Collapse of Showa Bridge during 1964 Niigata Earthquake: A reappraisal on the failure mechanisms

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Collapse of Showa Bridge during the 1964 Niigata earthquake has been, throughout the years, an iconic case study for demonstrating the devastating effects of liquefaction. Inertial forces during the initial shock (within the first 7 seconds of the earthquake) or lateral spreading of the surrounding ground (which started at 83 seconds after the start of the earthquake) cannot explain the failure of Showa Bridge as the bridge failed at about 70 seconds following the main shock and before the lateral spreading of the ground started. In this study, quantitative analysis is carried out for the various failure mechanisms that may have contributed to the failure. The study shows that at about 70 seconds after the onset of the earthquake, the increased natural period of the bridge (due to the elongation of unsupported length of the pile owing to soil liquefaction) tuned with the period of the liquefied ground causing resonance between the bridge and the ground motion. This tuning effect (resonance) caused excessive deflection at the pile head adequate to unseat the bridge deck from the supporting pier and thereby initiating the collapse of the bridge.
1.0 INTRODUCTION

1.1 Importance of the study

The collapse of Showa Bridge (see Figure 1 for location with respect to North-South direction, Figure 2 for a photograph of the collapse and Figure 3 for a schematic diagram) during the 1964 Niigata earthquake features in many publications as an iconic example of the detrimental effects of liquefaction induced lateral spreading of the ground, see for example Hamada and O’Rourke (1992), Kramer (1996), Bhattacharya (2003), Bhattacharya et al. (2005), Yoshida et al. (2007), Bhattacharya et al. (2008) and Bhattacharya and Tokimatsu (2013). It was generally believed that lateral spreading was the cause of failure of the bridge (Hamada and O’Rourke, 1992). This hypothesis is based on the reliable eye witness that the bridge failed 1 to 2 minutes after the earthquake started which clearly ruled out the possibility that inertia, in the initial strong shaking, was the contributor to the collapse.

However, Bhattacharya (2003), Bhattacharya et al. (2005), Bhattacharya and Madabhushi (2008) reanalysed the bridge and showed that lateral spreading hypothesis cannot explain the failure of the bridge. They argued: (a) had the cause of failure been due to lateral spreading, as suggested, the piers (see Pier P5 and Pier P6 in Figure 3) should have displaced identically in the direction of the slope. (b) the piers close to the riverbanks did not fail, where the lateral spreading was seen to be severe. This conjecture was later confirmed by the study carried out by Yoshida et al. (2007) who suggested that lateral spreading of the surrounding ground started after the bridge had collapsed. Towhata et al. (1992) indicated that the permanent ground displacements of liquefied strata are strongly affected by topographical and geological conditions, and are not explicit functions of earthquake time series. Kerciku et al. (2008) showed that liquefied soil under the middle of the bridge (under pier P5 and P6) was already at its lowest positions of potential energy and would not be expected to flow. All the above circumstantial evidences and arguments suggest that lateral spreading may not be the cause for the collapse of Showa bridge.
Essentially, no consensus is yet reached regarding the cause of collapse of this bridge and it remains one of the interesting case studies to analyze for earthquake geotechnical engineers. This paper aims to provide a failure hypothesis based on quantitative calculations which corroborates with the observations and evidences available in the literature and in public domain. This example of bridge failure can also be particularly important from the point of view of calibration of pile design methods and failure theories due to the following reasons:

1. This bridge collapsed just 15 days after the construction, and had steel tubular piles. This ensures less uncertainty of material strength, as degradation of piles due to corrosion is not expected.


3. In addition, the role of in-depth study of case histories in earthquake geotechnical engineering cannot be underestimated.
1.2 Details of the earthquake and the bridge
The Niigata earthquake occurred on the 14th of June 1964 and registered a moment magnitude of 7.6. Located some 55 km from the epicentre, crossing the Shinano River, Showa Bridge (simple steel girder bridge with pile foundations) was one of the bridges which collapsed as a result of the earthquake. The total length of the bridge was about 307m. The bridge had 12 composite girders and its breadth was about 24m. Main span length was about 28m and side span length was about 15m (Fukuoka 1966). Figure 1 shows the location of the bridge. It may be observed that the longitudinal axis of the bridge is at an angle of 30° North-West. The view of the collapsed Showa Bridge from the southwest side is shown in Figure 2.

1.3 Post earthquake observations
During the 1964 Niigata earthquake, the bridge site was subjected to extensive liquefaction and lateral spreading. Reliable eyewitness quoted by Horii (1968) and Hamada and O’Rourke (1992) along with the progressive damage simulation by Kazama et al. (2008) suggest that the bridge collapsed 1-2 minutes after the peak ground acceleration (PGA) had ceased. Yoshida et al. (2007) collated many eye witness statements and established the chronology of the bridge failure. Figure 3 shows a schematic diagram of the collapse of the bridge. Horizontal and vertical deflections of the pile cap are also indicated in the figure as \( \delta \) and \( l \) respectively. The sequential failure initiated when piers \( P_5 \) and \( P_6 \) collapsed in opposite directions, accompanied by the fall of girder \( G_{5,6} \) (between \( P_5 \) & \( P_6 \)) in the river. Immediately afterwards, in a domino effect, girders \( G_{6,7}, G_{4,5}, G_{3,4} \) and \( G_{2,3} \) partially fell in the river. Based on the eye witness reports, Kazama et al. (2008) also reported that the collapse of the bridge girders proceeded as \( G_{5,6} \rightarrow G_{6,7} \rightarrow G_{4,5} \rightarrow G_{3,4} \rightarrow G_{2,3} \). As a result, five of the twelve spans fell off the pile heads in the earthquake.

