mainly with two types of AGN: those at very low Eddington ratios (ADAFs) and those at very high ones (quasars). Equation (2) is appropriate for ADAFs, but an important fact is that the accretion flows in quasars are radiation-pressure dominated, not gas-pressure dominated, and will have typical aspect ratios h/r ∼ λ (NT73, Abramowicz et al. 1988). For quasars, λ ∼ 0.25 (McLure & Dunlop 2004) so that the aspect ratio h/r ∼ 0.25. Hence the thickness of the two types of flow are similar. This is the reason we make the assumption that the jet efficiencies η shown in Figure 2 can be used for both quasars and ADAFs.

It is immediately clear that η can differ significantly from model to model, which will affect quantitatively our results. However, given that in all of these cases η increases with increasing spin a, our results will be qualitatively the same for different assumed jet efficiencies.

We stress that all the jet efficiencies have assumptions and limitations. We believe that showing the results for six different jet efficiencies from the literature is the most informative way of presenting our results. Now that our assumptions have been clearly stated, we proceed to compare the results to observations.

### Table 1

<table>
<thead>
<tr>
<th>Shortname</th>
<th>Reference</th>
<th>h/r</th>
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</tr>
<tr>
<td>T10B</td>
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<tr>
<td>BB09</td>
<td>Benson &amp; Babul (2009)</td>
<td>0.35–0.45</td>
</tr>
<tr>
<td>N07</td>
<td>Nemmen et al. (2007)</td>
<td>0.9</td>
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<tr>
<td>HK06</td>
<td>Hawlev &amp; Krolik (2006)</td>
<td>0.18–0.4</td>
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<tr>
<td>M05</td>
<td>McKinney (2005)</td>
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### 3 THE RADIO LOUDNESS OF QUASARS

A necessary test of our parametrisation is whether it can produce the range in radio loudness observed amongst quasars. Quasars are SMBHs with black holes of m_{\text{s}} ≥ 10^8 M⊙ accreting close to the Eddington limit (e.g. De Villiers et al. 2003).
McLure & Dunlop (2004). For a given optical luminosity, a proxy for bolometric luminosity in unobscured objects, quasars are found to have a vast range of radio luminosities. Most of the quasars are found at the ‘radio-quiet’ end, where the ratio of radio to optical luminosity density is \( \leq 10 \). However, a small fraction show radio luminosities up to 1000 times larger, and it has been suggested that spin is the hidden variable dominating this scatter (e.g. Scheuer 1992; Wilson & Colbert 1995; Sikora et al. 2007).

3.1 Estimating observable quantities

We use Equations 1 and 2 to predict the observed properties associated with quasars, and test these against the sample of quasars studied by Cirasuolo et al. (2003). The accretion rates for our predictions are given by:

\[
\dot{m}c^2 = \frac{L_E \lambda m_8}{\epsilon}
\]

(3)

where \( L_E \) is the Eddington-rate luminosity, \( 1.3 \times 10^{38} \) W per solar mass, \( m_8 \) is the black hole mass, and the bolometric luminosity \( L_{bol} \) is given by \( L_{bol} = L_E \lambda m_8 \). Typical values for quasars are \( m_8 \geq 10^8 M_\odot \), \( \lambda \sim 0.3 \) (e.g. McLure & Dunlop 2004), so that \( L_{bol} \sim 4 \times 10^{38} \) W and \( \dot{m} \sim 0.7 M_\odot \) yr\(^{-1} \).

To convert from bolometric luminosity, \( L_{bol} \), to B-band monochromatic luminosity, \( L_{\nu B} \), we use:

\[
L_{\nu B} = C_{\nu B} \nu B L_{\nu B}
\]

(4)

where, in the B band, \( \nu B \) is the frequency and \( C_{\nu B} \) is the bolometric correction that converts from the monochromatic luminosity to bolometric luminosity. Here we use the bolometric corrections from Hopkins et al. (2007).

To convert \( Q_{jet} \) to \( L_{151} \), we use the conversion given by Miller et al. (1993) for radio-quiet quasars and Willott et al. (1999) for radio-loud quasars:

\[
\frac{Q_{jet}}{W} = 3 \times 10^{38} f^{1/2} \left( \frac{L_{151}}{10^{28} \text{Whz}^{-1}\text{sr}^{-1}} \right)^{1/2}
\]

(5)

The term \( f \) represents the combination of several uncertainty terms when estimating \( Q_{jet} \) from \( L_{151} \), which includes for example the filling factor in the lobes, departure from minimum energy, and the fraction of energy in non-radiating particles.

The plausible range of values for \( f \) has been estimated to be \( 1 \leq f \leq 20 \) by Willott et al. (1999, for details see Section 4 of their work). An independent method of estimating jet power from the radio luminosity has been developed by estimating the energy stored in X-ray cavities in the intra-cluster medium (Birzan et al. 2004, Cavagnolo et al. 2010). Cavagnolo et al. (2010) find that \( f=20 \) is required for both methods to agree.

For the remainder of this paper, we will therefore use a value of \( f=20 \), which means the jet powers estimated using the relations of Willott et al. (1999) and Cavagnolo et al. (2010) agree within their uncertainties. However, we note that the studies of Birzan et al. (2004) and Cavagnolo et al. (2010) consisted mostly of sources of moderate radio luminosity. Sources with higher radio luminosities might have typically lower values of \( f \), close to 1, as we discuss below.

The value of \( f=20 \) assumes a large contribution from non-radiating particles (\( \sim 200 \) times more energy in non-radiating particles than in radiating ones, see Section 4 of Willott et al. 1999). A large fraction of non-radiating particles can be inferred observationally if the pressure provided by radiating particles inside the lobes (derived from minimum energy arguments) is much lower than the external pressure acting on the lobes due to the intra-cluster gas. In this case the extra pressure must be provided by particles that are not emitting synchrotron radiation. There exist cases where the pressure from radiating particles is comparable to the external pressure, so that the fraction of non-radiating particles is small. In those cases \( f=1 \) is more appropriate (see Croston et al. 2008, and Figure 2 of Cavagnolo et al. 2010). From studies of the cavities in the intra-cluster medium, it seems possible that the sources that are found to have low jet powers for a given radio luminosity have a lower content of non-radiating particles, due to a lower entrainment of external material by the jets. (Croston et al. 2008, Cavagnolo et al. 2010).

Fewer detailed studies exist of the more powerful radio sources, since these are rare in the nearby Universe. However, some studies suggest the fraction of non-radiating particles is small in these cases (Croston et al. 2004). This is possibly due to the fact that the most powerful radio sources, Fanaroff & Riley (1974) class II objects, have strong bow shocks that push back the intergalactic medium so that entrainment is minimal. In these objects, a value of \( f=1 \) might be more appropriate in this case (Croston et al. 2004). The arrows shown in Figure 3 show how the curves would move if \( f \) were changed from \( f=20 \) to \( f=1 \).

Source-to-source variations are likely important, as reflected by the scatter between jet power and radio luminosity (Birzan et al. 2004, Cavagnolo et al. 2010). However, there might be systematic variations with luminosity, with the high-radio luminosity sources having a lower fraction of non-radiating particles, and hence requiring a lower value of \( f \). In such cases, assuming \( f=20 \) will systematically underestimate the radio luminosity that can be produced for a given jet power. For a given jet power, \( L_{151} \propto f^{-1/2} \), meaning that changing \( f \) from 20 to 1 would increase the radio luminosity by practically 2 dex (see the arrow on Figure 3).

Since the comparison data is at 1.4 GHz, we convert from 151 MHz assuming a single power law \( L_{\nu} \propto \nu^{-\alpha} \) assuming a spectral index of \( \alpha = 0.75 \).

3.2 Comparison of the models to the data

Figure 4 shows the loci of radio luminosity density versus optical luminosity density from our assumptions in Section 2 and Equations 3, 4, and 5. Each panel assumes the jet efficiencies of Figure 2 in the same order. We have plotted two tracks for each jet efficiency: one for \( \dot{a}=0.1 \) (dotted line) and another for \( \dot{a}=0.998 \) (dashed line). The cutoff maximum spin is somewhat arbitrary, but our choice is motivated by the theoretical maximum value predicted by Thorne (1974).

The black points are the data for the quasars studied by Cirasuolo et al. (2003), who matched two samples of optically selected quasars (the 2dF QSO redshift survey and the large bright quasar survey Croo et al. 2001, Hewett et al. 1995, to the FIRST radio survey Becker et al. 1993). The sensitivity of the FIRST survey is low enough that several decades of radio loudness can be explored, yet the sample is probably incomplete below radio luminosity densities of

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Figure 3. Radio vs optical luminosity densities for a sample of $0.35 \leq z \leq 2.1$ quasars. These were selected by matching an optically-selected sample of quasars to a survey at 1.4 GHz (Cirasuolo et al. 2003). Only sources with large enough radio luminosities to make the radio flux density cut make it into the sample, so that it is not complete below $\sim 10^{24}$ W Hz$^{-1}$ sr$^{-1}$. The accretion rates are estimated from Equation 3 for the range $3 \times 10^6 \leq \lambda m \leq 3 \times 10^9$ M$_\odot$. The dotted and dashed lines show the resulting tracks for spins $\hat{a} = 0.0$ and 0.998 respectively, using the jet efficiencies $\eta$ plotted in Figure 2. The cross shows the 95% confidence interval for the assumed bolometric corrections (horizontal line) and the effect of varying the radio spectral indices in the range $0.25 \leq \alpha \leq 1$ (vertical line). The arrow shows the effect on the tracks of changing $f$ from 20 to 1. The lower dash-dotted horizontal line represents the radio luminosity from a starburst forming massive stars at a rate of 1000 M$_\odot$ yr$^{-1}$ (for stars more massive than $\geq 5$ M$_\odot$ only, Condon 1992). This corresponds to a total star-formation rate of $\sim 4000$ M$_\odot$ yr$^{-1}$ assuming a Salpeter initial mass function. The upper dash-dotted line shows the FRI/FRII divide (Fanaroff & Riley 1974).

$L_{\nu,1.4} \sim 10^{24}$ W Hz$^{-1}$ sr$^{-1}$ (as noted by Cirasuolo et al. 2003).

The data show three main features: a high-radio luminosity envelope, a low-radio luminosity envelope, and as a result of the difference between these two, a scatter of $\sim 3$ dex. The high-luminosity envelope is not a selection effect but the lower envelope might well be due to incompleteness below $L_{\nu,1.4} \sim 10^{24}$ W Hz$^{-1}$ sr$^{-1}$.

Given a maximum achievable jet efficiency, $\eta(\hat{a}\sim 1)$, Equations 2 and 1 do predict an upper envelope showing a
correlation between radio and optical luminosity, \(Q_{\text{jet}} \propto m_\text{in}\). The exact location of the envelope, however, depends on the model assumed for \(\eta\), and different models reproduce the data in Figure 3 with varying degrees of success.

The BB09 model and HK06 produce upper envelopes in reasonable agreement with the data (although we stress the caveats mentioned in Section 2.2). The agreement is not perfect and some sources appear \(\sim 1\) dex higher than the curves. However, given the uncertainties in converting from bolometric to monochromatic luminosity, from jet power to radio luminosity density and the uncertainties in the actual radio spectral indices, we do not consider this discrepancy a worry.

The T10A and N07, efficiencies produce upper envelopes that are significantly lower. This is because the maximum efficiency these two models reach is \(\eta \sim 0.2-0.3\), while the most powerful radio-loud quasars and radio galaxies require jet efficiencies \(\gtrsim 1\) (Frusciante 2007; McNamara et al. 2011; Fernandes et al. 2010). Therefore, any model or simulation that does not reach such high values will not be able to reproduce the upper envelope (see also Frusciante 2010). This is the case for the T10B and M05 models, which produce even lower tracks.

However, we remind the reader that in Section 3.1 we have assumed a value of \(f = 20\) when converting from jet power to radio luminosity density. This implies a large component of non-radiating particles. The arrows shown in Figure 3 show how the curves would move if \(f\) were changed from \(f = 20\) to \(f = 1\). As discussed in Section 3.1, it is possible that the most powerful radio sources systematically require lower values of \(f\). For \(f = 1\), the high-spin tracks for T10A, N07 and HK06 will easily produce high enough radio luminosities, the BB09 will predict far too much radio luminosity for \(\dot{a} \sim 1\), and the T10B and M05 high spin tracks will be high enough to match the upper envelope.

