The SDSS-IV extended Baryon Oscillation Spectroscopic Survey: selecting emission line galaxies using the Fisher discriminant


1. Introduction

Large optical imaging surveys in astronomy, such as the Sloan Digital Sky Survey (SDSS, York et al. 2000) or the Canada-France-Hawaii Telescope Legacy Survey (CFHTLS, Gwyn 2012), have revolutionised the fields of galaxy evolution and cosmology. Indeed, they enable the photometric selection of large, controlled galaxy populations over either a very wide area or up to faint magnitudes. Such large, homogeneous galaxy samples are needed to define target catalogues for intensive spectroscopic surveys (e.g., the Main Galaxy Sample: Strauss et al. 2002; the VIMOS VLT Deep Survey, VVDS: Le Fèvre et al. 2005, 2013). Those spectroscopic surveys are then used to measure galaxy...
properties (e.g., Kauffmann et al. 2003; Ilbert et al. 2005) or cosmological parameters (e.g., Eisenstein et al. 2005; Percival et al. 2010; Anderson et al. 2012) with high statistical accuracy. In addition, the photometric galaxy samples themselves can also put interesting constraints on galaxy evolution or cosmology (e.g., van Dokkum et al. 2010; Seo et al. 2012).

In this context, a significant step was taken by the Baryon Oscillation Spectroscopic Survey (BOSS, Dawson et al. 2013), which uses 1.5 million galaxies over 10 000 deg$^2$ selected in the SDSS, to precisely measure the scale of the baryon acoustic oscillations (BAO) to redshifts $z < 0.6$, and 160 000 quasars to produce measurements at $z > 2.1$ using the quasar Lyman-$\alpha$ forest (Delubac et al. 2015; Font-Ribera et al. 2014).

The main goal of the BOSS survey is to put a cosmological constraint on dark energy through the measurement of the BAO, but its legacy for galaxy evolution will also be unique. The BOSS observations ended in early 2014, and the data were released as part of the DR11 and DR12 (Alam et al. 2015).

Building on the success of the BOSS survey, the extended Baryon Oscillation Spectroscopic Survey (eBOSS, Dawson et al. 2015) will use four different tracers of the underlying density field to expand the volume covered by BOSS focussing on the $z$ range $0.6 < z < 2.2$. The four eBOSS tracers are i) luminous red galaxies (LRGs) at $z < 0.7$; ii) emission line galaxies (ELGs) at $z < 0.8$; iii) quasars (at $0.9 < z < 2.2$); and iv) Lyman-$\alpha$ absorbers in the line of sight of high-redshift ($2.1 < z < 3.5$) quasars.

For the ELG tracers, 300 spectroscopic plates (BOSS plates have a $\sim 7$ deg$^2$ circular area and 900 fibres) are to be dedicated to observing 270 000 targets as potential ELGs in the South Galactic Cap (SGC). The choice of targeting ELGs is motivated by the presence of the [OII] emission line in the ELG spectrum, which permits an efficient redshift measurement with $\sim 1$ h of exposure time. The requirement for ensuring a measurement of BAO parameters with a precision of $\%$ with ELGs is to obtain the spectroscopic redshift measurements of 190 000 ELGs in the $0.6 < z_{\text{spec}} < 1.0$ redshift range with a precision better than 300 km s$^{-1}$, with $\%$ of catastrophic failures (precision greater than 1000 km s$^{-1}$). To fulfil those requirements, the initial eBOSS/ELG settings are an area of 1500 deg$^2$ and a 180 deg$^{-2}$ target density with a minimal efficiency of 70%, where we define the efficiency as the number of ELGs with a reliable $z_{\text{spec}}$ measurement with $0.6 < z_{\text{spec}} < 1.0$ divided by the number of targets. We used those values for the baseline of this study. The technique we propose here has the advantage of being flexible, thus could be adopted in the case where the final eBOSS/ELG requirements should differ from those values. For instance, for the eBOSS ELG programme a fibre density of 170 deg$^{-2}$ is assumed in Dawson et al. (2015) – hence shifting the minimum required efficiency to $74\%$ – as 10 deg$^{-2}$ fibres are reserved for other targets.

This paper is part of a series of papers analysing the properties of $z \sim 0.8$ ELG selection, paving the way for the final eBOSS ELG selection. This paper (Paper II) introduces a new method of selecting $z \sim 0.8$ ELG based on the SDSS detected objects and describes the redshift and [OII] properties of the selected galaxies. In Delubac et al. (2015, Paper III), we present the catalogue of the selected ELGs, along with various homogeneity and systematics tests. Comparat et al. (2015a, Paper I) study the [OII], H$\beta$, and [OIII] emission lines measurement at $z \sim 0.8$ with the BOSS spectrograph (Smeel et al. 2013), aiming to better understand the redshift estimation and the selected galaxy properties. It also details the spectroscopic observations dedicated to the preliminary study of ELG selection. Jouvel et al. (2015, Paper IV) analyses the properties (redshift, homogeneity) of a $z \sim 0.9$ ELG selection based on the Dark Energy Survey (DES$^1$; The Dark Energy Survey Collaboration 2005) photometry.

In this paper, we present a novel method of select $z \sim 0.8$ ELGs. Compared to the initial tests, which only used the optical bands (see Paper I), our analysis additionally includes one near-infrared band, hence adding one dimension to the colour–colour space. The most common method of selecting galaxies for a spectroscopic survey is to apply cuts in magnitudes and colour–colour spaces. It has been used for the surveys targeting a given redshift range (e.g., DEEP2: Newman et al. 2013; VIPERS: Guzzo et al. 2014) or for the surveys used for BAO measurements (e.g., SDSS/LRG: Eisenstein et al. 2001; WiggleZ: Drinkwater et al. 2010; the upcoming DESI/LRG-ELG$^2$). However, such an approach has some limitation when using a large number of multi-wavelength observations: when dealing with three or more colour–colour diagrams, the selection-box definition starts to be subjective, unless using an automatic exploration of all the possibilities. One possibility is to use neural networks (e.g., for the BOSS/QSOs: Dawson et al. 2013), which can bring efficient selections but at the cost of a less tractable selection. We introduce an alternative approach, the Fisher discriminant, which is equivalent to a hyperplane cut in the full colour space, that is to say, a cut on a simple linear combination of the colours. This hyperplane is automatically defined from a training sample and a list of criteria, which are here a redshift of $\sim 0.8$ and significant [OII] emission. We note that this approach – not used in astrophysics to our knowledge – is automatic and can be used in other situations where one wants to select a given population from multi-wavelength photometry, given that a training sample is available. We present in Sect. 2 the Fisher discriminant approach, then we introduce in Sect. 3 the photometric and spectroscopic data used in this study. We present in Sect. 4 the improvement with using the WISE/W1 data. Section 5 is dedicated to the tested $z \sim 0.8$ ELG selection schemes: we first describe them and then analyse their global properties in terms of redshift and [OII] emission. For two of the selections, we present stacked spectra and structural properties in Sect. 6. Finally, we conclude in Sect. 7.