![Figure 3: Schematic diagram of the collapse of the bridge along with the deflections of the pile caps (Iwasaki 1986)](image-url)
Figure 4 shows the structural details and soil data for a pile of pier P4 after post earthquake recovery. On the other hand, Figure 5 shows the deck-pier support arrangement where there is alternating roller (movable) and pinned (fixed) except for pier P6 where both the supports are roller. Yoshimi (2003) commented on the lack of redundancy in the structural design of the bridge. It may be noted from Figure 5 that relative displacement of more than 30cm at the deck level will lead to unseating of the deck and hence may lead to collapse.

Figure 4: Structural and soil data for a pile of pier P4 (Fukuoka 1966)

Figure 5: Support condition of the bridge at two piers
1.4 Liquefaction profile

The Showa Bridge was situated in the coastal alluvial plain of the Niigata city which consists of marine sediments due to current along the Japan sea coast and due to the river or lake deposit along the Shinano river. The sand was uniformly graded medium sand and its 60 percent diameter ($D_{60}$) was about 0.3mm (Fukuoka 1966). Hamada and O'Rourke (1992) estimated the ground liquefaction profile. As shown in Fig. 6, the soil liquefied to a maximum depth of about 10 m below the riverbed and to a maximum depth of approximately 5 m below the riverbed near the left abutment.

![Figure 6: Soil liquefaction profile (in grey), Hamada and O'Rourke (1992)](image)

2.0 GROUND ACCELERATION AND DISPLACEMENT

2.1 Recorded ground motion

Fig. 7(a) shows the time history of the acceleration, velocity and displacement recorded at the basement of a building (Kawagishi-Cho) at a location 1.25 km from the Showa bridge and Figure 7(b) shows the wavelet energy spectrum of the motion. Figure 8 (a) shows the details of the location of Kawagishi-Cho Apartment House along with the Showa bridge. Figure 8(b) on the other hand shows typical subsurface soil profile in entire Niigata city inferred from borehole data obtained before the earthquake. The profile suggests that the soils are primarily sandy down to the depth of 20 to 30m. The figure also shows the lines of equal N values. It may be mentioned that records at Kawagishi-Cho are the only available strong motion records recovered near Niigata city and the site was fully liquefied. The next section evaluates the motion to ascertain whether or not this can be used for studying the Showa Bridge failure.
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Figure 7(a): Recorded acceleration, velocity and displacement time histories, adapted from Kudo et al. (2000). Also in the diagram the time window (65s - 75s) when it is believed the Showa Bridge collapsed is indicated. (http://kyoshin.eri.u-tokyo.ac.jp/SMAD)

Figure 7(b): Wavelet Energy Spectrum of NS component of motion shown in Fig. 7(a)
2.2 Seismological evaluation of the ground motion

The 1964 Niigata earthquake occurred at the convergent boundary between the Eurasian and the North American plates, having a reverse faulting mechanism. Because the plate interaction at the boundary was complex and recorded ground motions at distant stations are contaminated by noise, the fault plane of this event (whether the fault plane was west-dipping or east-dipping) has not yet been unanimously agreed by seismologists (e.g. Abe, 1975; Shiba and Uetake, 2011; Hurukata and Harada, 2013). Recently, Shiba and Uetake (2011) have proposed a west-dipping fault plane, whereas Hurukata and Harada (2013) have suggested an east-dipping fault plane. In this study, the two alternatives by Shiba and Uetake (2011) and Hurukata and Harada (2013) (i.e. east-dipping and west-dipping fault planes) are adopted to examine the directivity of seismic wave propagation and
to calculate the distance between a site of interest (Showa Bridge and Kawagishi-Cho) and the rupture source.

Figure 9 shows the locations of the two fault planes for the 1964 Niigata earthquake: the fault plane 1 is based on Shiba and Uetake (2011) – i.e. west-dipping, while the fault plane 2 is based on Hurukata and Harada (2013) – i.e. east-dipping. Note that the fault plane 1 is steeper than the fault plane 2 (60 degrees versus 34 degrees). In the figure, the locations of Showa Bridge (37.9128N, 139.0427E) and Kawagishi-Cho (37.9093N, 139.0294E) are also indicated. For the fault plane 1, the shortest rupture distances to Showa Bridge and Kawagishi-Cho are calculated as 14.5 and 15.6 km, respectively. For the fault plane 2, the shortest rupture distances to Showa Bridge and Kawagishi-Cho are calculated as 17.0 and 17.5 km, respectively. The distance between Showa Bridge and Kawagishi-Cho is 1.25 km. From Figure 9, it is clear that the Showa Bridge and Kawagishi-Cho sites share the similar wave propagation path, noting that the rupture process of the 1964 Niigata earthquake occurred bilaterally from the hypocentre (Shiba and Uetake, 2011). Thus the directions of rupture propagation and seismic wave propagation coincide for the southern half of the fault plane.

As mentioned earlier, very important ground motion time-history data were recorded at the Kawagishi-Cho apartment building, where severe liquefaction was observed (and consequently, multiple apartment buildings toppled down because of liquefaction-induced instability at the building foundation). A map of Showa Bridge and Kawagishi-Cho is shown in Figure 8(a) and
similar extensive liquefaction was observed at/near Showa Bridge (Yoshida et al. 2007). Near ground surface soil profiles in Niigata City (top 5 to 15 m) are typically characterised by (liquefiable) soft sandy deposits (typical N values are less than 10), which are formed by Shinano River over many years (see Figure 8(b)). As noted by Kudo et al. (2000), in Niigata City, the basin effects are significant due to fluvial river deposits. Based on this information, it is reasonable to consider that surface soil profiles at the Kawagishi-Cho and Showa Bridge sites are broadly similar in terms of surface site amplification and liquefaction potential.