The upper envelope can also explain the result of Rawlings & Saunders (1991), who found a linear correlation between jet power and narrow-line luminosity (\(L_{\text{NL}}\), an isotropic proxy for \(L_{\text{bol}}\) for radio-loud AGN (their work assumed \(f = 2\) to convert from radio luminosity to jet power). If we assume \(L_{\text{NL}} \sim 500 - 1000 \times L_{\text{NL}}\), our curves with maximum efficiencies \(\eta \sim 0.1-1.0\) can also explain the data of Rawlings & Saunders (1991) as an approximate upper envelope. Sergeant et al. (1998) found an upper envelope for the radio luminosity density versus optical magnitude of steep-spectrum quasars, and argued it was not due to any selection effects or relativistic beaming. A similar envelope is also found between infrared luminosity density (another approximately isotropic estimator of \(L_{\text{bol}}\)) and low-frequency radio luminosity density for radio-selected AGNs, an envelope that can again be reasonably reproduced by our curves (Fernandes et al. 2010).

The minimum jet efficiency, \(\dot{a} = 0\), from HK06, N07 and BB09 predict lower envelopes, which appear in good agreement with the data. However, as Cirasuolo et al. (2003) point out, the sample of quasars might be incomplete below \(L_{\nu,14} \sim 10^{24}\) W Hz\(^{-1}\) sr\(^{-1}\), so that the agreement between the lower envelope and the data might be fortuitous. Again, the uncertainties when converting \(L_{\text{bol}}\) and \(Q_{\text{jet}}\) into \(L_{\text{B}}\) and \(L_{\nu,151}\) are large (see Figure 3), so that quasars with slightly lower radio-to-optical luminosity density ratios are not strictly in disagreement with our curves.

The fact that in the the M05, T10A and T10B models \(\eta \rightarrow 0\) as \(\dot{a} \rightarrow 0\), means that they do not have a lower envelope, but this is not in disagreement with current data, as explained above. The existence of a possible lower envelope requires further studies using deep radio observations of powerful quasars.

Discriminating whether this lower envelope is a real physical effect or just a selection effect, is further complicated by the fact that very powerful starbursts, with massive star-formation rates \(\sim 1000\) M\(_\odot\) yr\(^{-1}\) (for stars \(\geq 5\) M\(_\odot\)), which would correspond to a total star-formation rate of \(\sim 4000\) M\(_\odot\) yr\(^{-1}\) for a Salpeter initial mass function), can show radio luminosity densities as high as \(\sim 3 \times 10^{23}\) W Hz\(^{-1}\) sr\(^{-1}\) without the presence of an AGN (this is shown by the bottom horizontal line in Figure 6, following Condon 1992).

### 3.3 Implications for AGN

Also overplotted on Figure 3 is the divide between Fanaroff-Riley class I and class II objects (Fanaroff & Riley 1974, hereafter FRI and FRII sources). FRI and FRII sources have powerful extended jets, and the bulk of the quasars in the figure lie around or above the FRI/FRII divide. This suggests that extended jets are common around quasars, and indeed the common assumption that quasars were never associated with FRI-type jets has been proven false (see Blundell & Rawlings 2001; Heywood et al. 2007).

Miller et al. (1993) also found that many of the brightest optically-selected quasars at 0.3 \(\leq z \leq 0.5\) were FRII sources, and the high jet powers inferred by Cao & Rawlings (2004) for powerful nearby FRIs (\(>10^{36}\) W) seem difficult to reach without high accretion rates.

Turning this around, even with a high spin, no AGN with a low radiative luminosity is expected to show FRII luminosities (and presumably by extension no FRI jet structures either). For example, the FRI/FRII division is at a radio luminosity of \(\sim 2 \times 10^{25}\) W Hz\(^{-1}\) sr\(^{-1}\), which corresponds to \(Q_{\text{jet}} \sim 1.3 \times 10^{38}\) W (assuming \(f = 20\)). Even with jet efficiencies as high as \(\eta \sim 0.5\), this still requires an accretion rate of \(0.05\) M\(_\odot\) yr\(^{-1}\), which can only be achieved by SMBHs with \(\lambda M_\text{BH} \gtrsim 3 \times 10^7\) M\(_\odot\). This is the typical value for optically-selected quasars (McLure & Dunlop 2004), and corresponds to moderate to high Eddington rates for black hole masses \(\sim 3 \times 10^9\) M\(_\odot\), and only corresponds to modest Eddington rates for the rare black holes with masses \(\gtrsim 3 \times 10^9\) M\(_\odot\). This explains why FRII sources are mostly associated with HEG spectra, and only sometimes with LEGs spectra, while FRIs which can be associated with both HEG or LEG spectra (e.g. Ledlow & Owen 1996; Blundell & Rawlings 2001; Hardcastle et al. 2006).

Section 5 describes this quantitatively.

An upper limit on the observed radio luminosity density, \(L_{\nu,151}\), can be estimated by assuming \(\eta_{\text{max}} \sim 1\), \(\epsilon_{\text{max}} \sim 0.3\) as well as \(\lambda_{\text{max}} \sim 1\) and \(m_{\text{max}} \sim 3 \times 10^9\) M\(_\odot\). This yields maximum values of \(Q_{\text{jet,max}} \sim 10^{31}\) W, and \(L_{\nu,151,max} \sim 5 \times 10^{28}\) W Hz\(^{-1}\) sr\(^{-1}\) or \(L_{\nu,151,max} \sim 1 \times 10^{27}\) W Hz\(^{-1}\) sr\(^{-1}\). No radio galaxy observed so far has a radio luminosity significantly above this value (e.g. Rawlings & Saunders 1991; Wilott et al. 1999).

We now proceed to test whether under reasonable assumptions the spin paradigm can explain the different con-
troductions to the local radio LF from AGN with high and low accretion rates (HEGs and LEGs, respectively).

4 MODELLING THE LOCAL RADIO LUMINOSITY FUNCTION

We proceed to fit the local radio LF of LEGs and HEGs to find the distribution of spins that best describes each subpopulation. The best-fitting parametrisation allows us to interpret the physical conditions that lead to the spin distribution, it can be used to derive an estimate of the spin history of SMBHs.

Above $L_{21.4} \geq 10^{23}$ W Hz$^{-1}$ sr$^{-1}$, all the sources contributing to the radio LF have $m_* \geq 10^8$ $M_\odot$ (e.g. McLure et al. 2004; Smolčić et al. 2009). We will therefore limit our discussion to SMBHs with $m_* \geq 10^8$ $M_\odot$. The radio luminosity is determined from the jet power $Q_{\text{jet}}$ (see below), which from Equation 2 depends on the jet efficiency, $\eta$ as well as the accretion rate, $\dot{m}$.

Throughout this section we follow the convention that the sign $\phi(L)$ refers to a luminosity function while the sign $P(x)$ refers to a normalised probability distribution function (PDF):

$$\int P(x)dx = 1$$

Luminosity functions are PDFs that are not normalised to unity, but rather to a space density. Hence we will manipulate LFs in an analogous way to PDFs (note that in practice all the integrals are done using base-10 logarithms).

Assuming that the jet efficiency is essentially a monotonic function of spin, the PDF for jet efficiencies is related to the PDF for spins by:

$$P(\eta) d\eta = P(\dot{m}) d\dot{m}$$

The space density of sources with a given radio luminosity density $L_o$ is related to the space density of sources with a given jet power $Q$, via:

$$\phi(L_o) dL_o = \phi(Q) dQ.$$  

From Equation 2 the distribution of jet powers will depend both on the distribution of accretion rates and spins. The PDF of a given jet power $Q$ can be thought of as the probability of $Q$ and an accretion rate $\dot{m}$ and an efficiency $\eta$, marginalised over the ‘nuisance’ parameters $\dot{m}$ and $\eta$.

$$P(L_o) = \frac{dQ_{\text{jet}}}{dL_o} P(Q_{\text{jet}})$$

$$= \frac{dQ_{\text{jet}}}{dL_o} \int \int P(Q_{\text{jet}}, \dot{m}, \eta) d\dot{m} d\eta$$

Using Bayes’ theorem, we can write this in terms of the PDF of $Q$ given $\dot{m}$ and $\eta$ and the PDFs of $\dot{m}$ and $\eta$.

$$P(Q_{\text{jet}}, \dot{m}, \eta) = P(Q_{\text{jet}}|\dot{m}, \eta) P(\dot{m}, \eta)$$

For a given accretion and jet efficiency, only one value of the jet power is possible, so that the probability of $Q_{\text{jet}}$ given $\dot{m}$ and $\eta$ is a delta-function:

$$P(Q_{\text{jet}}|\dot{m}, \eta) = \delta(Q_{\text{jet}} - \eta \dot{m} c^2) ,$$

and hence

$$\int \int P(Q_{\text{jet}}|\dot{m}, \eta) P(\eta, \dot{m}) d\dot{m} d\eta$$

$$= \int \int \delta(Q_{\text{jet}} - \eta \dot{m} c^2) P(\eta, \dot{m}) d\dot{m} d\eta$$

$$= \int P(\eta, \dot{m} | Q_{\text{jet}} = \eta \dot{m} c^2) d\eta$$

For a particular class of objects, we make the approximation that the spin is independent from the instantaneous accretion rate, so that:

$$P(\eta, \dot{m}) = P(\eta) P(\dot{m}).$$

The space density of sources with a given radio luminosity is therefore given by:

$$\phi(L_o) = \frac{dQ_{\text{jet}}}{dL_o} \int P(\eta) P(\dot{m}) d\eta$$

$$= \frac{dQ_{\text{jet}}}{dL_o} \int P(\dot{a}) P(\dot{m}) d\dot{a}$$

We model the LEGs and HEGs separately, and we begin with the HEGs.

4.1 High-accretion rate radio galaxies

The HEGs are modelled by SMBHs with high accretion rates, which we refer to as QSOs for simplicity. The space density of SMBHs with a given accretion rate can be estimated from the X-ray LF, since the X-ray luminosity can be used to estimate the bolometric luminosity via

$$L_{\text{bol}} = C_X L_X$$

where $C_X$ is the bolometric correction at X-ray energies. Hence, the accretion rate $\dot{m}$ can be estimated as:

$$\dot{m} = \frac{C_X L_X}{\epsilon c^2}.$$  

The space density of HEGs with a given radio luminosity is therefore:

$$\phi_{\text{QSO}}(L_o) = \frac{dQ_{\text{jet}}}{dL_o} \int P_{\text{QSO}}(\dot{a}) P(L_o) \frac{dL_X}{d\dot{m}} d\dot{a}$$

To avoid including SMBHs with $m_* < 10^8$ $M_\odot$, we impose a minimum bolometric luminosity of $L_{\text{bol}} \geq 3 \times 10^{38}$ W. This can only be achieved by SMBHs with $m_* \geq 10^8$ $M_\odot$ at 25% of the Eddington luminosity (the characteristic value found by McLure & Dunlop 2004).

Assuming typical bolometric corrections, this corresponds to an X-ray luminosity of $9 \times 10^{36}$ W. We have also limited the upper X-ray luminosity to $\lesssim 1 \times 10^{39}$ W since no sources brighter than this have been observed (e.g. Silverman et al. 2008).

The X-ray LF of Silverman et al. (2008) is selected in the hard band (2-8 keV), meaning it is sensitive to unabsorbed and moderately absorbed sources (with column densities $N_H \leq 10^{25}$ m$^{-2}$ and $10^{26}$ m$^{-2} \leq N_H \leq 10^{28}$ m$^{-2}$, respectively). However, sources with column densities $\geq 1.5 \times 10^{28}$...
\( \text{m}^{-2} \) are optically-thick to Compton scattering (‘Compton-thick’) and will be missed by the X-ray LF.