In this paper, we adopt $H_0 = 70$ km s$^{-1}$ Mpc$^{-1}$, $\Omega_m = 0.30$, and $\Omega_\Lambda = 0.70$. All magnitudes are expressed in the AB system and corrected for the Galactic foreground extinction using the Schlegel et al. (1998) maps.

2. Fisher discriminant method

2.1. Principle

The goal of the linear discriminant analysis (LDA, Fisher 1936), also known as the Fisher method, is to define a discriminant (the Fisher discriminant $X_F$) that separates two known classes of a set of events best. We assume we have a collection of events $(y)$ where each event $y$ is known to belong to one of the two classes, $(y_1)$ and $(y_2)$. To each event are associated $N$ measurements: $y = (x_1, x_2, \ldots, x_N)$, each $x_i$ being a real variable measuring a given property. For instance, in the original taxonomic work of Fisher (1936), the two classes $(y_1)$ and $(y_2)$ are two different species of iris, Iris setosa and Iris versicolor; the events $y = (x_1, x_2, x_3, x_4)$ are a sample of fifty plants, for each of which are available four

\footnote{1 http://www.darkenergysurvey.org}
\footnote{2 Dark Energy Spectroscopic Instrument: http://desi.lbl.gov/cdr/}
Fisher discriminant for each event, the Fisher discriminant was obtained with Eq. (1) to a common scale, in order to facilitate the comparison between Fisher expressions. More precisely, we multiply it by a coefficient and add a constant value, so that the $X_1$ distribution for a complete subsample (the VVDS, see Sect. 3.2) has a mean value of 0 and a standard deviation of 1.

Our aim is to select ELGs at $0.6 \leq z_{\text{spec}} \leq 1.0$; we need to choose how to define the two considered classes, the $\text{Signal}_1$ and the Background classes. A first possible approach to define the two considered classes is to use criteria on both the spectroscopic redshift $z_{\text{spec}}$ and the total $[\text{OII}]$ flux $f_{\text{[OII]}}^{\text{tot}}$, with defining our $\text{Signal}_1$ class with galaxies in a high-redshift range and with a significant total $[\text{OII}]$ flux.

However, $f_{\text{[OII]}}^{\text{tot}}$ is available for relatively few galaxies compared to $z_{\text{spec}}$, which is a quantity usually provided in public surveys. To cover the maximum variable space, we can also take advantage of the fact that in our targeted redshift range, a large majority of galaxies are star-forming (e.g., Ilbert et al. 2013), as the star-formation rate density of the Universe is about ten times higher at $z \sim 1$ than today (e.g., Lilly et al. 1996; Madau et al. 1998; Hopkins & Beacom 2006). A possible alternate approach is to define our $\text{Signal}_1$ class only with galaxies in a high-redshift range. Proceeding in this way would allow us to use a large spectroscopic training sample, representative of the main types of galaxies at all redshifts.

Fig. 1. Illustration of the Fisher discriminant method with $N = 2$. The $(y_1)$ class is in blue dots, with the blue cross at $\bar{y}_1 = (3.5, 3)$, while the $(y_2)$ class is in pink triangles, with the pink cross at $\bar{y}_2 = (3, 2)$. For each event, the Fisher discriminant $X_FI$ corresponds to its orthogonal projection along the axis defined by $\bar{y}_1$ and $\bar{y}_2$. The dashed line illustrates the hyperplane used to split the events in two classes.

measurements done on the sepal and the petals. We then let $n_1$ and $n_2$ be the number of events in each class, $\bar{y}_1$ and $\bar{y}_2$, the means over each class, and $T$ the total variance-covariance matrix of the sample $(\bar{y})$.

The Fisher discriminant $X_{FI}$ is a linear combination of the $N$ variables $x_i$, aiming to provide the best separation between the two classes of events $(y_1)$ and $(y_2)$. In the $N$-dimension space of the measurement variables, it defines a hyperplane (dimension $N - 1$). This hyperplan is orthogonal to the axis defined by the line connecting $\bar{y}_1$ and $\bar{y}_2$, along which the distance between the projected points will naturally be a maximum. In other terms, the Fisher discriminant $X_{FI}$ is the orthogonal projection on this axis, as illustrated in Fig. 1 for $N = 2$. In his original work, Fisher (1936) proposed to normalise the projected distance by the quadratic sum of the projected dispersion of each class:

$$X_{FI} = \frac{n_1 n_2}{n_1 + n_2} (\bar{y}_1 - \bar{y}_2)^T T^{-1} y.$$  \hspace{1cm} (1)

A threshold value $X_{FI, \text{min}}$ is then used to associate the events with $X_{FI} < X_{FI, \text{min}}$ to the $(y_1)$ class and the events with $X_{FI} > X_{FI, \text{min}}$ to the $(y_2)$ class.

2.2. Application to ELGs

We now describe how we apply the Fisher discriminant approach to ELGs. The considered variable space is the galaxy colour space, and we compute the Fisher discriminant quantity $X_{FI}$ through the use of a spectroscopic sample of galaxies (presented in Sect. 3.2). As for any learning method, the training and test sample should ideally be as representative as possible of the data we want to apply the method to. This is the case in our study, where the training and test samples have homogeneous photometry coming from the surveys planned to be eventually used in eBOSS/ELG (except for the DECaLS data that we mimic with degrading the CFHTLS data; see Sect. 3.1). Please note that, as we test several selection schemes defined with different Fisher discriminants $X_{FI}$, we rescale the Fisher discriminant $X_{FI}$ obtained with Eq. (1) to a common scale, in order to facilitate the comparison between Fisher expressions. More precisely, we multiply it by a coefficient and add a constant value, so that the $X_1$ distribution for a complete subsample (the VVDS, see Sect. 3.2) has a mean value of 0 and a standard deviation of 1.

3. Data

In this section, we describe the data used in our study. First, we present the photometric data with which the ELG selection is done, then we describe the Fisher training sample used to define the tested Fisher discriminants $X_{FI}$; finally, we introduce the spectroscopic data used to quantify the efficiencies of the tested Fisher selection algorithms. We display in Fig. 2 the sky locations of the different surveys of interest in this study.