Figure 10 shows the acceleration and velocity time-history data at Kawagishi-Cho. As noted by Kudo et al. (2000), the initial part of the record (before 7 seconds) is mainly due to P-wave, while the latter part is affected by S-wave and surface waves. They also indicated that ground motions between 7 and 12 seconds contain long-period component (having the peak spectral value around 5-6 seconds), and these can be attributed to surface waves significantly affected by the Niigata basin. According to Kudo et al. (2000), the liquefaction triggering had started around 12 seconds. To visually inspect the effects of liquefaction triggering in the top surface soil, response spectra of the NS and EW components of the Kawagishi-Cho record are computed (damping ratio = 5%) for the entire time-history data and for the first 12 seconds of the data (i.e. focusing on the part that is not significantly affected by liquefaction). The results are shown in Figure 11. The comparison of response spectra indicates that the short-period content of ground motions is relatively low despite the fact that the large earthquake occurred at short distance (note: although the shortest rupture distance is about 15-20 km, the hypocentral distance is about 55-60 km; according to Shiba and Uetake (2011), the main asperity is located near the hypocenter). The main reason for the low short-period response spectra is attributed to significant site/basin effects. Figure 11 also shows that the response spectra for the entire record and the first 12 seconds are similar for vibration periods less than 5 seconds; for the NS component, the inclusion of the time-history data affected by liquefaction results in additional peak at around 6-7 seconds. It is reminded that the 1964 Niigata earthquake occurred at the off-shore plate boundary and the shortest source-to-site distances for Niigata City (where Kawagishi-Cho and Showa Bridge are located) are about 15-20 km. Therefore, it is unclear whether 'typical near-fault motion' condition (for shallow continental crustal earthquakes) is applicable to this case. In other words, it is not straightforward to separate the directivity effects and site/basin effects in the recorded ground motions at Kawagishi-Cho. The next section therefore explores the variability of ground motion in greater details.
2.3 Variability of Ground Motions at Kawagishi-Cho and Showa Bridge Site

Variability of ground motions at nearby sites is investigated for the case of Kawagishi-Cho and Showa Bridge during the 1964 Niigata earthquake. The analysis presented herein is focused on the ground motion intensities during the initial part of the ground motions (i.e. prior to liquefaction triggering), to which ground motion models are applicable. In addition, several key considerations that are unique to the problem are noted:
(a) Firstly, the wave propagation paths from the source region to Kawagishi-Cho/Showa Bridge are considered to be similar based on the relative locations of the two sites and the source rupture zone (Figure 9);

(b) Secondly, the near surface site profiles at the two locations are broadly similar based on the surveyed soil profile (Figure 8(b)) and the fact that major liquefaction was actually observed at the two locations (Yoshida et al. 2007).

To estimate the ground motion intensity at Showa Bridge given the recorded motion at Kawagishi-Cho, a prediction tool that is based on statistical analysis of ground motion data is adopted – i.e. spatial correlation model of a ground motion parameter for a given scenario. The tool was developed by Goda and Atkinson (2010) and Goda (2011), calibrated using extensive actual ground motion data around the world; notably, the dataset analysed by Goda (2011) includes the 2004 and 2007 Chuetsu-(Oki) earthquakes, which occurred in the same region.

The procedure of the estimation is briefly mentioned. A typical ground motion prediction equation can be expressed as: \[ \log_{10} Y = f(M, R, V_{30}, \theta) + \varepsilon \] where \( Y \) represents the ground motion parameter of interest (e.g. PGA and spectral acceleration); \( f(M, R, V_{30}, \theta) \) is the median prediction model as functions of magnitude \( M \), distance \( R \), site parameter \( V_{30} \), and other parameters \( \theta \); \( \varepsilon \) is the intra-event residual. It is noted that the above equation is focused upon a single event (rather than multiple events, as in the typical cases for ground motion models; note: the result is valid for both cases). In this model, \( Y \) is modelled as lognormal variate with median \( f(M, R, V_{30}, \theta) \) (described by several physical parameters) and error term \( \varepsilon \). \( \varepsilon \) is assumed to be normally distributed with zero mean and variance of \( \sigma_{\varepsilon}^2 \). If one is interested in estimating a ground motion parameter at an unobserved site based on the ground motion parameter at a nearby observed site, an extended version of the above ground motion model can be employed. One notable aspect in this estimation is the consideration of spatial correlation of ground motion parameters at nearby sites. The correlation of \( \varepsilon \) at two locations can be given by the intra-event spatial correlation \( \rho_{\varepsilon}(\Delta, T) \), where \( \Delta \) is the separation distance between two sites and \( T \) is the vibration period. The details of \( \rho_{\varepsilon}(\Delta, T) \) can be found in Goda and Atkinson (2010) and Goda (2011). Now, consider that the ground motion parameter is available at Kawagishi-Cho and based on this information, the ground motion parameter at Showa Bridge is estimated. For the bivariate case, the error term at Showa Bridge is characterised by the normal distribution with mean equal to \( \rho_{\varepsilon}(\Delta, T) \times \varepsilon_{\text{Kawagishi-Cho}} \) and variance equal to \( (1 - [\rho_{\varepsilon}(\Delta, T)]^2) \times \sigma_{\varepsilon}^2 \). With this information, one can
easily assess the confidence interval of the ground motion parameter at Showa Bridge given the observed ground motion at Kawagishi-Cho. The key parameters in the estimation procedure are \( \rho_x(\Delta, T) \) and \( \sigma_x^2 \).