In the X-ray luminosity range of interest, \( 9 \times 10^{36} \text{ W} \leq L_X \leq 1 \times 10^{39} \text{ W} \), approximately half of the hard X-ray sources are unabsorbed and the other half are absorbed but Compton thick. The fraction of Compton-thick AGN is estimated to be similar to the fraction of Compton-thin absorbed AGN, meaning the space density of quasars given by the hard X-ray LF has to be corrected by a factor \( \sim 1.5 \) (see e.g. Risaliti et al. 1999; Gilli et al. 2007; Goulding et al. 2010). Although there might be a slight evolution in the fraction of absorbed AGN (e.g. Treister & Urry 2006; Hasinger 2008), this correction is likely still correct at high redshift (e.g. Martínez-Sansigre et al. 2007; Gilli et al. 2007; Fiore et al. 2009). We therefore multiply the space density of the X-ray LF by a factor of 1.5, to estimate the space density of all QSOs (whether hidden or not).

4.2 Low-accretion rate radio galaxies

We model the LEG component of radio LF as SMBHs with low accretion rates, which we call ADAFs. This requires some extra assumptions, since no luminosity function is available to estimate their accretion rates. However, the local mass function of supermassive black holes, hereafter BHMF, provides the distribution of masses, which can be related to the distribution of accretion rates via a distribution of Eddington ratios:

\[
P(\dot{m}) = \int P(\dot{m}, m) dm
\]

\[
= \int P(\dot{m}|m)P(m) dm
\]

\[
= \int P(\lambda) \frac{d\lambda}{d\dot{m}'} P(\dot{m}') dm
\]

(19)

We have expressed the conditional probability of an accretion rate given a black hole mass, \( P(\dot{m}|m) \), as a probability of an Eddington ratio \( P(\lambda) \).

The radio LF due to ADAFs can therefore be modelled as:

\[
\phi_{\text{ADAF}}(L_\nu) = \frac{dQ_{\text{jet}}}{dL_\nu} \int P_{\text{ADAF}}(\dot{\lambda}) \int P(\lambda) \phi(m) \frac{d\lambda}{d\dot{m}'} d\dot{m}' d\dot{\lambda}
\]

(20)

Given our ignorance about the distribution of Eddington ratios, we choose a prior PDF which is flat in logarithmic space, known as a Jeffreys prior:

\[
P(\lambda) \propto \frac{1}{(\lambda_{\text{max}} - \lambda_{\text{min}})}
\]

(21)

We assume the ADAFs are described by SMBHs accreting at Eddington ratios in the range \( 10^{-8} \leq \lambda \leq 10^{-2} \), hence \( \lambda_{\text{max}}=10^{-2} \) and \( \lambda_{\text{min}}=10^{-8} \).

4.3 Model selection for the spin distribution

We now proceed to use the data from the observed local radio LF of LEGs and HEGs to constrain the spin distribution. Three models are considered.

Model A consists of a power law PDF for the spin:

\[
P_\lambda(\dot{\lambda}) = N_\lambda \dot{\lambda}^{-p}
\]

(22)

The power law index \( p \) is the only free parameter in this model, and it is given a flat prior PDF in the range \(-4 \leq p \leq 4 \). \( N_\lambda \) is simply a normalisation constant.

The next model, B, is a single gaussian distribution:

\[
P_B(\dot{\lambda}) = N_B e^{-\frac{1}{2} \left( \frac{\dot{\lambda} - \mu_B}{\sigma_B} \right)^2}.
\]

(23)

We fix \( \sigma_B=0.05 \) and \( N_B \) is the normalisation term, so this model has also only one free parameter, \( \mu_B \), to which we assign a flat prior in the range \( 0 \leq \mu_B \leq 1 \).

The value of \( \sigma_B=0.05 \) is assumed since it can provide a reasonable approximation to the width of the spin distributions expected to arise from accretion onto SMBHs as well as from major mergers (see Section 8). Note that if \( \mu_B \) is close to one edge, the PDFs will be truncated, so we calculate the normalisation term numerically, rather than using the analytic value of \( N_B = 1/\sigma_B \sqrt{2\pi} \).

Model C consists of two gaussians distribution with variable relative height:

\[
P_C(\dot{\lambda}) = N_C \left[ H_{\text{C1}} e^{-\frac{1}{2} \left( \frac{\dot{\lambda} - \mu_{\text{C1}}}{\sigma_{\text{C1}}} \right)^2} + e^{-\frac{1}{2} \left( \frac{\dot{\lambda} - \mu_{\text{C2}}}{\sigma_{\text{C2}}} \right)^2} \right].
\]

(24)

There are three free parameters: the two mean spins \( \mu_{\text{C1}} \), \( \mu_{\text{C2}} \) as well as the relative height of the first gaussian, \( H_{\text{C1}} \) which we call ADAFs. This requires some extra assumptions, since no luminosity function is available to estimate their accretion rates. However, the local mass function of supermassive black holes, hereafter BHMF, provides the distribution of masses, which can be related to the distribution of accretion rates via a distribution of Eddington ratios:

\[
P(\dot{m}) = \int P(\dot{m}', m) dm
\]

\[
= \int P(\dot{m}|m)P(m) dm
\]

\[
= \int P(\lambda) \frac{d\lambda}{d\dot{m}'} P(\dot{m}') dm
\]

(19)

We have expressed the conditional probability of an accretion rate given a black hole mass, \( P(\dot{m}|m) \), as a probability of an Eddington ratio \( P(\lambda) \).

The radio LF due to ADAFs can therefore be modelled as:

\[
\phi_{\text{ADAF}}(L_\nu) = \frac{dQ_{\text{jet}}}{dL_\nu} \int P_{\text{ADAF}}(\dot{\lambda}) \int P(\lambda) \phi(m) \frac{d\lambda}{d\dot{m}'} d\dot{m}' d\dot{\lambda}
\]

(20)

Given our ignorance about the distribution of Eddington ratios, we choose a prior PDF which is flat in logarithmic space, known as a Jeffreys prior:

\[
P(\lambda) \propto \frac{1}{(\lambda_{\text{max}} - \lambda_{\text{min}})}
\]

(21)

We assume the ADAFs are described by SMBHs accreting at Eddington ratios in the range \( 10^{-8} \leq \lambda \leq 10^{-2} \), hence \( \lambda_{\text{max}}=10^{-2} \) and \( \lambda_{\text{min}}=10^{-8} \).
The integral of the likelihood over the parameter space \{x_1, \ldots, x_n\} yields the ‘evidence’, \(P(\text{model}|\text{data})\):

\[
P(\text{data}|\text{model}) = \int P(\{x_1, \ldots, x_n\}) P_{\text{total}}(\text{model}|\{x_1, \ldots, x_n\}, \text{data}) d^n x,
\]

and Bayes’ theorem allows us to infer the probability of the model given the data:

\[
P(\text{model}|\text{data}) = \frac{P(\text{data}|\text{model}) P(\text{model})}{P(\text{data})}.
\]

Where \(P(\text{model})\) is the prior for a model. When comparing two models, the denominator can be eliminated by taking the ‘odds ratio’, \(P(\text{model}\_1|\text{data})/P(\text{model}\_2|\text{data})\).

\[
P(\text{model}\_1|\text{data})/P(\text{model}\_2|\text{data}) = \frac{P(\text{data}|\text{model}\_1) P(\text{model}\_1)}{P(\text{data}|\text{model}\_2) P(\text{model}\_2)}.
\]

Hence, using the odds ratio, we can compare two models at a time, and keep the model which fares best agains the others. In Equation 28 the integral over the parameter space, and the priors \(P(\{x_1, \ldots, x_n\})\) penalise the use of extra parameters as well as the exploration of parameter space with a low likelihood. Hence, models with different number of parameters can be compared in a fair way.

Finally, we use the different jet efficiencies \(\eta(\hat{a})\) described in Section 2 and shown in Figure 2. Using these jet efficiencies and our parametrisation we are able to fit the local radio LF, and Section 5 presents the results.

### Table 2

<table>
<thead>
<tr>
<th>(\eta)</th>
<th>Models</th>
<th>(\log_{10}[\text{Odds Ratio}])</th>
</tr>
</thead>
<tbody>
<tr>
<td>T10A</td>
<td>B / A</td>
<td>257</td>
</tr>
<tr>
<td>T10A</td>
<td>C / B</td>
<td>100</td>
</tr>
<tr>
<td>T10A</td>
<td>C / A</td>
<td>357</td>
</tr>
<tr>
<td>T10B</td>
<td>B / A</td>
<td>&gt;247</td>
</tr>
<tr>
<td>T10B</td>
<td>C / B</td>
<td>34</td>
</tr>
<tr>
<td>T10B</td>
<td>C / A</td>
<td>&gt;281</td>
</tr>
<tr>
<td>BB09</td>
<td>B / A</td>
<td>&gt;177</td>
</tr>
<tr>
<td>BB09</td>
<td>C / B</td>
<td>31</td>
</tr>
<tr>
<td>BB09</td>
<td>C / A</td>
<td>&gt;209</td>
</tr>
<tr>
<td>N07</td>
<td>B / A</td>
<td>&gt;261</td>
</tr>
<tr>
<td>N07</td>
<td>C / B</td>
<td>51</td>
</tr>
<tr>
<td>N07</td>
<td>C / A</td>
<td>&gt;311</td>
</tr>
<tr>
<td>HK06</td>
<td>B / A</td>
<td>&gt;161</td>
</tr>
<tr>
<td>HK06</td>
<td>C / B</td>
<td>3</td>
</tr>
<tr>
<td>HK06</td>
<td>C / A</td>
<td>&gt;163</td>
</tr>
<tr>
<td>M05</td>
<td>B / A</td>
<td>&gt;264</td>
</tr>
<tr>
<td>M05</td>
<td>C / B</td>
<td>54</td>
</tr>
<tr>
<td>M05</td>
<td>C / A</td>
<td>&gt;319</td>
</tr>
</tbody>
</table>

Table 2. Summary of results of the model selection. Section 4.3 describes the models and the model selection method. The first column indicates the two models being compared, with the most likely model on the left. The second column shows the base-10 logarithm of the odds ratio (given by Equation 29; see Section 4.3 for more details). The right-censored results marked with a > occur due to the fact that the evidence of model A is too small for the program.

5 THE DISTRIBUTION OF SPINS FROM THE LOCAL RADIO LF

5.1 Comparison to the \(z=0\) radio LF

To constrain the best-fitting model and parameters, we use the data kindly provided by P. Best prior to publication (Best et al. 2011, in prep., from the original sample of Best et al. 2003), who have separated the local radio LF into HEGs and LEGs. These are plotted as empty triangles and filled circles, respectively, in Figure 4.

Using Equation 29 and assuming equal priors for all models, \(P(\text{model}\_1)=P(\text{model}\_2)=P(\text{model}\_C)\), we select the best model, which we find to be model C (see Table 2). We note that model C has been chosen despite the Occam factors that penalise the exploration of extra parameters.

Once we have chosen a model, the best-fitting parameters are chosen by maximising the likelihood, which is equivalent to the traditional \(\chi^2\) minimisation. We find the best-fitting parameters for SMBHs with high and low accretion rates (‘QSOs’ and ‘ADAFs’ respectively) separately, and Table 3 summarises the results. Table 4 summarises the best-fitting parameters for the rejected models.

Figure 4 shows that the best-fitting parameters can accurately reproduce the local radio LF of LEGs and HEGs in the region \(L_{1.4} > 3 \times 10^{23}\) W Hz\(^{-1}\) sr\(^{-1}\). The region \(1-3 \times 10^{23}\) W Hz\(^{-1}\) sr\(^{-1}\), is not so well fit, but a few points are worth mentioning. Although the fits look better if we only fit the region \(> 3 \times 10^{23}\) W Hz\(^{-1}\) sr\(^{-1}\), the best-fitting parameters are essentially unchanged.