3.1. Photometry

We here present the different photometric surveys we use in this study to estimate object colours. We test different schemes, based on objects detected in the SDSS. The general properties of the used photometry are summed up in Table 1. We note that the issues related to colours computed with magnitudes measured through different surveys are significantly mitigated for our SDSS-SCUSS-WISE colours, because our SCUSS and WISE photometry is done consistently with the SDSS (forced photometry on SDSS objects, using SDSS structural information: Lang et al. 2014; Zou et al. 2015).

SDSS. The SDSS (York et al. 2000; Alam et al. 2015; DR12) provides photometry in the optical $ugriz$ broad-bands to a depth of $r \sim 22.5$ mag over $\sim 15000$ deg$^2$ of high-latitude sky, split into two regions of $\sim 7500$ deg$^2$, namely the Northern Galactic Cap (NGC) and the Southern Galactic Cap (NGC). Since we are interested in galaxy colours, we use the modelMag magnitudes\footnote{http://www.sdss.org/dr12/algorithms/magnitudes/#mag_model}; those are computed through a luminosity profile – fitted to the $r$-band data – convolved with the PSF in each band, and this permits unbiased colour measurements in
the absence of colour gradients. Our photometric object detection list is constituted of objects from the PhotoPrimary list\(^4\).

**WISE.** The Wide-Field Infrared Survey Explorer (WISE; Wright et al. 2010) measured the full sky in four mid-infrared bands centred on 3.4 μm, 4.6 μm, 12 μm, and 22 μm, known as W1 through W4. We make use of the “forced photometry” done on the SDSS objects here (Lang et al. 2014); this photometry uses measured SDSS source positions, star-galaxy separation, and galaxy profiles to define the sources whose fluxes are to be measured in the WISE images. In this work, we use only the W1 channel, because it appeared during our preliminary studies that also using W2 creates spatial inhomogeneities in our selections, thus reflecting the underlying variations in the signal-to-noise ratio in W2.


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**Table 1. Photometric data properties summary (Sect. 3.1).**

<table>
<thead>
<tr>
<th>Survey</th>
<th>BOSS/SGC (~3100 deg(^2)) coverage</th>
<th>BOSS/NGC (~7500 deg(^2)) coverage</th>
<th>Band depth (mag)</th>
</tr>
</thead>
<tbody>
<tr>
<td>SDSS</td>
<td>100%</td>
<td>100%</td>
<td>(g = 23.1, r = 22.7, i = 22.2, z = 20.7)</td>
</tr>
<tr>
<td>WISE (forced photometry)</td>
<td>100%</td>
<td>100%</td>
<td>(W1 = 20.3)</td>
</tr>
<tr>
<td>SCUSS</td>
<td>100%</td>
<td>–</td>
<td>(u - 23)</td>
</tr>
<tr>
<td>DECaLS/DR1 (CFHTLS-Wide degraded)</td>
<td>~30%</td>
<td>~45%</td>
<td>(z = 22.7)</td>
</tr>
</tbody>
</table>

**Notes.** Reported depths correspond to a 5\(\sigma\) point-source detection.

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SCUSS. The South Galactic Cap u-band Sky Survey (SCUSS; Xu Zhou et al., in prep.; Zou et al. 2015) is an international cooperative project, which is undertaken by the National Astronomical Observatories of China (Chinese Academy of Sciences) and Steward Observatory (University of Arizona, USA). It is a u-band (effective wavelength \(\sim 3538\) Å) imaging survey programme with the 90-inch (2.3 m) Bok telescope located on Kitt Peak. This survey has imaged \(\sim 5000\) deg\(^2\) in the SGC with 80% of the area overlapped with the southern SDSS data, but 1–1.5 mag deeper than the SDSS u-band photometry. The u-band filter used in the SCUSS project is similar to the SDSS u-band filter but slightly bluer. For our aims, this deep u-band imaging brings valuable improvement with respect to the SDSS u-band photometry, given that the u-band magnitude tightly correlates with the [OII] flux (Comparat et al. 2015b) and that the typical ELGs at 0.6 \(\leq z_{\text{spec}} \leq 1\) are too faint to have a robust measurement in the SDSS u-band.

For SCUSS we also use a forced model photometry on SDSS objects (Zou et al. 2015). This photometry constructs 2D models (de Vaucouleurs and exponential) based on SDSS r-band galaxy profiles and star-galaxy separation, and estimates object fluxes through comparing the models with the object images of SCUSS. The model magnitudes in SCUSS is derived from the object flux with higher likelihood in the de Vaucouleurs and exponential model fitting.

**CFHTLS degraded to DECaLS.** We also test a scheme where the SDSS z-band is replaced by the DECaLS z-band. The DECam Legacy Survey\(^5\) (DECaLS) will conduct a three-band imaging survey of the SDSS extragalactic footprint. The Dark Energy Camera (DECam) will be used to image the 6700 deg\(^2\) footprint overlapping SDSS in the region \(-10 < \text{Dec [deg]} < 30\), to depths of \(g = 24.7\) mag, \(r = 23.9\) mag, and \(z = 23.0\) mag. The survey will be conducted from 2014 through 2017, with periodic data releases beginning in March 2015. As of January 2015, \(>1000\) deg\(^2\) have already been observed in the SGC in the z-band to a depth of \(z = 22.7\) mag (whereas the g- and r-band observations have a significant lower coverage). To simulate the DECaLS photometry, which is not public yet, we degrade the CFHTLS-Wide \(^{6}\) (Gwyn 2012) z-band photometry to the depth of the DECaLS z-band photometry by adding random Gaussian noise. For both surveys we do a linear fit to the data: \(\log_{10}(em) = zp + s \times m\), where \(m\) is the magnitude and \(em\) the magnitude error. Then, if an object has \(m_{\text{CFHTLS}} = m_o\), we degrade it to \(m_{\text{DECaLS}} = m_o + r \times \sqrt{10^{\log_{10}(em_{\text{CFHTLS}} - 10^{zp + s \times m_{\text{CFHTLS}}})} - 10^{zp + s \times m_{\text{CFHTLS}}}}\), where \(r\) is randomly drawn from a Gaussian distribution centred on 0 with a width of 1 and associate to this object a magnitude error of \(10^{zp + s \times m_{\text{CFHTLS}} + r \times \sqrt{\log_{10}(em_{\text{CFHTLS}} - 10^{zp + s \times m_{\text{CFHTLS}}})}}\). We note that we did not model the

\(^5\) http://portal.nersc.gov/decals/

\(^6\) http://terapix.iap.fr/cplt/TO007/doc/TO007-doc.html
scatter in the magnitude error, since this feature has no influence on our selection process.