Another important information is the intra-event spatial correlation and to provide the empirical estimates of the correlation using extensive ground motion data worldwide, comparison of spatial correlations for the well-recorded 41 earthquakes is presented in Figure 12 (Goda, 2011). In addition, the results for the two relevant regional earthquakes are shown in Figure 13. The result shown in Figures 12 and 13 is the estimated intra-event spatial correlation at the shortest separation distance (\( \Delta \approx 2.5 \) km; 5 km bin size). This separation distance is the closest one can go (note: to estimate the spatial correlation coefficient for the closest separation distance bin, a sufficient number of data points (more than 50) was used (thus the estimates are relatively stable in a statistical sense). The results shown in Figures 12 and 13 suggest that \( \rho_x(\Delta, T) \) at the separation distance of 0.5 km is about 0.4-0.9; this variability is attributed to vibration period and different earthquakes. As the vibration period increases, \( \rho_x(\Delta, T) \) increases. For the considered case, the relevant vibration period is longer than 3 seconds (note: the correlation model is available up to 5 seconds). For this period range, \( \rho_x(\Delta, T) \) is between 0.7 and 0.9 (typical value is 0.8).

Values of the intra-event standard deviation \( \sigma_x \) of well-recorded earthquakes range from 0.15 and 0.4 (log 10 base); see Goda (2011). On average, \( \sigma_x = 0.3 \) is a reasonable choice. In particular, for the two relevant earthquakes in Niigata region, i.e. 2004 and 2007 Chuetsu-(Oki) earthquakes, values of \( \sigma_x \) are about 0.3-0.33. The mentioned values of \( \sigma_x \) is based on ground motion data distributed over a wide area (for a given event), while more detailed investigations that are focused upon specific site-path combinations suggest that the intra-event standard deviation is much less than the overall estimate. Specifically, the study by Morikawa et al. (2008) indicated that the reduction of \( \sigma_x \) can be as large as 60-70% (i.e. \( \sigma_x \) for the specific site-path combination becomes about (as low as) 0.1). Because the specific site-path is applicable to the situation discussed in this note, a reduction of \( \sigma_x \) can be justified; as a typical value, 50% reduction is considered in the following part.

Using the representative parameter values of \( \rho_x(\Delta, T) \) and \( \sigma_x \) (i.e. 0.8 and 0.15), the error term at Showa Bridge is characterised by the normal distribution with mean equal to 0.8 \( \varepsilon_{\text{Kawagishi}-\text{Cho}} \) and variance equal to \( 0.36 \times 0.15^2 = 0.0081 \) (i.e. intra-event standard deviation is 0.09 (log10 base)). Because the median ground motion prediction is almost identical (difference is caused by the
difference in rupture distance, which is less than 1 km), variability of the estimated ground motion is mainly characterised by the intra-event standard deviation; $\sigma_x = 0.09$ indicates that the 16-84% confidence interval of the ground motion parameter ratio at Showa Bridge and Kawagishi-Cho is between 0.813 and 1.230. In other words, about $\pm 20\%$ difference may be adopted as a representative range of variation of the ground motion parameter. It is noted that the effect of the mean shift is not explicitly considered herein because the comparison of the ground motion parameters is made for the specific two sites (rather than for the generic condition as in a ground motion model; as additional information, using the equation by Zhao et al. (2006), $\varepsilon_{Kawagish-Ch}$ is computed as about -0.1 to 0.05 for the vibration period of 4-5 seconds. Similar method has been used by Bhattacharya and Goda (2013) in analysing a building failure during the 1995 Kobe earthquake.

Figure 12. Estimated spatial correlations for 41 well-recorded earthquakes (Goda, 2011).
Kudo et al. (2000) suggests that the long period ground motion was not produced by liquefaction but it radiated from the same source. They attributed the essential nature of the ground motion to the earthquake source, propagation path and deep sediments of regional scale. Therefore, the ground motion recorded is also assumed not to have significant SSI (Soil-Structure Interaction) effects that may affect the conclusion to be drawn in the paper. The plots on Fig. 7(a) also show the window when the Showa Bridge collapsed. It may be observed that there is slight increase in acceleration i.e. a shock wave or a jolt during the time of collapse. It has been hypothesised (Kudo et al. 2000 and Yoshida et al. 2007) that this long period motion was presumably surface waves from the same earthquake source and travelled the same propagation path. From the ground motion, it is evident that the period of the ground is about 6-7 seconds during the bridge collapse.

2.4 Wavelet Energy Spectrum of the ground motion

Conventional trigonometric basis functions used in the Fourier analysis of the earthquake ground motions, as discussed above, may not reveal the temporal characteristics of the frequency content. Wavelet transform decomposes time-domain signals in time and frequency/period, localizes both of them in a single graph, and represents a time-domain function as a linear contribution of a family of basis functions. Wavelet energy spectrum is an engineering technique for tracing the energy and its relevant period and time through a recorded motion. In this section, energy spectrum has been used based on Mexican hat mother wavelet basis function (Zhou and Adeli 2003a, and 2003b). Fig. 7(b) shows the energy spectrum for NS component of recorded motion as shown in Fig. 7(a).
As is evident from the energy concentration of the energy spectrum (Fig. 7b), it may be reasonable to assume that the soil has started to liquefy from about 10 seconds of the earthquake and it is completely liquefied at around 25 seconds. Most of the energy of the time history will be dissipated by higher damping of the liquefied soil after this time. Hence concentration of energy is much weak after about 30 seconds. The shock wave or a jolt during the time of collapse of the bridge (i.e. around 70 seconds of the earthquake) transmits substantial amount of energy and is clearly evident from the energy concentration of the spectrum in Fig. 7(b). This also corroborates with the hypothesis of Kudo et al (2000) and Yoshida et al (2007).