Some models for the efficiencies do a remarkable job of explaining the radio LF, particularly the LEGs (e.g. BB09, HK06). Models that cannot reach very high values of \(\eta\) struggle to fit the LEGs, but can still fit the HEGs reasonably well. For example the shape of the QSO model function from M05 is almost identical to the HEG LF, although the normalisation is slightly off.
We have assumed a value of \( f = 20 \), but if we change this to \( f = 1 \) (at all radio luminosities) the T10B and M05 models reproduce the LEGs better, and provide a reasonable fit. In this case the M05 model requires all the spin to lie around \( \hat{a} = 0.14 \) for the HEGs, while the LEGs require a bimodal distribution (with means of \( \mu_{C1} = 0.86 \) and \( \mu_{C2} = 0.10 \)). The T10B model requires bimodal distributions for both the HEGs (0.33 and 0.00 respectively). The T10A, BB09, N07 and HK06, on the other hand, require all the probability density to lie around zero spin (both \( \mu_{C1} \) and \( \mu_{C2} = 0.00 \)) for both HEGs and LEGs). Despite the low spin values, all three models overpredict the LEGs and HEGs, and provide a very poor fit in the case of \( f = 1 \).

As was discussed in Section 3.1 the typical value of \( f \) might change systematically with luminosity. A possible improvement to our modelling would be to vary \( f \) with radio luminosity. Currently we do not wish to follow this approach since we do not have enough independent constraints, so allowing \( f \) to vary constrained only by the radio LF of HEGs and LEGs would lead to ‘fine tuning’ of parameters rather than allowing us to make inferences. The value of \( f = 20 \) is justified independently and is appropriate for the radio sources in the local Universe (see Section 3.1).

The QSO LF includes a break (due to the break in the X-ray LF) which looks similar to the break observed in the HEGs, although the normalisation is not exactly in the right place. The shape of the break in the X-ray LF is approximately preserved due to the fact that the jet efficiencies are generally shallow at the low-spin end (e.g. HK06, N07, BB09). The jet efficiencies that are steeper at the low-spin end have smoother breaks (M05, T10).

Similarly, in many models there is a break in the LEG LF. This originates in the break of the mass function, but in some models with very steep values of \( \eta \) at high spin the break is smoothed out. This is most noticeable in BB09. The observed break in the LEG radio LF is not as marked as that in the mass function since, due to their different accretion rates and jet efficiencies, SMBHs with a range of masses contribute to that region of the LEG radio LF.

We note that removing the Compton-thick correction, modelled as a 50% increase in the space density of HEGs (Section 3.1), makes no difference to our results. For all the jet efficiencies, the resulting best-fitting parameters for the HEG-QSOs are practically identical to those when including the Compton-thick sources. The only exception is for BB09: when removing the Compton-thick correction the smaller gaussian has a mean spin of 0.99 and an amplitude 0.01 relative to the gaussian with mean spin 0.00 (compare with the results in Table 3).

Overall, we consider the fits acceptable, given that they are based on a few simple physically-motivated prescriptions. We remind the reader that the uncertainties in converting jet powers to radio luminosity densities, discussed in Section 3.1 apply here equally.

Most notably, assuming \( f = 20 \) requires the models to achieve \( \eta_{\text{max}} > 1 \) in order to explain the LEGs, due to their low accretion rates but high radio luminosities. Reducing \( f \) to \( ~1 \) would mean the low-\( \eta \) models would fare much better (e.g. M05, T10B and to a certain extent N07) but then the models with high \( \eta_{\text{min}} \), such as HK06 and BB09, would overpredict the radio LF.

The exact choice of cutoff for the maximum spin also makes a difference. For example BB09 argue for lower values of maximum spin in ADAFs, and indeed if we set an upper cutoff of \( \hat{a} \approx 0.95 \) the BB09 model provides a better fit to the LEGs than for \( \hat{a} = 0.998 \).

We have only fitted the data above radio luminosity densities of \( 10^{23} \) \( \text{W Hz}^{-1} \text{sr}^{-1} \), but we can see how our best-fits fare in the lower luminosity region, where we have not fitted to the data. Figure 25 shows what our models predict in this region. Indeed, extrapolation of our model radio LFs to lower radio luminosity densities does not overpredict significantly the observed radio LFs of HEGs or LEGs.

The ADAF models provide a very good match to the LEGs in the range \( 10^{21} - 10^{23} \) \( \text{W Hz}^{-1} \text{sr}^{-1} \). There is no need for a further component to explain the LEGs: the prediction from our model is therefore that SMBHs with \( m_* \gtrsim 10^9 \text{M}_\odot \) dominate the LEG radio LF down to \( 10^{21} \) \( \text{W Hz}^{-1} \text{sr}^{-1} \).
Figure 4. The $z=0$ radio luminosity function split into high-excitation gas (HEGs, open triangles) and low-excitation gas sources (LEGs, black circles, data from P. Best, et al., in prep.). The empty squares indicate the summed radio LF. The acronyms summarise the jet efficiencies $\eta$ shown in Figure 2. The curves show the best-fitting curves from our most appropriate model (model C), chosen using the odds ratio as described in Section 4.3. The dashed line shows the radio LF modelled from high-accretion rate SMBHs (labelled QSOs, for simplicity), and is compared to the HEGs, while the dotted line shows the radio LF modelled from low-accretion rate objects (labelled ADAFs) which is compared to the LEGs. The model has three free parameters which describe the spin distribution. These parameters are fixed by comparison with the data. The figure shows how the two components of the radio LF (HEGs and LEGs) can be explained by a population of high-accretion rate SMBHs and one of low-accretion rate SMBHs, different distributions of spins.

so that any contribution from lower mass SMBHs must be small.

The QSO models do not fit the entire HEG radio LF, but an important positive result is that they do not overpredict the density of lower-radio luminosity HEGs. Indeed, an extra population is probably needed to explain the higher space density of HEGs, and these are most likely SMBHs with lower masses and moderate or low accretion rates, for example Seyfert galaxies and low-luminosity AGN (e.g. Nagar et al. 2005; Filho et al. 2006).

We can also estimate the distribution for all SMBHs, by combining the spin distributions of ADAFs and QSOs weighed by their space densities:
Figure 5. The entire observed $z=0$ radio luminosity function down to $10^{21}$ W Hz$^{-1}$ sr$^{-1}$ compared to our models with their best-fitting parameters. This figure is similar to Figure 4 but it shows a wider range in radio luminosity density. The parameters have only been fit in the region $\geq 10^{23}$ W Hz$^{-1}$ sr$^{-1}$, so we are now comparing the predictions from our best-fitting models to the observed radio LF. We can see that the ADAF models provide a very good match to the LEGs all the way down to luminosity densities of $10^{21}$ W Hz$^{-1}$ sr$^{-1}$. There is no need for a further component to explain the LEGs, so our model predicts that the LEGs down to $10^{21}$ W Hz$^{-1}$ sr$^{-1}$ are all powered by SMBHs with $m_{\bullet} \gtrsim 10^8 M_{\odot}$, with a negligible contribution from lower mass SMBHs. The models do not provide such good fits for the HEGs, indeed an extra component is required to explain the high space density of HEGs at luminosity densities $< 10^{23}$ W Hz$^{-1}$ sr$^{-1}$. The most likely explanation is that SMBHs with masses below $10^8 M_{\odot}$ and moderate accretion rates dominate this region of the HEG radio LF (these sources are typically Seyfert galaxies and low-luminosity AGN, LLAGN, e.g. Nagar et al. 2005; Filho et al. 2006).

\[ P_{\text{SMBH}}(\hat{a}) = \frac{w_{\text{QSO}}P_{\text{QSO}}(\hat{a}) + w_{\text{ADAF}}P_{\text{ADAF}}(\hat{a})}{w_{\text{QSO}} + w_{\text{ADAF}}} \]  
\[ w_{\text{ADAF}} = \sum \phi_{\text{ADAF}}(L_\nu) \]
\[ w_{\text{QSO}} = \sum \phi_{\text{QSO}}(L_\nu) \]

\[ \langle \hat{a} \rangle_{\text{SMBH}} = \int \hat{a} P_{\text{SMBH}}(\hat{a}) d\hat{a}, \]
Observational constraints on the spin of SMBHs

The inferred distribution of spins for all SMBHs are shown in Figure 6, where we have combined the distributions for QSOs and ADAFs, and weighted them by the relative modelled space densities of QSOs and ADAFs respectively. All the distributions are bimodal, although the relative importance of the two components varies greatly between different jet efficiencies (e.g. contrast HK06 and M05). Note that we weigh by the model distributions \( \phi_{\text{QSO}}(L_\nu) \) and \( \phi_{\text{ADAF}}(L_\nu) \), so that the expectation value will be most reliable for jet efficiencies that can reproduce the observations better.

For any given jet efficiency, the range of expectation values for the mean spin of all SMBHs is similar for models A and B as it is for model C (see Table 4 and Figure 6).

In Section 8 we discuss the implications of such a bimodal distribution, and compare it to theoretical predictions from accretion and mergers of SMBHs.

Interestingly, regarding the radio-loudness of quasars, our results suggest that there should be something resembling...
blending a dichotomy in radio-loudness (see Figure 2). There has been some debate regarding the existence of a dichotomy in radio-loudness (e.g. Ivezić 2002, Cirasuolo et al. 2003), but we note here that the dichotomy in spins will translate into a dichotomy in jet efficiency, which does not necessarily map linearly into a dichotomy in the ratio of radio-to-optical luminosity density (often used to define radio-loudness). The uncertainties in converting from jet power to radio luminosity density, the scatter in bolometric corrections and selection effects can all blur out such a dichotomy.

5.2 A prediction for the $z=1$ radio LF

If we assume that the individual spin distributions for ADAFs and QSOs do not change significantly up to redshift of $z=1$, then we can compare our predictions to the observed radio LF at this redshift.

We can use the observed X-ray LF, which tells us how the space density of SMBHs with high accretion rates increases with $z$. However, we need to make an extra assumption about the ADAFs, represented by the BHMF. If we assume that the space density of SMBHs accreting at very low rates has not changed significantly between $z=1$ and 0, then we can use the local BHMF, with the same distribution of Eddington ratios (this is supported observationally by the relatively constant evolution of AGN with moderate radio luminosities, see Smolčić et al. 2004).

The larger volumes probed at $z=1$, together with the strong evolution of the radio LF of FRII sources (Willott et al. 2001), mean that we are able to observe radio sources up to the highest radio luminosities, $\sim10^{26}$ W Hz$^{-1}$ sr$^{-1}$ at 1.4 GHz. Such sources have are typically FRIIs and are rarely seen in the local radio LF due to the smaller local volume.

Figure 7 shows the resulting radio LFs from the QSOs and ADAFs, compared to the observed radio LF, for the same range of radio luminosities that we have observed. We can see, that unlike at $z=0$, it is the QSOs that dominate the radio LF. The solid line in Figure 7 shows the observed radio LF at $z=1$, combining the high radio luminosity LF from Willott et al. (2001) and the low radio luminosity LF from Smolčić et al. (2009).

Our model overpredicts the radio LF in some regions, particularly around $L_r \sim10^{26}$ W Hz$^{-1}$ sr$^{-1}$. We note however, that this is an ill-constrained region of the radio LF: too faint for the samples used by Willott et al. (2001), but too rare in space density for the area covered by Smolčić et al. (2009). Indeed the apparent ‘wiggle’ is a consequence of the analytic function fitted to the radio LF by Willott et al. (2001).

The good agreement over so many decades of radio luminosity is very encouraging. Looking at the results for the different jet efficiencies, we can make the following predictions for the $z=1$ radio LF:

At radio luminosity densities $\gtrsim10^{26}$ W Hz$^{-1}$ sr$^{-1}$, the composition of the $z=1$ radio LF should comprise $\sim100\%$ HEGs. This prediction is in very good agreement with observations (Fernandes et al. 2011, in prep.). In the range $10^{23} - 10^{26}$ W Hz$^{-1}$ sr$^{-1}$, at the higher luminosities we expect the HEGs to dominate, with LEGs making up only $\sim10\%$ of the total population. We then expect the fraction of LEGs to increase rapidly with decreasing luminosity and eventually dominate. The dominance of the HEG population, unlike in the local radio LF, is due to the strong increase between $z=0$ and 1 of the comoving accretion rate onto SMBHs, which is reflected in the strong evolution in the X-ray LF (e.g. Silverman et al. 2008).