In addition to the DECaLS, the DES – started in Autumn 2013 – also uses the DECam instrument to image 5000 deg$^2$ in the grizY-bands to about two magnitudes deeper than the DECaLS. Therefore, the DES $z$-band photometry for the −500 deg$^2$ overlapping region between the SDSS and DES could also be considered.

### 3.2. Fisher training sample

For each selection scheme, we need to define the Fisher discriminant quantity $X_{\text{Fisher}}$, i.e. the linear combination combination. This is done through the use of a spectroscopic training sample, for which the used photometry and the quantity used to define the classes, the spectroscopic redshift $z_{\text{spec}}$ (and eventually the total [OII] flux $f_{\text{OII}}$), are known. As explained in Sect. 2.2, our approach is to use a large, composite sample of galaxies, in order to cover the loci as much as possible in the colour space occupied by the different type of galaxies at all redshifts. We list below the surveys we use to define our Fisher training sample.

**VIPERS.** The VIMOS Extragalactic Redshift Survey (VIPERS, Guzzo et al. 2014) is an on-going large programme that builds a spectroscopic sample of $10^5$ galaxies with $15 < i < 22.5$ and $0.5 < z_{\text{spec}} < 1.5$ over a total area of $24\ deg^2$ within the CFHTLS-Wide W1 and W4 fields. The observations are done with the VIMOS instrument (Le Fèvre et al. 2003) with the LR-RED grism (wavelength coverage: $\sim 5500–9500$ Å; spectral resolution: $R \sim 250$; 0.75 h exposure time). The low-redshift ($z_{\text{spec}} < 0.5$) galaxies are efficiently removed from the target section through a colour cut, resulting in a completeness $>95\%$ in the $0.6 < z_{\text{spec}} < 1.2$ range (Guzzo et al. 2014). This sample is crucial for our study, because it covers our targeted redshift range and is flux-selected with an $i$-band flux fainter than the SDSS $i$-band depth. Among the 57 204 spectra of the First Data Release (Garilli et al. 2014; Franzetti et al. 2014), we restricted ourselves to those that have a secure redshift flag (2 ≤ $\text{Flag} < 5$) and that are detected in the SDSS.

Other public surveys. In our Fisher training sample, we include SDSS galaxies belonging to the following public surveys: the F02 and F22 fields of the VIMOS VLT Deep Survey (VVDS, Le Fèvre et al. 2005, 2013; VIMOS LR-RED grism: $\sim 5500–9500$ Å; $R \sim 250$; 0.75 h and 4.5 h), the zCOSMOS 10k-Bright Spectroscopic Sample (Lilly et al. 2009; VIMOS MR grism: $5500–9650$ Å; $R \sim 600$; 1 h exposure time), and the EGS field of DEEP2 (Newman et al. 2013; DEIMOS spectrograph: 6500–9300 Å; $R \sim 5900$; 1 h exposure time). We consider only objects having reliable spectroscopic redshifts. These surveys, including VIPERS, are magnitude-limited, with a magnitude limit fainter than the SDSS depth (VVDS/F02: 17.5 < $i$ < 24, VVDS/F22: 17.5 < $i$ < 22.5, zCOSMOS/Bright: $i < 22.5$, DEEP2/EGS: $R < 24.1$), so that they include all possible types of galaxies detected in the SDSS (lying in the observed sky region). We also add all the SDSS DR12 public spectroscopic redshifts (DR12, Alam et al. 2015; SDSS and BOSS spectrographs: 3800–9200 Å and 3650–10400 Å; $R \sim 1500$–2500; 0.75–1 h exposure time) covering those survey regions.

**Comparat et al. (2015b) ELGs.** Futhermore, we enlarge our Fisher training sample by adding $\sim 10^6$ ELGs observed as pilot programmes for eBOSS and DESI (Paper I).

**Total [OII] flux.** In addition, we extracted the total [OII] fluxes for the VIPERS, VVDS, and BOSS/eBOSS surveys in a consistent way from the spectra $f_{\text{OII}}$ (see Paper I for details).

### 3.3. Spectroscopic verification sample

We tested the efficiency of our ELG Fisher selection algorithms in a 8.82 deg$^2$ area centred approximately at (RA, Dec) $\sim (36.0, -4.8)$ (see bottom panel of Fig. 2), thus using a verification sample that is independent of our training sample ($\sim 6\%$ overlap). This part of the sky has been extensively observed in 2014 with ten eBOSS/ELG test plates (eboss6: plates 8123–8130; eboss7: plates 8355, 8356), with 4 × 15 min exposures using the BOSS spectrograph (3650–10400 Å; $R \sim 1500$–2500). The eboss7 plates have been specifically dedicated to two of our tested photometric Fisher discriminant selections (Fisher_UGRIZW1 and Fisher_GRIW1, see Sect. 5), which thus have a spectroscopic coverage of the target selection of $\sim 93\%$, the remaining $\sim 7\%$ having not been targeted for tiling reasons. The observations and their reduction are described in Paper I, to which we refer the reader. In short, the observations were done with the BOSS spectrograph (Smee et al. 2013) of the 2.5 m telescope located at Apache Point Observatory (New Mexico, USA), using 2" diameter fibers and an exposure time of $\sim 1$ h. The reduction provides various information, with a confidence flag based on the continuum ($z$Cont) and emission lines ($zQ$). The $z$Cont flag quantifies the degree to which the continuum is detected, and the $zQ$ flag quantifies the number of detected emission lines, along with the signal-to-noise ratio ($S/N$) thereof. We refer to Paper I for further details on the definition of $z$Cont and $zQ$. We have restricted this study to galaxies having a secure confidence flag; that is,

- $zQ \geq 1.5$ (2a)
- or ($zQ = 1$ and $z$Cont $\geq 0.5$) (2b)
- or ($zQ = 0$ and $z$Cont $\geq 1.0$), (2c)

meaning that the galaxy has either unobserved emission features – one line at $S/N \geq 5$ or two or more lines at $S/N \geq 3$ (Eq. (2a)) – or a trustable combination of a detection of emission features and of the continuum: one line at $S/N \geq 3$ and a continuum detected at $S/N \geq 8$ with at least three emission lines (Eq. (2b)) or a continuum detected at $S/N \geq 10$ with at least three emission lines (Eq. (2c)). We illustrate in Fig. 3 those flags with three eboss6-7 spectra. The expected catastrophic $z_{\text{spec}}$ estimate rate, estimated through the visual inspection of more than 10 000 BOSS spectra, can be estimated for each $z$Cont, $zQ$. We note that in the 0.6 ≤ $z \leq 1.0$ range, the galaxies selected with Eqs. (2a), (2c) have, on average, lower precision in the $z_{\text{spec}}$ estimate (median value of $z_{\text{spec,est}}/(1+z_{\text{spec}})$ of 1.5–1.7×10$^{-4}$ vs. 0.5×10$^{-4}$) and a slightly higher catastrophic $z_{\text{spec}}$ estimate rate when compared to the galaxies selected with Eq. (2a).