2.5 Orbital plots of acceleration and displacement

Figure 14 plots the orbital acceleration and displacement plotted for the time window 65-75 seconds i.e. during which the bridge failed. The bold line in the figures represents the orientation of the Showa Bridge (i.e. 30° North-West). From the orbital plots of the ground displacements, it is clear that there was cyclic ground displacement i.e. the ground was displacing probably back and forth whereas lateral spreading (permanent unidirectional soil flow) started at about 83 seconds, Yoshida et al. (2007). However no precise magnitude of ground displacement can be estimated for the Showa Bridge location. The magnitude of displacement at the recording site in the direction of bridge (30° North West) is about 22 cm as shown in Fig. 14(b). These values of ground displacement have been used for displacement based analysis. It must be mentioned that these values are the best educated guess and may not be the exact magnitude of displacement at the Showa bridge site. However, based on the conclusions reached by Kudo et al. (2000) that the long period ground motion was not produced by the liquefaction but radiated from the same source, the assumption of ground displacement of 22 cm may not be a bad estimate and may provide us with the valuable qualitative/quantitative information on the Showa bridge collapse.

Figure 14: Orbital ground motion plotted for the time window 65 to 75 seconds i.e. during which the bridge failed: (a) Ground acceleration (b) Ground displacement
3.0 EFFECT OF INERTIAL FORCE AND GROUND DISPLACEMENT ON THE SHOWA BRIDGE COLLAPSE

3.1 Cyclic longitudinal scratch on the girders and the inertial forces

Based on the design of the bridge, the relative movement needs to be about 30cm for the girder to dislodge from the pier cap. As shown in Fig. 5, the Showa Bridge deck was composed of panels, each resting alternatively on movable and fixed supports. Fig. 15 shows cyclic longitudinal scratches found at the bottom of the girders at the movable supports suggesting that the friction forces were overcome and the girders moved under the inertial earthquake action. Therefore, non-catastrophic inertial relative displacement did occur during the first few seconds of strong ground shaking. Hence, it may be reasonable to infer that the strong earthquake motion resulted in some lateral deformation of the piles, but it was not adequate to directly cause the failure of the bridge. Therefore, effect of inertial action in the initial part of the strong shaking is not taken into account in the subsequent analyses.

Figure 15: Damage to the shoe of a movable joint of the Showa Bridge, Towhata (1999)

3.2 Method of analysis

Though studies on two-dimensional and three-dimensional soil-pile interaction have been carried out in the recent past (Finn and Fujita 2002, Elgamal et al. 2009, Maheshwari and Sarkar 2011, Sarkar and Maheshwari 2012), a relatively simple but detailed nonlinear BNWF (Beam on Nonlinear Winkler Foundation) model is prepared to study the response of the bridge pile subjected to a combination of ground displacement and axial load (Fig. 16). In this study, dynamics of problem has been modelled by displacement-based method adapted by pseudo static analysis and soil movement distribution based on linear variation with depth (Tokimatsu et al., 2005). It must be mentioned that axial load from the deck was acting on the pile at all times during the earthquake. The analysis of the BNWF model is carried out by a finite element based structural analysis program SAP 2000 (CSI, 2004).
3.3 Soil-pile model

The 25m long pile passes through a four-phase system of air, water, liquefied soil and non-liquefied soil surrounding it. The pile is modelled as a beam-column element. The soil surrounding the pile is modelled as lateral soil springs (p-y spring). The superstructure of Showa Bridge, i.e., the bridge deck was composed of girders each alternatively resting on roller and fixed support over the pier cap. The construction of the bridge was such that one end of the girder was locked and the other end was free to slide longitudinally off the piers. Once the liquefaction starts, the pile head supporting the bridge deck undergoes large displacement and resistance offered from the bridge deck is minimized and the pile head acts similar to free head. The present analytical model considers the boundary condition at pile head as free. Present analysis also assumes that the pile is stable under vertical settlement, hence the support condition is considered as a hinged support at the tip of the pile. The dead weight from deck slab acting on the pile is calculated by Bhattacharya et al. (2005) to be 740kN.

Figure 16: Displacement based model of the Showa Bridge pile subjected to lateral force due to soil movement
3.4 Soil model

The top 10m soil surrounding the pile liquefied during the earthquake. Hence, during liquefaction state, only the bottom 6m of non-liquefied soil was providing lateral support to the piles. The nonlinear springs properties (p-y curve) to represent the bottom 6m soil are calculated according to the API (2003) guidelines. The in-situ relative density ($D_r$) of the soil is established from the experimental value of ‘N’ of standard penetration test as per the correlation given below (Meyerhof 1957).

$$D_r = 21 \left( \frac{N}{0.7 + \sigma_v / 98} \right) \text{ (\%)}$$

where, $\sigma_v$ is the effective overburden stress in kPa at the depth of SPT.