5.3 The comoving accretion rate of radio sources

Applying Equations 31, 34 and 35 to the accretion rate, rather than the spin, we can estimate the expectation value for the accretion rate onto ADAFs and onto QSOs.

Figure 9 shows the evolution of the comoving accretion rate (left panel), and the fraction of the total accretion rate onto ADAFs and onto QSOs (right panel) as a function of redshift. At $z=0$, approximately half of the accretion onto the most massive black holes is occurring via high accretion rates (in the form of QSOs), and the other half via low accretion rates (ADAFs). The fraction of accretion occurring in high-accretion rate objects increases rapidly with redshift. The right panel of Figure 9 shows our estimate, although again if the mass function of SMBH decreases significantly, the curve for ADAF will overpredict the accretion rate onto low-accretion rate sources.

Our left panel of Figure 9 is very similar to Figure 4 of Merloni & Heinz (2008). For both works, the accretion rate from QSOs is derived from the X-ray LF, so unsurprisingly the curves agree very well.

The difference lies in the density of accretion onto ADAFs, where we have assumed a distribution of Eddington ratios for the local SMBH mass function, and assumed this to stay constant with redshift. We have used de inferred distribution of spins to produce a distribution of jet efficiencies. Merloni & Heinz (2008), on the other hand, assume a fixed fiducial jet efficiency and derive the accretion rate from the radio LF.

Similarly, Shankar et al. (2008) use a sample of optically- and radio-selected AGN to derive the mean jet efficiency, together with the scatter. The resulting jet efficiency for the sample is $\sim0.01$. The sample is actually the same one used in our Section 3, so that the same caveats mentioned in Section 5.2 should be borne in mind, since the sample includes only objects which are bright enough to be detected both in the optical and radio surveys.

6 THE EVOLUTION OF THE COSMIC SPIN

In this Section we use our results from Sections 4 and 5 to infer our best estimate for the cosmic spin history of the most massive black holes. Comparison of Figures 8 and 9 shows that as the redshift increases, the fraction of SMBHs with high spin decreases.

We stress that Figure 9 assumes negligible evolution in the black hole mass function. This is probably an acceptable approximation up to $z\sim1$, but at higher redshifts we expect the space density of the most massive black holes to have decreased significantly. At higher redshifts, the distribution of SMBHs will closely match that of the HEGs alone, and most of the probability density will lie at low spins.

Before we continue, we warn of two important points. First, it is not the intention of this paper to judge the different models of jet formation around SMBHs. Second, as
discussed earlier, the quality of the fit is partly determined by our choice of $f$ factor when converting jet power to radio luminosity, and a lower value would cause the models that currently look best to overpredict the radio LF, so that some of the less-favoured models would then provide better fits (see discussion in Section 5.1).

Hence we choose to estimate the mean cosmic spin history using two sets of efficiencies. The first uses all the models independently of whether they can reproduce the radio-loudness of quasars or the local radio LF. The second will use only the four efficiencies that show some success at reproducing the observations, namely T10A, BB09, N07 and HK06. We label these as the ‘best fitting set’.

The cosmic spin of SMBHs evolves from distributions...
Figure 8. Spin distributions at $z=1$ for all SMBHs. These have been obtained in an analogous way to Figure 6, only using the X-ray LF at $z=1$. The vertical dotted lines mark once again the mean value. We have assumed the ADAFs not to evolve significantly up to $z=1$, which means we are likely to overestimate their contribution. Comparing this figure with Figure 6, we can see that the fraction of SMBHs with a high spin decreases with increasing redshift.

dominated by low spins at high redshifts, to bimodal distributions with comparable high-spin and low-spin components at low redshifts. It is the fraction of highly spinning black holes that increases with cosmic time. To quantify this, we consider the fraction of SMBHs with $\hat{a} \geq 0.5$. The fractions, or probabilities of $\hat{a} \geq 0.5$, are shown for each jet efficiency in Table 5 together with the mean fractions of all the sources, and of the best fitting set only. If we consider all the efficiencies together, the fraction of SMBHs with $\hat{a} \geq 0.5$ increases from $0.34 \pm 0.29$ at $z=1$ to $0.45 \pm 0.33$ at $z=0$. However, we believe a more accurate result is given by the best fitting set of efficiencies, T10A, BB09, N07 and HK06: in this case the fraction of SMBHs with $\hat{a} \geq 0.5$ is $0.16 \pm 0.03$ at $z=1$ and $0.24 \pm 0.09$ at $z=0$. The uncertainties are due to the variations of the fraction between different efficiencies (see Table 5). At redshifts >1 we expect the fraction of SMBHs with $\hat{a} \geq 0.5$ to be even lower than the quoted values.

Given the shape of the distribution functions, the most informative way of describing the spin history is to show the distributions and determine the fraction with high spin. A mean value does not reflect the bimodality, however, for
Observational constraints on the spin of SMBHs

6.1 The expectation value of spin with redshift

Figure 10 shows the evolution of $\langle \hat{a}(z) \rangle$ (solid line) together with the standard deviation (dashed lines). The standard deviation is measured from the square root of the variance. The large value of the variance is caused by the bimodal nature of the spin distribution at each redshift (as shown by Figures 6 and 8). Due to the fact that the spin distributions are bimodal, the expectation value should be taken simply as a fiducial value, and the exact value is clearly uncertain. However, this expectation value evolves with redshift, and we see that it was lower at $z=1$ and has slightly increased to a higher value in the present-day Universe (see Figure 10). In Section 8 we discuss the physical implications of this evolution.

6.2 A best estimate of the evolution of the mean spin

Figure 10 shows a range of different spin histories, due to the differences in the jet efficiencies from Figure 2. We wish to use all the available information, in the form of the different jet efficiencies, for a best estimate of the spin history. We consider both the entire set of jet efficiencies, as well as considering the best-fitting set alone.

To obtain the best estimate of the spin history, we take the mean of all the results as a function of redshift. However, the individual results are not always compatible. The $N$ individual results $\hat{a}_i(z)$ are compatible if $\sum_i [(\hat{a}_i(z) - \langle \hat{a}(z) \rangle)/\sigma_i]^2 \leq (N-1)$, where $\langle \hat{a}(z) \rangle$ is the mean from all the individual results (see e.g. [Press 1997]).

In order to combine incompatible results, we consider the probability that each measurement of $\hat{a}_i(z)$ is correct, as well as the probability that it is not correct. A correct measurement is one where the quoted uncertainty is accurate, whereas an incorrect measurement is quoting uncertainties that are too small or might suffer from systematics. Incorrect measurements have error bars that are too small, hence they are incompatible.

We follow the method describe by [Press 1997], and in particular their Equation 16, which gives the posterior probability for the value of $\langle \hat{a}(z) \rangle$ given data:

$$P(\langle \hat{a}(z) \rangle | \text{data}) \propto \int P(p) \prod_i [\rho P_{Ci} + (1-p)P_{ti}] dp \quad (36)$$

where $P_{Ci}$ and $P_{ti}$ are the probability distribution functions for correct and incorrect estimates, and the product $\prod_i$ is over the $n_i$ different estimates.

The first term in the square bracket is the product of the probability $p$ that measurement $i$ is correct times the probability distribution function for that measurement (using the standard deviation of the correct measurement, $\sigma_{Ci}$). The second term is the product of the probability $1-p$ that the measurement is incorrect. The probability distribution function $P_{ti}$ therefore requires a standard deviation which is large enough to make the measurement correct. We label this as $\sigma_{ti}$. The integral over $dp$ means we marginalise over both cases.

We approximate the probability distribution functions for $\langle \hat{a}(z) \rangle$ as gaussians. In the case of $P_{Ci}$, we assume the standard deviation $\sigma_{Ci}$ to given by the errors shown on Figure 10.

Table 5. Fraction of SMBHs with $\hat{a} \geq 0.5$ at $z=0$ and 1, for each of the six jet efficiencies. At the bottom we show the mean values for all the efficiencies and for the best fitting set only.

<table>
<thead>
<tr>
<th>$\eta$</th>
<th>$P(\hat{a} \geq 0.5)$ at $z=0$</th>
<th>$P(\hat{a} \geq 0.5)$ at $z=1$</th>
</tr>
</thead>
<tbody>
<tr>
<td>T10A</td>
<td>0.14</td>
<td>0.13</td>
</tr>
<tr>
<td>T10B</td>
<td>0.94</td>
<td>0.78</td>
</tr>
<tr>
<td>BB09</td>
<td>0.33</td>
<td>0.19</td>
</tr>
<tr>
<td>N07</td>
<td>0.20</td>
<td>0.13</td>
</tr>
<tr>
<td>HK06</td>
<td>0.30</td>
<td>0.17</td>
</tr>
<tr>
<td>M05</td>
<td>0.80</td>
<td>0.62</td>
</tr>
<tr>
<td>all</td>
<td>0.45±0.33</td>
<td>0.34±0.29</td>
</tr>
<tr>
<td>best fitting</td>
<td>0.24±0.09</td>
<td>0.16±0.03</td>
</tr>
</tbody>
</table>

Figure 9. Expectation value for the comoving accretion rate from QSOs and ADAFs (left panel) and relative fraction of the accretion rate (right panel), derived in an analogous way to Equations 31, 34 and Equation 35, but applied to $\dot{m}$ rather than $\dot{a}$. 

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We now consider two extreme cases:

1. There is the possibility that some of the estimates of \( \langle a(z) \rangle \) are indeed incorrect. If, however, incorrect estimates were assigned a larger uncertainty, they would become correct. How large this new uncertainty should be is somewhat arbitrary, and might vary from model to model. Hence, we assign the same very large new uncertainty to all estimates, \( \sigma_i = \sigma_1 = 1 \), and within this uncertainty all our estimates agree. We also assume a flat prior for the probability that measurements are correct, in the range \( 0 \leq p \leq 1 \), so that \( P(p) = 1 \). Equation (36) then simplifies to:

\[
\begin{align*}
P(\langle a(z) \rangle | \text{data}) = & \frac{e^{-\frac{1}{2} \sum_i (\frac{a(z_i) - \langle a(z_i) \rangle}{\sigma_{C_i}})^2}}{2 (2\pi)^{\frac{1}{2}} \prod_i \sigma_{C_i}} + \frac{e^{-\frac{1}{2} \sum_i (a(z_i) - \langle a(z) \rangle)^2}}{2 (2\pi)^{\frac{1}{2}}} \\
& \text{(37)}
\end{align*}
\]

2. The measurements are all correct, since their uncertainties are large, they are formally consistent with each other.
Figure 11. Best estimates of the evolution of the mean cosmic spin of SMBHs with redshift, derived using Equation (36). The left panel combines all the results of Figure 10 and since these are not compatible, it considers the probability that each independent estimate is correct as well as the probability that it is incorrect, and marginalises over these (see Equation 37). The definition of compatible results is given in Section 6.2. The right panel uses the results from T10A, BB09, N07 and HK06 only (the ‘best fitting set’), and since these are compatible, it considers all the independent estimates to be correct, and is simply the product of their individual posterior probability distribution functions (Equation 38). In this case a more modest spin evolution is seen between $z=1$ and 0., and note that the $-1\sigma$ and $-2\sigma$ contours fall mostly below the $\hat{a}=0$. Both estimates assume that the space density of low-accretion rate SMBHs, ADAFs described by the local black hole mass function, is constant with $z$. Since the ADAFs tend to have higher spin values, this approximation is likely to overestimate the mean spin at the high-redshift end $(z \gtrsim 1)$.

other. We therefore assign a delta-function prior at ‘certainty’, $P(p)=\delta(p=1)$ and Equation (38) simplifies instead to the standard result:

$$P(\langle \hat{a}(z) \rangle | \text{data}) \propto e^{-\frac{1}{2} \sum \left( \frac{\langle \hat{a}(z) \rangle - \langle \hat{a}(z) \rangle_0}{C_i} \right)^2}$$

(38)

Figure 11 shows the resulting evolution of $\langle \hat{a}(z) \rangle$ under these two assumptions. When combining all the results of Figure 10 some of the results are incompatible, so that we use case 1 (Equation 37). The typical spin at $z=1$ is $\hat{a}=0.35$ and increases to $\sim 0.75$ at $z=0$. The right panel of Figure 11 shows the resulting spin history when combining the T10A, BB09, N07 and HK06 results only, using case 2 and Equation 38. In this case a more modest increase is seen, from $\hat{a} \sim 0.25$ at $z=1$ to $\sim 0.35$ at $z=0$. The right panel is derived from our best fitting set, and represents our best estimate of the mean spin history.