The eboss6-7 data make it possible an unbiased and complete analysis for two of our tested selections (Fisher_UGRIZW1 and Fisher_GRIW1). For the remaining tested selections, those eboss6-7 data represent a biased and incomplete subsample of the selections, so they cannot be used to reliably infer the selection properties. To overcome this, we duplicate the analysis using complementary data for all the selections: the CFHTLS-Wide photometric redshifts for the redshift, and the VIPERS total [OII] fluxes for the [OII] diagnosis. The CFHTLS-Wide photometric redshifts (T0007 release; Ilbert et al. 2006; Coupon et al. 2009) are of very good quality up to $i < 22.5$ (bias below 1%, scatter of $\sim 0.04$, and less than 4% outliers). Using the eboss6-7 test plates, we demonstrate the reliability of those photometric redshifts for ELGs up to redshift $\sim 1$ in

1 http://terapix.iap.fr/rubrique.php?id_rubrique=267
Appendix A. As explained in the previous section, the VIPERS sample is magnitude-complete down to $i = 22.5$ mag in the redshift range $0.6 \leq z_{\text{spec}} \leq 1.2$.

Objects with a signal-to-noise ratio ($S/N$) of 3 in the [O\text{II}] flux measurements have on average $f_{\text{[O\text{II}]}_{\text{tot}}} \sim 10^{-16.6}$ erg s$^{-1}$ cm$^{-2}$ in the VIPERS observations and $f_{\text{[O\text{II}]}_{\text{tot}}} \sim 10^{-16.4}$ erg s$^{-1}$ cm$^{-2}$ in the eboss6-7 observations.

4. Improvement with using the WISE/W1 data

The WISE/W1 near-infrared data bring crucial information for identifying the galaxy redshift, and the combination with other colours permits isolating $0.6 \leq z_{\text{spec}} \leq 1.0$ ELGs. We illustrate this point with the $r - W1$ vs. $g - r$ diagram in Fig. 4, using both model predictions and data.

In the left-hand panel, we plot the tracks predicted by the Bruzual & Charlot (2003) stellar population models with standard settings ($\zeta_{\text{form}} = 3$, solar metallicity) for four different exponentially declining star formation histories (SFH $\tau = 0.05, 1, 5, 10$ Gyr) with no dust. Models with SFH $\tau = 5, 10$ Gyr are representative of ELGs, while models with SFH $\tau = 0.05, 1$ Gyr are representative of LRGs. Besides, it is known that galaxies at $0.6 \leq z_{\text{spec}} \leq 1.0$ with star formation can be dusty. We represent the effect of a $E(B - V) = 0.2$ reddening using the Calzetti et al. (2000) law, and this value corresponds to the median value for $0.6 \leq z \leq 1.0$ star-forming galaxies with $i < 22.5$ mag in the COSMOS catalogue (Ilbert et al. 2009). To guide the eye, we shade the approximate locus where $0.6 \leq z_{\text{spec}} \leq 1.0$ ELGs are expected to lie according to those models.

The assumptions made to compute the models (formation redshift, metallicity, SFH, dust) are simple and generic: to verify that the model predictions agree with observed galaxy properties, we look at the same colour–diagram, but with observed data. We plot the loci of the SDSS objects belonging to complete spectroscopic surveys (see Sect. 3.2) with $i < 22.5$ mag. In the middle panel, we gather the VVDS/F22 galaxies in bins of spectroscopic redshift: the colour evolution with the redshift agrees with the model predictions, with $0.6 \leq z_{\text{spec}} \leq 1.0$ galaxies lying at $1 \leq r - W1 \leq 3$ and spanning a wide range of $g - r$ colours. Then we plot in the right-hand panel the $0.6 \leq z_{\text{spec}} \leq 1$ VIPERS galaxies binned by [O\text{II}] luminosity. Again, the data and the model predictions agree, with $0.6 \leq z_{\text{spec}} \leq 1.0$ ELGs having blue $g - r \leq 1$ colours.

Thus, we see that the $0.6 \leq z_{\text{spec}} \leq 1.0$ ELGs can be isolated using colours that include the WISE/W1 data. The $z_{\text{spec}} < 0.6$ galaxies should lie in a different locus at bluer $r - W1$ colours; stars are also expected to minimally contaminate the ELG selection (Fig. 4, middle panel). The $z_{\text{spec}} > 1$ galaxies lie at a locus overlapping the blue-shadowed area; however, we note that our requirement that the eBOSS/ELG galaxies are detected in the SDSS significantly reduces the contamination from them, because the SDSS is too shallow to detect a large number of $z_{\text{spec}} > 1$ galaxies.

5. ELG selection with Fisher discriminant

We present in this section different target selections to account for different possible strategies. The eBOSS/ELG observations are planned to be done in the SGC and to begin in autumn 2016. A key point is the availability of the photometric data ahead of observations. The SDSS, SCUSS, and WISE data are already available, while the DECaLS data are in the process of acquisition and reduction. A first possibility is to make use of the maximum photometric information available today on the SGC, i.e. to combine the SDSS, SCUSS, and WISE data. A second possibility is to minimise the number of combined surveys, i.e. combining the SDSS and WISE data, to minimise possible systematics. A last possibility is to take advantage of the near availability of the DECam/$z$ data, which will be two magnitudes deeper than the SDSS/$z$ data. Indeed, the DECaLS/$z$-band imaging already covers more than 1000 deg$^2$ over the SGC and should be made public through annual releases starting in March 2015, and the DES/$z$-band data over the “fat”-Stripe-82 region should be made public in 2015.