From typical stress-strain response of liquefied soil obtained from multi-stage triaxial testing, it is observed that in the initial phase of straining of liquefied soil, there is a zone of zero-resistance depending on the relative density of soil (for example see Yasuda et al. 1999, Vaid and Thomas 1999, Shamoto et al. 1997 and Kokusho et al. 2004 etc). Beyond this threshold strain, there is increase in resistance probably due to suppressed dilation. Rollins et al. (2005) also observed similar load-deflection curve of a pile during the full-scale testing where the soil surrounding the pile was liquefied by blast. In this study, the effective stress at the base of the liquefied soil layer is assumed to be zero considering the initial zone of zero resistance though there may be some residual stress in the soil during the process of liquefaction. The spring properties of the bottom 6m soil is estimated as if the soil layer is at the ground level. Fig. 10 shows the schematic of the modelled soil spring. The soil spring parameters for the bottom 6m non-liquefied soil used in the analysis is obtained from API (2003) and further details can be found in Dash et al. (2010). The submerged unit weight of soil is assumed as 10kN/m$^3$.

3.5 Structural details of the bridge pile

The foundation of each supporting pier was a single row of 9 tubular steel piles connected laterally by a pile cap. Each pile was 25m long with outer diameter (D) of 0.609m. The wall thickness of the upper 12m of the pile was 16mm and the bottom 13m thickness was 9mm. The material of the Showa Bridge piles, as per the Japanese standard JIS-A: 5525 (JSA, 2004) was assumed to be SKK490 grade steel pipe with the yield strength ($\sigma_y$) and ultimate strength ($\sigma_u$) of 315MPa and 490MPa respectively. The stress-strain behaviour of the pile is presented in Fig. 17. Table 1 shows the sectional details and capacities of the of the pile section adopted for the analyses.
Table 1: Structural details of the Showa Bridge pile

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Note:
P_y = Yield capacity of pile in axial compression or tension
P_u = Ultimate capacity of pile axial compression or tension
M_y = Yield moment capacity of pile
M_p = Plastic moment capacity of pile
a: for P = 0 kN; b: for P = 370 kN; c: for P = 740 kN;

3.6 Analysis approach: Displacement based approach

Ground displacements are applied at the free ends of the p-y springs of the liquefied layer (Figure 16) to model the lateral soil flow. This applied ground displacements are assumed to be relative to the bottom of non-liquefied soil layer. The p-y springs of the liquefied soil are modeled by reducing the strength and stiffness of the springs using a reduction factor, the p-multiplier. Though many p-multiplier values are reported in literature based on (N1)_w value of soil (AIJ 2001, Brandenberg 2005, RTRI 1999), there is no consensus on which value to be adopted. This study uses representative (N1)_w value of 10 for the liquefied clean sand to obtain the p-multiplier value (Idriss and Boulanger, 2008). For this (N1)_w value the reduction factors according to AIJ (2001), Brandenberg (2005) and RTRI (1999) are 1/10, 1/50, and 1/1000, respectively. Referring to the discussion in the Soil model section, it may be mentioned stress-strain responses of the liquefied soil show zone of zero resistance up to some threshold strain and increase in resistance after that strain.
value. So discarding the higher and lower estimates of the reduction factor, p-multiplier value of 1/50 (Brandenberg 2005) has been adopted for the present analysis in order to obtain a reasonable estimate of the response soil-pile system under liquefying soil condition.

### 3.7 Analysis procedure

Details of the methodology of analysis can be found in Dash et al. (2010). To make the paper self explanatory, salient features are reiterated in this section. The axial load is present throughout the lateral loading phase and a nonlinear pseudo-static analysis was performed by using SAP 2000 (CSI, 2004), which is essentially a modified time history analysis. In the time history analyses, the damping and mass of the system was forced to be near zero value to make it pseudo-static. As shown in Fig. 18, the pile is first subjected to the full axial load ($P_{\text{max}}$) and then the lateral load was applied by increasing the ground displacement linearly up to its maximum ($\Delta_{\text{max}}$), keeping the axial load constant. To ensure gradual increase of loading, time values at A, B and C in the figure were defined arbitrarily as 0s, 60s and 400s for both axial and lateral loading. This is necessary for nonlinear pseudo-static analysis and the analysis also includes P-delta and large displacement effects.

![Loading function used for the study](image)

#### Figure 18: Loading function used for the study

### 3.8 Analysis considerations

Analyses were carried out considering three different axial load conditions as described in the Table 2.

**Table 2: Different analyses performed**

<table>
<thead>
<tr>
<th>Axial load, P(kN)</th>
<th>Remarks</th>
</tr>
</thead>
<tbody>
<tr>
<td>$P_{\text{max}} = 0$</td>
<td>Analysis without axial load considerations.</td>
</tr>
<tr>
<td>$P_{\text{max}} = 370$</td>
<td>The static load acting on the pile is half of the dead load. This may represent the condition when one deck has completely dislodged and the lateral flow of soil continues i.e. Pier P4 in Fig. 3 (Yoshida et al. (2007)).</td>
</tr>
</tbody>
</table>
3.9 Results of the analyses

To compare the results, spatial variability of the ground displacement is ignored in this study i.e. peak ground displacement of 22cm (see Figure 14) is assumed to be applicable to all the piles as lateral spreading is yet to start. Failure criterion of the pile is taken to be the condition when the displacement of deck is larger than 0.5D (leading to unseating of the deck, see Figure 5) or the maximum bending moment in pile is close to the plastic moment capacity, $M_p$ (leading to plastic hinge formation), the values of which can be found in Table 1.