We stress that at all redshifts, we are assuming the population of ADAFs is well represented by the $z=0$ SMBH mass function convolved with the distribution of Eddington ratios discussed in Section 6.2. This is probably a good approximation up to $z \sim 1$, since most of the mass of SMBHs with $m_\ast \gtrsim 10^8 M_\odot$ was accreted at higher redshifts. The SMBH mass function is probably similar at $z \sim 1$ and $z \sim 0$, but at $z \sim 3$ it will be significantly different. The space density of high-mass SMBHs could be much lower. Hence our inferred spin history contains too high a contribution from ADAFs at high redshifts, so that we probably overestimate the spin at $z \gtrsim 1$.

Finally, we note that although the evolution of the expectation value, $\langle \hat{a}(z) \rangle$, appears weak, this is not necessarily the best way to illustrate the evolution in spin for such bimodal distributions. The evolution in spin is stronger than what $\langle \hat{a}(z) \rangle$ would suggest: at high redshift most of the SMBHs have the spin distribution describing the QSOs so that most sources have very low spins, with a negligible fraction having high spins. At low redshift, most of the SMBHs are described by the ADAF spin distribution, meaning that around half of the sources have high spins.

It is important to note that the evolution in the spin is driven by the disappearance of high-accretion rate, low-spin SMBHs, whose space density decreases enough that the approximately constant population of low-accretion rate, high-spin objects becomes dominant.

7 COMPARISON TO OTHER INFERENCES ON BLACK HOLE SPIN

The spin of black holes in AGN have been estimated in different ways, and our results do not necessarily agree with those of other groups. For example, Elvis et al. (2002) and Wang et al. (2006) have claimed that most SMBHs must be spinning rapidly, while more recently Fender et al. (2010) have found no correlation between black hole spin and jet power for X-ray binaries. We therefore compare our results to previous work and discuss the possible reasons for discrepancies.

7.1 The mean radiative efficiency

We begin by comparing to estimates of the spin from the mean radiative efficiency. Comparing the total energy radiated by AGN over cosmic time with the mass density of SMBHs in the local Universe can be used to estimate the mean radiative efficiency $\langle \eta \rangle$. The mean radiative efficiency can be converted into a black hole spin using the NT73 model, but as is shown in Figure 1 the radiative efficiency from simulations can differ from the NT73 by factors of $\sim 2$, resulting in large uncertainties.

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used the intensity of the X-ray background and assumed the bulk of the AGN causing it to be at \( z = 2 \). The authors inferred \( \langle \epsilon \rangle \geq 0.15 \), suggesting the mean spin of SMBHs is \( \hat{a} \approx 0.9 \). The bulk of the sources producing the X-ray background, however, are at lower redshifts than their assumed value of \( z = 2 \). A more appropriate characteristic redshift would have been \( z = 0.7 - 1.0 \) (see e.g. Barger et al. 2003; Ueda et al. 2003), which would bring their mean efficiency down to values of \( \langle \epsilon \rangle \gtrsim 0.08 - 0.1 \).

Another high value of the radiative efficiency was inferred by Wang et al. (2006) using a different method. These authors compared the luminosity function of quasars to the mass function of quasars in redshift bins, and estimate \( \langle \epsilon \rangle \) to be in the range 0.20-0.35, suggesting the SMBHs are spinning rapidly.

In order to derive a radiative efficiency, Wang et al. (2006) equate the integral of the luminosity function \( \int L_{\text{bol}} \phi(L_{\text{bol}}) dL_{\text{bol}} \) to the integral of the mass-density function of quasars \( \int m_\star \phi(m_\star) dm_\star \). However, these authors derive the mass functions from the broad-line widths of the quasars in a magnitude-limited sample. Only quasars brighter than the limiting magnitude (\( B \)-band magnitude of 19.4) can have their masses measured and included. Since quasars have a range of Eddington ratios (e.g. McLure & Dunlop 2004), the correspondence between bolometric luminosity and black hole mass is not one-to-one. While the luminosity integral used by Wang et al. (2006) is complete above their flux limit, the mass integral is not. This is because not all quasars with mass above their nominal mass lower limit are optically bright enough to be detected in their survey so that their mass function is incomplete. The fact that the luminosity integral is complete but the mass integral is incomplete means that they will overestimate the amount of energy that was radiated away. We therefore consider their estimate of the radiative efficiency, and hence spin, as an upper limit.

Most of the recent estimates of the mean efficiency from the Soltan argument typically find values of \( \langle \epsilon \rangle \) in the range 0.06-0.1, with a typical value of \( \langle \epsilon \rangle \approx 0.07 \) (e.g. Marconi et al. 2004; Cao & Li 2008; Shankar et al. 2009; Martínez-Sansigre & Taylor 2009, see their Section 5 for a discussion of recent results).

We can compare all the previously-mentioned estimates to our results by computing the luminosity-weighted mean spin:

\[
\langle \hat{a} \rangle_L \equiv \frac{\int \langle \hat{a} \rangle_L \phi(L_{\text{bol}}) dL_{\text{bol}}}{\int \phi(L_{\text{bol}}) dL_{\text{bol}}}
\]

\[
= \frac{\int \langle \hat{a} \rangle_L P(\langle \hat{a} \rangle_L | \text{data}) d\langle \hat{a} \rangle_L \left[ \int C_X L_X \phi(L_X, z) dL_X \right] dL_{\text{bol}}}{\int C_X L_X \phi(L_X, z) dL_X dL_{\text{bol}}}
\]

(30)

For the weighting function in Equation (30) we use the X-ray LF in the range \( 0 \leq z \leq 3 \), and due to the strong evolution of the X-ray LF, practically all of the weight lies with the high redshift values of \( \langle \hat{a} \rangle_L \), since the bulk of the luminosity was emitted at \( z \gtrsim 1 \).

\( P(\langle \hat{a} \rangle_L | \text{data}) \) is given by the left panel of Figure 11, which then yields a value of \( \langle \hat{a} \rangle_L = 0.40 \). The resultant mean radiative efficiency \( \langle \epsilon \rangle_L \) is therefore \( \epsilon(0.40) = 0.075 \). However, when using the spin history from the right panel in Figure 11 (the best fitting set), we infer \( \langle \hat{a} \rangle_L = 0.28 \), or \( \epsilon = 0.068 \). The mean radiative efficiency derived from our spin history is therefore in excellent agreement with the estimates from the literature.

7.2 Lack of correlation between estimated spins and jet powers in galactic black holes

Comparing the spin measurements of GBHs (galactic black holes) with their radio luminosities, Fender et al. (2010) conclude that there is evidence for an additional parameter which controls the amount of power in jets, yet this parameter does not correlate with the spins estimated from fitting the accretion disc or the reflection edge.

In many aspects, AGN behave as scaled up versions of GBHs (e.g. Marscher et al. 2002; Merloni et al. 2003; Falcke et al. 2004; McHardy et al. 2004). The lack of correlation between ‘radio loudness’ and spin in GBHs is therefore a concern for our work.

It is encouraging that when plotting a measure of bolometric luminosity versus a measure of jet power, both GBHs and SMBHs show correlations spanning several decades, but also a scatter of 2 or 3 decades in radio luminosity (e.g. Sikora et al. 2007; Fender et al. 2010). In this paper, the scatter has been interpreted as arising mainly due to variations in black hole spin (see also Sikora et al. 2007), however Fender et al. (2010) find no correlation with published spin estimates for the GBHs. Fender et al. (2010) conclude that the lack of correlation could be due to spin having no effect on the observed jet power, or alternatively due to either the spin measurements or the measurements of jet power being inaccurate.

It is possible that at low spins, the power from the disc jet is larger than the power from the black hole jet (e.g. the HK06, N07 and BB09 jet efficiencies in Figure 2), complicating the interpretation. However, if spin has an observable effect on the jet power, then one would expect some correlation between spin and jet power. If the disc jet were always more important than the jet driven by the spin of the black hole, then the spin would be irrelevant when explaining observations of jets.

Subsection 7.2.2 discusses the uncertainties in estimating the jet power from core radio luminosities, Subsection 7.2.2 discusses the uncertainties in the estimates of black hole spin from fitting the accretion disc luminosity or the iron reflection lines, and Section 7.2.3 discusses the observed lack of correlation.

7.2.1 Estimated jet powers

Fender et al. (2010) measure the jet powers from the core luminosities, as is usual in the GBH community. However, for AGN the core luminosity is totally incapable of predicting the total radio luminosity (see Figure 7 of Klöckner et al. 2009), and it is the total radio luminosity that is required to trace the jet power (e.g. Rawlings & Saunders 1991; Wilott et al. 1993; Birzan et al. 2004; Cavagnolo et al. 2010).

We note the cases of Cygnus X-1 and S26 (a micro-quasar with extended radio structure reminiscent of an FRII radio galaxy) where the extended lobe radio luminosity is \( \sim 2 \) decades brighter than expected from the cores (Gallo et al.)
Reynolds & Fabian (2008) and Penna et al. (2010) also support the view that for thin discs $(h/r \lesssim 0.1)$ the deviations from NT are small.

The simulations of Beckwith et al. (2008b) and Noble et al. (2009) suggest that deviations from the NT73 model are particularly important at low-spins. Beckwith et al. (2008b) also discuss the possible dependence of this on $h/r$, and note that height in their simulations is $-0.06-0.2$.

For moderately thick discs $(h/r\sim 0.2)$, the simulations by Fragile (2004) found that when the tilt angle was zero, the dependence of the characteristic radius with spin resembled closely that of the NT73 model. However, with tilt angles of only 15 degrees, the characteristic radius is constant with spin, and any attempt to infer the spin from the characteristic radius will severely underestimate the spin (Fragile 2004).

Another potential problem can occur if the accretion disc truncates at a larger radius than the ISCO, for example if the accretion rate is too low to sustain an optically-thin disc in the innermost region, and the accretion flow becomes an ADAF instead. In this case, the radius of the ISCO will be overestimated, meaning the inferred value of the spin will be a lower limit. Indeed, in Cygnus X-1, the fits to the thermal continuum and the K-α line suggest the truncation radius is at a distance $\sim 2-3 \times$ larger than the ISCO (Gierliński et al. 1995; Makishima et al. 2008).

For one of the sources with a measured high spin ($\hat{a}=0.94$ Miller et al. 2009), a subsequent analysis by Done & Diaz Trigo (2010) has found that the extremely broad line is artefact due to the brightness of the source causing ‘Pile-up’ of photons. The authors find that after taking this effect into account the line is narrower than previously determined, corresponding to a characteristic radius that does not require high spin and might even imply a truncated disc.

Indeed, we note that spin measurements of the same GBH from fitting the disc continuum and from the fitting the reflection components do not always agree within the quoted uncertainties (see Table 1 of Fender et al. 2010). Some GBHs have had their spin estimated both from disc-fitting and from iron lines, yet the two estimates do not always agree within their formal uncertainties.

From disc-fitting alone, the reported measurements for GRS1915+105 from disc-fitting range from 0 to 0.998 (see references in Fender et al. 2010). More recently, Blum et al. (2009) have estimated the spin again from disc-fitting and from the K-α reflection line, and obtain spin values of $\hat{a}=0.56$ and 0.98 respectively. Blum et al. (2009) use observations of GRS1915+105 during a low-hard state only, with $\lambda<0.3$, and argue that some of the discrepancy with other groups could be partly due to observing at different states (e.g. Middleton et al. 2006), observed the source when $\lambda>0.3$.