We first present in this section the tested ELG selection algorithms, which were built on the Fisher discriminant (Sect. 5.2). We present in Sect. 5.3 selections based on colour–colour cuts. The aim is two-fold: (1) we present the initially tested selection using $ugri$-bands to illustrate the improvement due to the addition of the WISE/W1-band; (2) the colour–colour cuts using WISE/W1 allow the comparison of the Fisher selections with classical methods. We then analyse the selection’s redshift and [O\text{II}] emission properties, along with their efficiencies (Sect. 5.4). This analysis is presented in two complementary manners to overcome the fact that the eboss6-7 test plates cover a biased subsample of some selections. In fact, the eboss6-7 test plates were designed to sample some selections, amongst which the Fisher_UGRIZW1, Fisher_GRIW1, and CC_UGRI selections (defined in Sects. 5.2 and 5.3). Those three selections thus have a $\sim 95\%$ coverage with eboss6-7, since the remaining $\sim 5\%$ were not targeted for tiling reasons and are thus an unbiased subsample. However, none of the ten eboss6-7 test plates have been specifically designed for the other tested selections: even if up to $\sim 90\%$ of a selection is observed with eboss6-7, the unobserved $\sim 10\%$ is a biased subsample, thus preventing reliable statistics to be computed. For the
redshift, we present results for eboss6–7 spectroscopic redshifts (Fisher_UGRIZW1, Fisher_GRIW1, and CC_UGRI selections) and for photometric redshifts (all selections). For the [OII] properties, we present results for the eboss6–7 test plates (Fisher_UGRIZW1, Fisher_GRIW1, and CC_UGRI) and for the VIPERS objects (all selections). Lastly, we present a brief illustration of the flexibility in terms of target density of our approach (Sect. 5.5).

5.1. Why use a Fisher discriminant approach?

The initially tested selection based on an SDSS-detection for eBOSS/ELG uses cuts in the $u$ri and g$ri$ colour–colour diagrams. This selection, which we label CC_UGRI (“CC” for colour–colour), is explained in Paper I and has been tested with the eboss6 observations. Our analysis deals with the five $ugriz$ optical bands and the WISE/W1 near-infrared band, hence five independent colours. Though it is possible to define boxes in some colour–colour diagrams using those five colours, this task is complex and subjective, and this motivated us to use this alternative Fisher discriminant approach, which automatically defines the cut in the full colour–colour space. The only requirement is the availability of a training sample, which we have in hand thanks to the numerous spectroscopic data covering the SDSS footprint (see Sect. 3.2).

We thus present below the tested Fisher selections, and to compare their performance with classical colour–colour cuts, we also present two colour–colour cuts using the WISE/W1-band. In addition, we present the CC_UGRI selection performance to illustrate the improvement due to the addition of the WISE/W1-band.

5.2. Fisher selection schemes

The strength of this Fisher selection scheme is its simplicity: our selections are solely based on the Fisher discriminant quantity ($X_{FL_{\text{min}}} < X_{F1}$) and on cuts in magnitudes and magnitude errors. $X_{FL_{\text{min}}}$ is tuned so that the selection has the desired object density. The tested selection schemes (including the Fisher discriminant definition) are described in Table 2.

As explained in Sect. 2.2, there are two possible approaches to defining the Signal1 and Background classes for the Fisher discriminant training. The first possible approach is to use criteria on both spectroscopic redshift $z_{\text{spec}}$ and the total [OII] flux:

- **Signal 1**: $0.6 < z_{\text{spec}} < 1.2$ and $f_{\text{tot}}(\text{OII}) > 10^{-16}$ erg s$^{-1}$ cm$^{-2}$
- **Background**: $z_{\text{spec}} < 0.5$.

With this, we account for the possibility that in our training sample, we miss some [OII] line measurement due to sky lines at $z_{\text{spec}} > 0.9$, while keeping objects at $0.9 < z_{\text{spec}} < 1.2$ in our Signal1 class with significant flux in the g-band, since it is correlated with the [OII] flux (see Comparat et al. 2015b). Because we are working with objects detected in the SDSS, the vast majority of the galaxies we want to exclude will be at low redshift, so we only include those in our Background class (regardless of the [OII] flux). The second possible approach is to define our Signal class using only the $z_{\text{spec}}$ quantity:

- **Signal 2**: $0.75 < z_{\text{spec}} < 1.3$
- **Background**: $z_{\text{spec}} < 0.5$.

We tested five selections, based on three different survey combinations:

- Fisher_UGRIZW1: SCUSS/u + SDSS/griz + WISE/W1;
- Fisher_GRIW1: SDSS/griz + WISE/W1;
- Fisher_GRIW1[OII]: SDSS/griz + WISE/W1, with a Fisher training using Eq. (3);
- Fisher_GRZW1[OII]: SDSS/griz + CFHTLS-W/c (degraded to the DECaLS depth) + WISE/W1;
- Fisher_GRZW1[OIII]: same as Fisher_GRZW1[OII], but with higher object density.

Except for the Fisher_GRIW1[OII] selection, all the Fisher trainings were done with Eq. (4). Our choice to define the tested selections were guided by the eBOSS/ELG experiment requirements (number of targets, available imaging at the start of spectroscopic observations). On the one hand, the Fisher_UGRIZW1 selection is based on a broad wavelength coverage (from the $u$-band to the W1-band) and is limited to the SGC: as mentioned in Sect. 3.1, the SCUSS deep $u$-band photometry provides us with a measurement of the ultra-violet emission at redshifts $0.6$–$1.0$. On the other hand, the Fisher_GRIW1 selection has a narrower wavelength coverage, but has the advantages of being available on both the SGC and the NGC and of minimising the number
of surveys used. Eventually, the Fisher\textsubscript{GRZW1} selections use a deeper – hence less scattered – $z$-band photometry. We tested two scenarios (target densities of 180 deg$^{-2}$ and 300 deg$^{-2}$) to see to what extent the target density can be increased, in case the available DECaLS $z$-band photometry is available for an area smaller than 1500 deg$^2$.