Based on the analyses, deck displacements equivalent to the pile head deflection are plotted against the peak ground displacement in Figure 19. The maximum bending moment in the pile as a fraction of plastic moment capacity of the pile section is also indicated in the figure by using a star mark. It may be observed that the pile head deflection, for the ground displacement of 0.22m and full axial load condition (740kN), is well above the limiting deflection of 0.3m (0.5D) to resist the unseating of the deck. However, the moment induced in the pile section is well below the plastic moment capacity ($M_p$). This implies that the peak ground displacement of 22cm in the time frame of 65s-75s of the earthquake coupled with the full axial load of 740kN is sufficient to dislodge the deck from the pile cap leading to collapse of the bridge. It must be mentioned however that the actual ground displacement experienced by the pile will be relative to the non-liquefied hard layer and will be lower than 22cm.
For the analysis with ground displacement as lateral load and axial load of 370kN, the predicted pile head deflection is just about the limiting deflection of 0.3m to dislodge the deck at the peak ground displacement. On the other hand, the pile head deflection from the analysis without considering the axial load is well below the limiting deflection of 0.3m suggesting that the failure is not predicted in this condition.

Based on the analyses and the failure prediction obtained, factor of safety, FOS (ratio of the deflection required to unseat the deck slab to the pile head deflection), has been computed and the observations may be summarised in the Table 3. Therefore, considering the liquefaction of the soil layer during the strong shock, the ground displacement of 22cm coupled with the axial load from the deck (i.e. total dead weight of 740kN from deck slab) can reasonably predict the collapse of the bridge.

It may also be noted that the applied ground displacement profile in the analysis shown in Figure 16 is relative to the bottom nonliquefied soil layer. It may also be mentioned that the recorded ground displacement time history shown in Figure 7 is not the value relative to the layer underlying the liquefied soil but the absolute value. Hence the peak ground displacement of 22cm as obtained
from Figure 8 is absolute and relative ground displacement may further be less depending on the characteristics of the strong motion (phase angle) and cyclic ground displacement. Hence the relative deck displacement obtained from the analysis and subsequently employed for the prediction of the collapse of the bridge would also be less based on the application of relative ground displacement profile.

Based on the analysis presented, it may be concluded that the ground displacement only may not be capable to explain the collapse of the bridge with full conviction. The next section of the paper, therefore, explores the effects of dynamics of the shock wave or jolt on the bridge at the time interval of 65-75 seconds (see Figure 7(a) and 7(b) i.e. recorded ground motion section).

<table>
<thead>
<tr>
<th>Failure Condition</th>
<th>Factor of Safety, FOS, against unseating of the deck</th>
<th>Prediction of bridge failure &amp; Remark</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ground displacement of 22cm without axial load ( (P = 0) )</td>
<td>FOS &gt;1.0</td>
<td>Not predicted</td>
</tr>
<tr>
<td>Ground displacement of 22cm coupled with axial load ( P = 370 \text{kN} )</td>
<td>FOS = 1.04</td>
<td>Almost predicted</td>
</tr>
<tr>
<td>Ground displacement of 22cm coupled with axial load ( P = 740 \text{kN} )</td>
<td>FOS &lt;1.0</td>
<td>Predicted but the applied displacement of 22cm is absolute not relative to the pile base. Actual displacement will be lower depending on the characteristics of the strong motion (phase angle) and cyclic ground displacement.</td>
</tr>
</tbody>
</table>

4.0 EFFECT OF DYNAMICS ON THE BRIDGE COLLAPSE

4.1 Estimation of period

The fundamental period of a bridge deck-pile-soil system will change with the liquefaction-induced-stiffness degradation of the soil surrounding the pile. The fundamental period, in most cases, will lengthen depending on the thickness of the liquefied soil layer. This has been shown through high quality experimental results carried out by Lombardi and Bhattacharya (2013) and analytical work by Bhattacharya et al (2008) and Adhikari and Bhattacharya (2008). To examine the effects of thickness of the liquefied soil layer on the period of pile foundations of the Showa Bridge, an idealised pile configuration has been adopted as shown in Figure 20(a).

The pile is assumed to be fixed at a depth of 4D below the liquefied soil layer (for further details see Bhattacharya et al. 2005). Weight from the deck on the pile is applied as mass, \( M \) on the free head of the pile. The fundamental period of the pile is then computed by considering the pile
to be simple cantilever for different length of the liquefied soil layer, \( L \), and is shown in Figure 20(b). The simplified assumption is that liquefied soil offers no stiffness to small amplitude vibrations, the discussion of which can be found in Bhattacharya et al. (2009). It may be observed that the period increases with increasing thickness of the liquefied soil layer. For liquefied soil thickness of 10m as in case of pier \( P_4 \), the fundamental period of the pile system increases from 2seconds before liquefaction to about 6seconds after liquefaction.

4.2 Check for resonance

Based on the recorded motion, it can be estimated that the period of ground motion is 6 to 7 sec at about 70 sec after the onset of the earthquake. Assuming 10m of resonant wavelength of liquefied layer, the equivalent shear wave velocity can be estimated to be about 6.7m/s (see equation 1):

\[
\frac{vT}{4} = 10 \quad \Rightarrow \quad v = \frac{40}{T} = \frac{40}{6} = 6.7 \quad \text{m/sec}
\]  

(1)