Finally, an additional complication arises from the pres-
ence of absorbing material along the line of sight and near the black hole. Photoelectric absorption from gas with a range of ionisation parameters can lead to a spectral shape similar to a red wing, and some authors suggest that the broad reflection lines can be fitted without requiring relativistic blurring (e.g. Done & Gierliński 2006; Miller et al. 2008; Turner & Miller 2009; Miyakawa et al. 2009; Yaqoob et al. 2010). This is an area of intense debate, where other authors suggest that relativistic blurring is indeed required to explain the lines (e.g. Reynolds et al. 2009; Fabian et al. 2009; Zoghbi et al. 2010).

7.2.3 Lack of correlation between spins and jet powers

To summarise, while measurements from the reflection lines of disc fitting offer an exciting and promising method to determine black hole spin, the accuracy of these measurements is still being debated. Our primary concern is that the characteristic radius inferred by these measurements might not always correspond to the ISCO. These concerns apply to fitting both the continuum-fitting and the reflection line methods.

This is not a criticism on our part, since the spin estimated from \( \eta \) in our work is also hugely uncertain and Figure 2 shows the different jet efficiencies we have used: it is clear that they vary enormously. Converting between jet powers and radio luminosities is also highly uncertain in GBHs as well as in AGN (see Sections 3.1 and 7.2.1). An additional consideration to bear in mind is that measures of AGN jet power from the total radio luminosities are actually derived from the total energy deposited over typically \( \sim 10^7 \) years, so that they are only time-averaged values.

Given the uncertainties we do not think that the observed lack of correlation between spins and radio luminosities found by Fender et al. (2010) is at odds with our assumption that spin is a monotonically-increasing function of spin. The uncertainties in the spin estimates and the estimates of the jet power are still too large. We do not think that the current evidence is strong enough to conclusively rule out the spin paradigm.

We stress that there is strong evidence amongst GBHs for the jet power to correlate with the state of the accretion flow (e.g. Fender et al. 2004; Done et al. 2007). We are not arguing here that such effects are not important in AGN.

Amongst AGN, however, huge differences in (time-averaged) jet power are also observed with no noticeable difference in the accretion flow (reflected, for example, by the shape of the SED or the Eddington ration, e.g. Elvis et al. 1994; Sikora et al. 2007). It is this difference that requires an additional hidden variable such as spin.

Finally, we note also that winds with similar escape velocities have been detected in radio-loud and radio-quiet AGN (Tombesi et al. 2010a, 2010b). Their results are consistent with both populations having similar underlying distribution, but the radio-loud sample is much smaller (5 objects) than the radio-quiet sample (42), and unsurprisingly the latter shows a larger spread in velocities, with maximum values \( \sim 0.3c \). These winds are likely to be powered by accretion close to the Eddington limit (King & Pounds 2003, rather than jets.

8 DISCUSSION

We have used an assumption where the power available for the production of jets is a fraction of the accreted energy, \( \eta \). We have used the values for \( \eta \) given by recent theoretical and simulation work, summarised in Figure 2. This approximation can explain the radio loudness of quasars as a dependence on the spin of the accreting SMBH as well as explaining several observed properties of radio-selected AGNs.

In Section 3 we use three parametrisations for the spin distribution of high- and low-accretion rate SMBHs, and use the radio LFs of HEGs and LEGs together with a bayesian model-selection method to select the most appropriate parametrisation. A two-gaussian model is chosen, ahead of power-law distributions or single-gaussian models. This two-gaussian distribution of spins can explain reasonably well the radio LF of HEGs and LEGs individually.

It is interesting that both the high-accretion rate regime (in the form of the upper envelope for the quasars in Section 3), as well as the low-accretion rate regime (the ADAF-LEGs in Section 3) require a mechanism to produce very high jet efficiencies, \( \eta_{\text{max}} \sim 1 \). This seems to be independent of the accretion mode, and black hole spin provides one possible mechanism for such high jet efficiencies, as shown by some of the models in Figure 2.

For the two-gaussian distribution, the best-fit parameters for the LEGs-ADAFs choses two gaussians of similar amplitude, one with minimum spin and the other with maximum spin. This suggests that there are similar numbers of high-spin and low-spin SMBHs amongst the SMBHs with low-accretion rates. The best-fit distribution for the HEGs-QSOs is also found to have a bimodal distribution, but this time with a very low amplitude for the high spin peak. Hence, most of the SMBHs with high-accretion rates have low spins.

Since we infer a bimodal distribution for spins, which is heavily favoured over smooth power-law distributions, our model predicts a dichotomy in the radio-loudness of quasars. However, detecting such a dichotomy might prove difficult due to source-to-source variations in the conversion from jet power to radio luminosity density and from bolometric to monochromatic luminosity, as well as due to observational selection effects.

We are able to make falsifiable predictions about the contribution of HEGs and LEGs to the radio LF. At \( z=0 \), we predict that the radio LF of LEGs is dominated by black holes with \( m_\bullet \geq 10^8 \ M_\odot \) down to radio luminosity densities of \( \sim 10^{23} \ W \ Hz^{-1} \ sr^{-1} \) at 1.4 GHz. At \( z=1 \) and above a certain luminosity density, which we estimate to correspond to \( \sim 10^{26} \ W \ Hz^{-1} \ sr^{-1} \), we expect all the radio sources to be composed entirely of HEGs. Below this value, we expect a rapidly increasing number of LEGs. The appearance of a large population of HEGs amongst the radio sources is due to the the strong increase of the comoving accretion rate onto SMBHs.

As discussed in Section 6, the evolution in cosmic spin is most notable in the fraction of SMBHs with high spins. This fraction is low at high redshifts, and increases towards lower redshifts. The evolution in spin is really driven by the gradual disappearance of a high-accretion rate but low-
spin population, so that the low-accretion rate and high-spin population becomes gradually dominant.

Combining the results from the different jet efficiencies, with the best-fitting parameters, and the evolution of the X-ray LF, we are able to estimate the expectation value for the spin as a function of redshift for black holes with $m_* \gtrsim 10^6 \, M_\odot$: We find marginal evidence for evolution in the spin distributions. If we use all the efficiencies, we find the fraction of SMBHs with $\hat{a} \geq 0.5$ increases from $0.34 \pm 0.29$ at $z=1$ to $0.45 \pm 0.33$ at $z=0$. If only the best fitting set is used, this fraction is found to be $0.16 \pm 0.03$ at $z=1$ and $0.24 \pm 0.09$ at $z=0$.

The mean cosmic spin increases from $\hat{a} \sim 0.35$ at $z \sim 1$ to $\hat{a} \sim 0.75$ at $z \sim 0$. However, when using the three best fitting jet efficiencies only, the evolution is found to be more modest: from $\hat{a} \sim 0.25$ to $\hat{a} \sim 0.35$ in the same redshift interval. This second set of values represents our best estimate.

The luminosity-weighted spin comes out to be $\hat{a}_L=0.40$ for all efficiencies and $\hat{a}_L=0.28$ for the best fitting set. This predicts the mean radiative efficiency to be $\langle \epsilon \rangle = 0.075$ (or $\langle \epsilon \rangle = 0.068$ when using the best fitting set). These quantities can be compared to independent constraints from the Soltan argument, and are in excellent agreement with them.

Overall, we infer a very modest evolution of the mean spin, although given the bimodal distributions a mean value is not the best description of the evolution of the spin. Indeed, the spin distributions evolve from distributions dominated by a single low spin component at high redshift, towards bimodal distributions at low redshift. In addition, as stressed in Section 6 we are probably overestimating the high-spin contribution at $z \gtrsim 1$.

Perhaps counter-intuitively, the epoch of lowest black hole spin corresponds to the epoch of highest accretion. The evolution of $\langle \hat{a}(z) \rangle$ inferred here, however, is consistent with the picture of ‘chaotic accretion’: matter from the host galaxy falls into the quasar from random directions and with different orientations of the angular momentum vector (see King et al. 2008).

Depending on the angle between the angular momentum vectors of the black hole and the accretion disc, these two will either align or counter-align. During approximately half of the time the accreted matter has the opposite direction of angular momentum to the black hole (King et al. 2005, Lodato & Pringle 2006). Co-rotating orbits are physically closer to the event horizon of the hole than counter-rotating ones. Therefore co-rotating matter increases the angular momentum by a smaller amount than the decrease brought by counter-rotating matter. Chaotic accretion is expected to lead to SMBHs with low spins ($\hat{a} \sim 0.1$ King et al. 2008), and our result is in agreement with spun down AGNs at high redshift, when the mean accretion rate was higher.

For accretion to significantly affect the spin of a black hole, the increase in mass must be significant (Bardeen 1970). We approximate this as the condition

$$\frac{\Delta m}{m_*} \sim 1,$$

which, if not met, implies no significant decrease in $\hat{a}$ due to chaotic accretion.

The higher mean spin at lower redshifts suggests major mergers of SMBHs are driving the increase in spin. Galaxy major mergers are expected to lead to major mergers of the central SMBHs. During the coalescence of two black holes of similar mass, the orbital angular momentum will contribute significantly to the final angular momentum of the coalesced black hole. Hence, major galaxy mergers are expected to lead to central SMBHs with a moderately high spin value (e.g. Hughes & Blandford 2003, Rezzolla et al. 2008). Minor black hole mergers, on the other hand, tend to lead to low values of spin in the coalesced hole (see Hughes & Blandford 2003). Values of $\langle \hat{a} \rangle \sim 0.7$ can be rea-

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**Figure 12.** Distribution of final black hole spins from a Montecarlo simulation of $10^5$ SMBHs undergoing one major merger each. We use the analytic formula of Rezzolla et al. (2008), which requires the initial masses and spins of both black holes, as well as three angles describing the relative orientations with each other of the angular momentum vectors of each black hole and the total angular momentum vector (for a total of 7 free parameters). The three angles have flat probability distribution functions between 0 and $2\pi$. The two initial spins are allowed any values between 0 and 0.1, while the three angles any value between 0 and $2\pi$. The smaller mass is always fixed at a value of 1. In the left-hand panel, the larger mass is drawn from a flat distribution within the range 1-4. We are therefore representing what is normally considered as a major merger. In the right-hand panel, the larger mass is fixed at 1, representing equal mass mergers. The vertical dashed line represents the mean. The panels illustrate that high mean spin values, $\langle \hat{a} \rangle \sim 0.6-0.7$ can be reached by single-event major mergers. Allowing the initial spins to have values $0 \leq \hat{a} \leq 1$ instead, with a flat distribution in this range, leads to much broader distributions of the final spins, but with essentially the same mean values.
isotropically single-event major mergers, the distribution is centred around $\langle \hat{a} \rangle = 0.58$ and has a full width zero intensity of about 0.3. The right-hand panel represents equal-mass mergers only (1:1 mass ratio), it is centred around $\langle \hat{a} \rangle = 0.69$ and is very narrow, with a full width zero intensity of about 0.05. The narrow distribution is partly due to the narrow initial spins, in the range 0-0.1. A broader distribution of initial spins would also lead to a broader distribution of final spins yet the mean would remain unchanged.

We have carried out a second simple simulation, shown in Figure 13. Here, $10^5$ black holes have each suffered a random number of mergers. All initial SMBH spins are drawn from a flat distribution between 0 and 0.1, reflecting the low spin values expected from chaotic accretion. After the merger, they are assumed to accrete a small enough fraction of their own mass that the spin is not significantly changed (the condition in Equation 40 is not met). The exact number of mergers each black hole will undergo is determined by drawing from a Poisson distribution with mean 0.7, reflecting the mean number of mergers the host galaxy has experienced since $z \approx 1$ (Robaina et al. 2010). The stellar masses of the bulges of the host galaxies are drawn from a Schechter function, and the masses of the merging black hole are assumed to be a fixed fraction of this mass ($1.4 \times 10^{-3}$ of the stellar mass, Haring & Rix 2004). The final spin is estimated using the formula given by Rezzolla et al. (2008), where we have randomised the orbital parameters (the orientations of each angular momentum component with respect to each other) as well as the initial black hole spins.