Figure 5 illustrates how the Fisher correlates with redshift and [O\textsc{ii}] flux. The VIPERS sample, with [O\textsc{ii}] flux measurement in $0.6 \lesssim z_{\text{spec}} \lesssim 1.2$, allows us to see the simultaneous dependence on $z_{\text{spec}}$ and $F_{\text{[O\textsc{ii}]}\text{tot}}$, whereas we use the VVDS/F22 sample to probe the dependence only on $z_{\text{spec}}$, but over a wide redshift range ($0 \lesssim z_{\text{spec}} < 1.2$). We recall that the data plotted here are the subsamples of the VIPERS and VVDS/F22 detected in the SDSS and that, due to the SDSS depth, the number of galaxies per redshift bin decreases for $z_{\text{spec}} \gtrsim 0.6$. The Fisher\textsubscript{UGRIZW1} quantity correlates with both redshift and [O\textsc{ii}] flux, which means that selecting objects with high values of Fisher\textsubscript{UGRIZW1} should be efficient in selecting ELGs in $0.6 \lesssim z \lesssim 1.0$. We note that the Fisher training here is done on $z_{\text{spec}}$ only (Eq. (4)): the efficiency in selecting [O\textsc{ii}] emitters is a byproduct of the present of the deep SCUSS $u$-band. Indeed, the faint magnitude cut on the SCUSS photometry favours $z \sim 0.8$ star-forming galaxies against $z \sim 0.8$ passive galaxies, which have faint emission in the $u$-band (see for instance Comparat et al. 2015b). In contrast, we observe that, though having a strong correlation with redshift by training, the Fisher\textsubscript{GRIW1} is inefficient at distinguishing [O\textsc{ii}] emitters. Adding [O\textsc{ii}] in the training (Fisher\textsubscript{GRIW1}\textsubscript{\textsc{lit}}, trained with Eq.(3)) improves the efficiency in selecting [O\textsc{ii}] emitters, but at the cost of slightly reducing the correlation with redshift. Lastly, the Fisher\textsubscript{GRZW1} efficiently distinguishes the redshift, but favours low [O\textsc{ii}] emitters at $z_{\text{spec}} \sim 1$.

Before applying the cut on the Fisher discriminant, we apply cuts on the magnitudes and their errors (see Table 2). The aim is twofold: the cut on the bright magnitudes removes objects that surely are at low redshift ($z \lesssim 0.6$) from the samples. The cut on the faint magnitudes and on the magnitude errors ensures that we

<table>
<thead>
<tr>
<th>Table 2. Criteria used to define our Fisher selections.</th>
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<tbody>
<tr>
<td><strong>Fisher\textsubscript{UGRIZW1}</strong></td>
</tr>
<tr>
<td><strong>Photometry</strong></td>
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<td></td>
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<td></td>
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<tr>
<td><strong>$X_1$ training</strong></td>
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<td></td>
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<tr>
<td><strong>Other cuts</strong></td>
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</table>

**Notes.** For the Fisher\textsubscript{GRZW1} selection, the $^{(1)}$ denotes quantities related to the deep (300 objects per deg$^2$) selection.
use reasonable photometry and mitigates inhomogeneous spatial distribution. We note that the Fisher discriminant’s dependence on redshift and [OII] flux illustrated in Fig. 5 does not change when those cuts are applied, though the sample is significantly smaller.

We also apply the following cuts: 1) we reject potential stars; 2) we reject objects lying in regions where the photometry is uncertain; 3) we reject objects with BINNED2 ≠ 0. To reject potential stars, we reject objects with OBJC_TYPE ≠ 3 and r < 22, where OBJC_TYPE is the SDSS star/galaxy separator. Regarding the regions where the photometry is uncertain, we use the SDSS masks (bright_star, bad_field, bright_object_rykoff) and a custom mask for the W1 bright-object neighbourhood. In fact, as explained in Lang et al. (2014, see their Fig. 10), SDSS objects falling in W1 halo outskirts are not masked and have a significantly overestimated W1 flux – so are very red in r-W1.

To build our custom W1 mask, we detect spatial 5σ overdensities of SDSS r < 22.5 mag objects with 3 mag < r − W1 < 5 mag and mask objects within a radius of 0.4° around those overdensities. Our custom W1 mask includes ~200 overdensities in the SGC (and ~350 in the NGC). We note that the masking is independent of any ELG selection. We also notice that, though the CFHTLS masking is independent of any ELG selection. We also notice that, though the CFHTLS/W1 region used in this study does not include bright W1 objects, such a W1 mask is nevertheless required when using our selections over larger regions, as for instance in Paper III, where the homogeneity and systematics analysis of our selections over the SGC is done. Eventually we only keep objects with BINNED2 = 0, because this (slightly) reduces the number of objects with unexploitable spectra. (BINNED2 is one of the SDSS photometric flags.)

5.3. Colour–colour cut selections

We also present some selections using colour–colour cuts in the following analysis. First, we present the CC_UGR selection, which uses cuts in the u and gri colour–colour diagrams. This selection is detailed in Paper I and has been tested with the eboss6 observations. It allows the improvement in the selection to be quantified thanks to the addition of the WISE/W1-band.

Additionally, we present two selections based on colour–colour cuts using the ugriz,W1-bandset and the gri,W1-bandset, which we label CC_UGRIZW1 and CC_GRIW1. Those allow a comparison of the Fisher discriminant selection performances with classical colour–colour cuts. The CC_UGRIZW1 selection has cuts similar to the Fisher_UGRIZW1 (see Table 2) selection except the cut on the Fisher discriminant, which is replaced by

\[ g - r > 2.0 \times (u - r) - 3.00, \]
\[ g - r < 1.2 \times (r - i), \]
\[ i - z > -2.4 \times (r - i) + 0.60, \text{ and} \]
\[ r - W1 > 2.0 \times (g - r) + 0.35. \]

Figure 6 represents the Fisher_UGRIZW1 and Fisher_GRIW1 selections on zspec and F_{[OII]}^{tot} for our observed eboss6–7 plates. The dot size scales with the number of objects entering the bin. For each redshift bin (using z_{phot}), we colour-coded at \( \log_{10}(F_{[OII]}^{tot}) = -17.8 \) the ratio of the number of selected photometric objects to the number of photometric objects passing all the cuts in Table 2 except the cut on the Fisher discriminant. The horizontal dashed line represents the approximate \( F_{[OII]}^{tot} \) of objects with \( S/N = 3 \).

The CC_GRIW1 selection has cuts similar to the Fisher_GRIW1 (see Table 2) selection except the cut on the Fisher discriminant, which is replaced by

\[ g - r < 1.0, \]
\[ r - i > 0.5, \text{ and} \]
\[ r - W1 > 2.5 \times (g - r) + 0.25. \]

5.4. Selection properties

We recall that the redshift requirements for a 180 deg−2 eBOSS/ELG target selection are (1) an efficiency of 70% in the 0.6 ≤ z ≤ 1.0 range (i.e. at least 70% of the targets have a measurable z_{spec} with 0.6 ≤ z ≤ 1.0); (2) a redshift failure rate ≤1% in 0.6 ≤ z ≤ 1.0.