This post-liquefaction shear wave velocity of soil is very small and transient stiffening of sand due to dilatancy mechanism in undrained condition is sometimes assumed to provide higher shear wave velocity rather than zero (theoretically value for fully liquefied ground). Variation of average shear wave velocity through post-liquefaction regime has been previously shown by Zeghal and Elgamal (1994), Elgamal, et al., (1996), and Davis and Berrill (1998) to be around 4 m/sec to 15 m/sec in Wildlife Array, California, in Superstition Hills 1987 earthquake, and Port Island in Kobe 1995 earthquake.
The acceleration, velocity and displacement spectra considering a Single Degree of Freedom (SDOF) system for the base motions as shown in Figure 21(a) are obtained with damping constant $\zeta$ of 5% and 20%. Though the earthquake time histories shown in Figure 7 are recorded on the surface and ideally deconvoluted motions shall be used for the study, the recorded surface motions are used directly as base motion. The assumption will not, however, deter from overall big picture of the resonance mechanism being studied. The acceleration, velocity and displacement spectra are shown in Figure 21 and it may be observed that the spectral displacement reaches its peak at the period range of 6-7 seconds. An acceleration displacement response spectrum (ADRS) is plotted in Figure 22 for better comparison of the spectral behaviour.
Figure 21: Acceleration, velocity and displacement spectra for a SDOF system for the time histories mentioned in Figure 7 for damping of 5% and 20%

Figure 22: Acceleration-displacement response spectra for a SDOF system for the time histories mentioned in Figure 7 for damping of 20%
It is also evident from Figure 22 that displacement is higher at the time period of 6 seconds and hence the response of the system will be high period or low frequency ground motion sensitive. The displacement time histories for a SDOF system with a period of 6 seconds for the specified base motions are shown in Figure 23. The displacement time histories show peaks in the time range of 10s-25s and then an increase at the time window of 65s-75s. It may also be observed from Figure 7(b) that the period of motion in the time window of 65s-75s is around 6-7 seconds. Wavelet Energy Spectrum in Figure 7(b) also shows that the amplitude of the energy at around 70 sec. is 6.5 m$^2$/s$^4$ which is more than half of the maximum energy at 20 sec (12 m$^2$/s$^4$). It implies that for fully liquefied ground, considerable energy is transmitted to pile due to the jolt in post-liquefaction regime.

![Displacement time histories for a SDOF system with period $T=6$ seconds and damping of 20%](image)

Figure 23: Displacement time histories for a SDOF system with period $T=6$ seconds and damping of 20%

Due to the tuning of the period of the bridge (circa 6 second, see Figure 20) and the period of the ground (circa 6 to 7 seconds, see Figure 7(b)) at that time about 70 second, it is highly likely that this may have initiated the collapse or contributed to the collapse. Therefore, it may be hypothesized that resonance between ground motion and the bridge combined with the additional energy due to the jolt can be a major contributor as the bridge collapsed roughly at 72s though the
ground displacement was larger at initial 10-25s. Haldar et al. (2008) also investigated the failure of the Showa Bridge and they concluded that the soil of the riverbed under the bridge liquefied sequentially and hence the flexibility of the soil-pile system increased with time. Yoshida et al. (2007) and Kerciku et al. (2007, 2008) were also of the same opinion.

**DISCUSSION**

The role of in-depth analysis of case histories cannot be underestimated. Collapse of Showa Bridge provides a unique insight into various failure mechanisms that needs to be checked for any bridge. Three broad failure mechanisms for Showa Bridge piles can be postulated:

1. Bending failure due to inertia in the first part of the strong motion. This can be discarded as the bridge did not fail in the initial 10 seconds.

2. Bending failure due to lateral spreading: This failure mechanism can be discarded as lateral spreading started at about 83 seconds after the bridge collapsed. Also the piles close to the bridge abutments did not fail where the lateral spreading was known to be severe. On the contrary, the piles in the middle of the bridge failed where the lateral spreading is expected to be the least.

3. The proposed mechanism is the tuning of the bridge with the ground during the jolt causing large displacement at the pile which may have unseated the deck. It may also be mentioned that the depth of the liquefied layer is more towards the left half of the bridge as is evident from the liquefaction profile shown in Figure 6. Depending on the thickness of the liquefied soil layer, the flexibility of the soil-pile system is more towards the left half of the bridge and hence possibility of greater pile head deflection due to resonance. Therefore, depending on the thickness of the liquefied layer and resulting resonance (tuning with the earthquake), the deflections at the pile head is more on the left half of the bridge and is adequate to unseat the bridge deck. This could explain the reason why collapse was mainly observed on the left half of the bridge.

4. The current codes of practice or design guidelines does not consider all the above failure mechanisms. It is therefore necessary to carry out seismic requalification studies of bridges in liquefiable areas. A method to carry our seismic requalification studies is given by Sarkar et al (2014)

**5.0 CONCLUSION**

Quantitative back-analysis has been carried out to understand the failure mechanism of Showa Bridge. Following major conclusions may be summarised from the present study:
1. Due to liquefaction induced soil stiffness degradation, time period of the middle of the bridge (pile-soil-pier-deck system) increased from about 2 seconds to about 6 seconds. This resulting high period of the bridge falls in the displacement sensitive zone of the response spectra. Also the natural period of the liquefied soil falls in the range of 6-7 seconds in the time window of 65-75 seconds leading to resonance between the ground motion and the bridge. This resonance coupled with the jolt at 70 seconds of the earthquake is thought to be a major contributor of failure of Showa Bridge.

2. Soil liquefaction profile as estimated by Hamada and O’Rourke (1992) shows more depth of liquefaction on left half of the bridge. Depending on the thickness of the liquefied soil layer and the corresponding period lengthening of the soil-pile system more tuning with the earthquake (i.e. resonance) and enhanced pile head deflection is expected on the left half side of the bridge. This may explain the observation that collapse occurred only on the left half of the bridge.
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