In this simulation, 50% of the SMBHs do not undergo any mergers, and they retain the small initial spin (the flat component around $\hat{a} = 0.0-0.1$). A significant fraction undergo 1 or 2 mergers (35% and 12% respectively, peaking at 0.65 and 0.8), and a small fraction undergo three or more mergers (3%, causing the high-spin tail). The distribution shows a sharp peak around $\hat{a} = 0.65$, but the expectation spin is only $\langle \hat{a} \rangle = 0.35$ (vertical dashed line in Figure 13), in very good agreement with our results from the best fitting set. This low mean value is due to the large fraction of black holes that have not undergone any mergers and have kept their original spins (0-0.1). The mean from this simple simulation is slightly lower than our estimate from fitting the radio LF of HEGs and LEGs, but the distribution is qualitatively similar.

As discussed by Robaina et al. (2010), the mass limit of their survey requires both progenitor galaxies to have masses $\gtrsim 5 \times 10^{10} M_\odot$. Hence major mergers involving one progenitor with a mass $< 5 \times 10^{10} M_\odot$ are missed out, and their estimate is a lower limit on the mean number of major mergers experienced by galaxies with mass $\gtrsim 10^{11} M_\odot$. Indeed, studying the projected axial distribution of galaxies more massive than $10^{11} M_\odot$, van der Wel et al. (2009) have argued that they must have all undergone a major merger. In addition, these mergers are expected to have been relatively gas-poor, otherwise the projected axial distributions would be more similar to discs (Naab et al. 2004; van der Wel et al. 2009). Hence the mean of 0.7 mergers per galaxy, on average, might be an underestimate.

However, Figure 13 does predict an approximately bi-modal distribution, qualitatively similar to what we infer at $z=0$ (see Section 5 and in particular Figure 6), with reasonably similar expectation values. Our results suggest the

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**Figure 13.** Simulation of final black hole spins after $10^5$ SMBHs undergoing a variable number of mergers. The number of mergers undergone is drawn from a Poisson function with mean 0.7 (following the results of Robaina et al. 2010). The final spin is calculated using the analytic formula of Rezzolla et al. (2008) (see caption to Figure 12). We have assumed flat distributions for all the two black hole masses, the two black hole spins and the three angles. In this simulation, the black hole masses are assumed to be a constant fraction $1.4 \times 10^{-3}$ of the galaxy stellar mass (Haring & Rix 2004). These stellar masses are allowed to have masses in the range $5 \times 10^{10} - 4 \times 10^{11} M_\odot$, and are drawn at random from a Schechter function with a break at mass $1.4 \times 10^{11} M_\odot$, and low-mass end power law index of -1.2 (Cole et al. 2001). The initial spins of the SMBHs are drawn from a flat probability distribution between $\hat{a}=0-0.1$, and the spin of the coalesced SMBH is tracked (later incoming SMBHs are also assumed to have an initial spin in the range 0-0.1). The mergers are assumed to occur isotropically, and the final black hole spins are again inferred using the analytic formula of Rezzolla et al. (2008). The distribution shows 3 obvious signals: the sources having undergone zero mergers are gathered around $\langle \hat{a} \rangle = 0.0-0.1$, those having merged once peak around 0.65, and those having merged twice extend up to 0.85. The resulting expectation value of $\langle \hat{a} \rangle = 0.35$ is marked by the vertical dashed line.
high-spin end to peak around $\hat{a} \sim 0.80-0.99$, rather than 0.7, but otherwise the distribution Figure 13 is similar to the distributions inferred for the LEGs. We do note that achieving the high spins we infer in our bimodal distributions, $\hat{a} \sim 1$, remains very difficult.

The galaxy mergers driving the spin-up do not need to be completely ‘dry’ (e.g. van Dokkum 2005); provided that after the merger, the condition in Equation 40 is not met, the spin of the SMBHs will be predominantly determined by the coalescence of the two SMBHs as no significant spin-down will occur. Given a black hole mass of $10^8 M_\odot$, needs to accrete a mass $\sim 10^8 M_\odot$ to spin down, and assuming a fraction $1.4 \times 10^{-3}$ of the galaxy’s gas makes it to the black hole (e.g. Häring & Rix 2004), spinning down the most massive black holes requires $\sim 10^{11} M_\odot$ of molecular gas. This is a very high gas mass, much higher than found in low-redshift elliptical galaxies (Lees et al. 1991; Young 2002).

Another key issue is that our estimate of $\langle \hat{a}(z) \rangle$ is dominated by black holes with masses $\gtrsim 10^9 M_\odot$, which reside in bulges with stellar masses $\gtrsim 10^{11} M_\odot$, and these have generally elliptical morphologies. Thus, we have indirectly selected galaxies with elliptical morphologies, which is a proxy for selecting galaxies that have undergone at least one major merger. It is the fact that elliptical galaxies have undergone major mergers that allows their central SMBHs to have high spin values. This point was noted by Scheuer (1992) and related arguments have also been put forward by Wilson & Colbert (1993), Sikora et al. (2007) and Volonteri et al. (2007).

Figure 14 is only a simple simulation, and detailed studies of the cosmic evolution of SMBH spins from mergers can be found, for example, in Volonteri et al. (2007), Berti & Volonteri (2005), Lagos et al. (2009). The simulations carried out by Fanidakis et al. (2011) incorporate a semi-analytic model of the accretion onto SMBHs in the centres of galaxies, and in this simulation mergers of galaxies also cause mergers of the central SMBHs. The simulation tracks down the spin of the central SMBHs, and assumes chaotic accretion spins the black holes down. Figure 14 shows the resulting spin history for black holes with $m_\bullet \gtrsim 10^8 M_\odot$ (N. Fanidakis, 2010, priv. comm.).

The behaviour seen in Figure 14 is almost identical to our Figure 11. This similarity extends also to the standard deviations, reflecting the broad distribution of SMBH spins at each redshift. The value of $\langle \hat{a}(z) \rangle$ from the simulation is also in good quantitative agreement with our values at $z \gtrsim 1$.

This line of argument suggests that their lower-luminosity AGN in spiral galaxies will have SMBHs with low spin values (King & Pringle 2007). At first sight, this would appear in contradiction with the spin estimate for the nearby AGN MCG-6-30-15, $\hat{a}=0.98$, from a broad iron line (Brenneman & Reynolds 2006). However, the host galaxy of this source is actually an S0 (Perrett et al. 2000), so the high spin could have been acquired through merging. In addition, the caveats discussed in Section 7.2 should be kept in mind.

Major mergers are also expected to happen at high-redshift ($z \gtrsim 1$), but higher gas masses in the host galaxies imply higher accretion rates which will lead to a spin down (Equation 40 will be satisfied). Hence, while the mechanism to spin SMBHs up (major merging) is occurring both at high and low redshifts, the increase in spin at low redshifts can be attributed to a gradual disappearance of the ‘braking’ mechanism (chaotic accretion of a significant mass).

If high-redshift quasars have a low mean spin due to chaotic accretion, it implies they have had time to spin down. The timescale for spin down is related to the timescale for alignment ($\sim 10^7$ yr for $\hat{a} \sim 1$, Equation 15 of Lodato & Pringle 2006) since after a few alignments and anti-alignments the spin will have decreased to $\sim 0.1$. AGNs with a higher spin value are expected to have a longer alignment timescale (Lodato & Pringle 2006), so jets from high-spin SMBHs will be more stable than those of SMBHs with low spin, implying powerful observed FRIIs could live for a few $10^7$ yr (indeed the ages estimated by Scheuer 1993, Willett et al. 1999, Blundell & Rawlings 2000) and will be rapidly spinning. Given that the most powerful radio-loud quasars typical jet advance speeds are $\sim 0.05 c$ (Scheuer 1993), and assuming a maximum age of $5 \times 10^7$ yr, the largest jets are expected to be $\sim 8$ Mpc at the most, in excellent agreement with observations (e.g. Blundell et al. 1994).

Our bimodal distribution of spins suggests that in the local Universe, the SMBHs with mass $\gtrsim 10^8 M_\odot$ will be able to produce jets with only a modest rate of accretion ($\lambda \lesssim 1$). It is therefore no surprise that approximately 30% of local massive ellipticals have jets with moderate radio luminosities (e.g. Mauch & Sadler 2007).

Our estimate of $\langle \hat{a}(z) \rangle$ is not in disagreement with the high values of $\hat{a} \sim 0.9$ inferred for the SMBHs of low-redshift elliptical galaxies (see N07). The authors inferred the spin from the correlation between Bondi accretion rate and jet power for nearby elliptical galaxies found by Allen et al. (2006), and using an ADAF model for the production of
jets around rotating SMBHs. The sources in the sample of Allen et al. (2006) were selected to show jet-induced cavities in the hot gas imaged using X-rays. Hence, the sample is biased towards elliptical galaxies with jets, which in our picture and that of N07 corresponds to high spin. Although our mean spin in the local Universe is typically lower than 0.9, approximately half of the SMBHs accreting as ADAFs are predicted to have near-maximal spins (Section 4), hence there is no conflict between our results and those of N07.

Finally, we speculate how our inferred cosmic spin history can be explained in the context of galaxy groups and clusters. We have argued that SMBH major mergers caused by galaxy major mergers will spin up the black holes. For major mergers to occur efficiently, there must be a high density of massive galaxies, yet the translational velocities of the galaxies must not exceed the escape velocities of the galaxies themselves, which correspond to \(v_{\text{esc}} \approx 200-400 \text{ km s}^{-1}\) for massive galaxies hosting black holes of mass \(M_\bullet > 10^8 \text{ M}_\odot\) (Ferrarese & Merritt 2000).

The ideal environment for mergers therefore corresponds to groups or to the outskirts of low-redshift clusters of galaxies. At \(z \approx 2\), the clusters of galaxies have not yet virialised fully, and the characteristic velocities of galaxies in these high-redshift protoclusters will not exceed this velocity significantly. Hence, mergers are expected to be efficient, and the mean spin of SMBHs will be initially high due to mergers. However, at \(z \approx 2\) large reservoirs of gas will also be present, allowing the SMBHs to accrete large masses.

The most massive SMBHs will reside at the centres of these protoclusters: with black hole masses \(M_\bullet > 10^9 \text{ M}_\odot\), \(v_{\text{esc}} \approx 0.1\) and initially \(\dot{a} \approx 0.6\) due to mergers, these central SMBHs will produce powerful FRII jets. The injection of energy from these FRII jets into the intracluster medium will prevent further cooling of the gas cutting down the supply of gas for future star-formation and SMBH growth in galaxies in the protocluster (e.g. Binney & Tremaine 1987, Rawlings & Jarvis 2004).

The SMBHs in the central dominant galaxies might well retain their high spin from the high-redshift epoch, \(z \approx 2\), provided that the total mass accreted after their last major merger is small compared to the black hole mass, \(m_\bullet \approx 10^9 \text{ M}_\odot\). Indeed the little evolution observed amongst the high mass end of the stellar mass function, with stellar mass \(>3 \times 10^{11} \text{ M}_\odot\), suggests little merging activity below \(z \approx 1\) for the most massive galaxies (Banerji et al. 2010).

The bulk of the accretion is, however, in the form of radio-quiet quasars \(m_\bullet \approx 10^8 \text{ M}_\odot\), \(\dot{a} \approx 0\), whose spin at high redshift is low due to prolonged chaotic accretion. Presumably these objects have not yet undergone a major merger or have been able to accrete their own mass, \(\Delta m_\bullet / m_\bullet > 1\), to spin themselves down to \(\dot{a} \approx 0\). The number of such objects is large compared to the number of \(10^9 \text{ M}_\odot\) SMBHs in future central dominant galaxies, which brings the mean spin down.

At \(z < 1\) mergers of massive galaxies will still occur, particularly in environments with velocities \(\sim 300 \text{ km s}^{-1}\), corresponding to group environments and the outskirts of clusters. These mergers will spin up the SMBHs. The gas in the host galaxies will have been stripped by ram pressure, while the intracluster gas is hot and will not resupply the galaxies. With little gas in the host galaxy, the braking mechanism, chaotic accretion of a significant mass, disappears.

Future episodic accretion onto SMBHs with \(m_\bullet = 10^8 - 10^9 \text{ M}_\odot\) will be modest and will not affect the spin. It will lead to intermittent FRI-ADAF activity, rather than to radio-quiet quasars. Occasionally a major accretion episode might occur, creating sources such as Cygnus A, but such episodes will be very rare.

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