Figure 6 represents the Fisher_UGRIZW1 and Fisher_GRIW1 selections in the [OII] flux versus redshift diagram using our eboss6–7 test plates measurements. For each redshift bin (using z_{phot}), we colour-code at \( \log_{10}(F_{[OII]}^{tot}) = -17.8 \) the ratio of the number of selected photometric objects to the number of photometric objects passing all the cuts in Table 2, except the cut on the Fisher discriminant. We do not display the Fisher_GRIW1 and Fisher_GRIW1 selections because their eboss6–7 observations are biased. As expected from the preliminary analysis of Fig. 5, the two Fisher selections are efficient in selecting 0.6 ≤ z ≤ 1.0 galaxies with a significant [OII] flux. More precisely, we see that the cut on the Fisher discriminant is very efficient in rejecting z_{spec} < 0.6 objects, as it rejects >99% of those.

We now study the magnitude and colours distributions for our tested selections, then the redshift distributions and the [OII] emission; we finally present the overall statistics for all the tested selections.

5.4.1. Magnitudes and colours

Figure 7 summarises the magnitude and colour distributions of the Fisher selections, along with the percentage of selected objects.
objects with \(0.6 \leq z_{\text{phot}} \leq 1.0\). Overall, the five Fisher selections have broadly similar magnitude distributions, except for the \(u\)-band and the DECaLS/\(z\)-band, where we apply different magnitude cuts. When compared to the four other Fisher selections, the Fisher_UGRIZW1 selection almost has no objects with red \(u - r > 2\) colours, which are likely to be more passive galaxies. One reason for that is the presence of an upper \(u\)-band magnitude limit in the selection criteria, which requires a minimum flux in the \(u\)-band. For all colours, the Fisher_GRIZW1 selection has a distribution that is bluer than the Fisher_GRIW1 selection one, confirming the link between blue colours and \([\text{OII}]\) emission. When compared to the Fisher_GRIZW1 selection, the Fisher_GRIZW1 selection shows small differences; for instance, it has slightly redder \(g - r\) colours and slightly bluer \(r - W1\) colours, consistent with a lower redshift (see Fig. 4). Additionally, all our Fisher selections show common trends in the percentage of selected objects with \(0.6 \leq z_{\text{phot}} \leq 1.0\). For instance, the selected objects with faint \(u\) or \(g\) magnitudes are, for the large majority, in our desired redshift range; however, the depth of the images and the requirement to obtain an usable spectrum with a 1h observation prevent us from pushing the selection at fainter magnitudes.

In Sect. 4, we studied the location of the \(0.6 \leq z_{\text{phot}} \leq 1.0\) ELGs in the \(r - W1\) vs. \(g - r\) colour–colour diagram. We look in Fig. 8 at the same diagram for our tested Fisher selections; overall, the selected galaxies are indeed located in the expected region. We can see some small differences in the loci occupied by the different selections. For instance, the approximate cut in this diagram has a steeper slope for the Fisher_UGRIZW1 and Fisher_GRIZW1 selection than for the Fisher_GRIW1 and Fisher_GRIZW1 selection, and this steeper slope implies the selection of more galaxies at \((g - r, r - W1) \sim (0, 1)\) that have higher redshift and are strongly star-forming, while the flatter slope implies the selection of more galaxies at \((g - r, r - W1) \sim (1, 2)\), with less star formation.

### 5.4.2. Redshift

We now study the redshift distributions for the Fisher and colour–colour selections. The top panel of the Fig. 9 represents the \(z_{\text{spec}}\) distribution from eboss6−7 observations for the three selections that have unbiased sampling. The middle (bottom, respectively) panel represents the CFHTLS/\(z_{\text{phot}}\) distribution for the Fisher selections (colour–colour selections, respectively). We observe that the eboss6−7 \(z_{\text{spec}}\) distributions for the Fisher_UGRIZW1 and Fisher_GRIW1 selections are close, i.e. peaked between \(0.6 \leq z_{\text{phot}} \leq 1.0\) with little contamination from \(z_{\text{spec}} < 0.6\) objects. The Fisher_UGRIZW1 selection has a slightly higher median \(z_{\text{spec}}\) than the Fisher_GRIW1 selection. The CC_UGRIZW1 selection has a distribution that is slightly shifted to lower redshifts with more contamination from \(z_{\text{spec}} < 0.6\) objects.

We verify in the middle and bottom panels that the \(z_{\text{phot}}\) distributions faithfully mimic the \(z_{\text{spec}}\) distributions for the
Fig. 9. Redshift distributions for the five Fisher and the CC_UGRI selections. The median redshift value is indicated by an arrow on the top x-axis. Top panel: eboss6-7 $z_{\text{spec}}$. Middle panel: CFHTLS $z_{\text{phot}}$ for the Fisher selections. Bottom panel: CFHTLS $z_{\text{phot}}$ for the colour–colour selections. We report the Fisher_UGRIZW1 selection to facilitate the comparison.

Three selections of the top panel, though with a slight shift towards higher values of redshift at $\sim 1$, as expected from Appendix A. Furthermore, we see that the Fisher_GRIW1$^{0.1}$ selection has more contamination from $z_{\text{phot}} < 0.6$ objects than the Fisher_GRIW1 selection. The Fisher_GRZW1$_{180}$ selection has slightly more galaxies at $z > 1$, while the Fisher_GRZW1$_{300}$ selection has a distribution peaking at a lower redshift and has more $z_{\text{phot}} < 0.6$ contamination than the Fisher_GRZW1$_{180}$ selection.

The colour–colour selections including the W1-band have $z_{\text{phot}}$ distributions comparable to the Fisher selections. We see that including the W1-band reduces the contamination from $z_{\text{phot}} < 0.6$ objects.

5.4.3. [OII] flux

In Fig. 10 we display the total [OII] flux distributions, and in Fig. 11 the percentage of objects with $f_{\text{[OII]}} > 10^{-16}$ erg cm$^{-2}$ s$^{-1}$ Å$^{-1}$ as a function of the $g$-band magnitude.
Total fluxes above $10^{-16}$ erg cm$^{-2}$ s$^{-1}$ Å$^{-1}$ are detected at more than 5σ in both the VIPERS and eBOSS. This threshold allows us to directly compare the percentages using the VIPERS and the eBOSS, overcoming the fact the VIPERS spectra have a slightly higher signal-to-noise ratio than the eBOSS spectra.

The Fisher_UGRIZW1 selection emits more [OII] than does the Fisher_GRIW1 selection. This is consistently seen from eboss6-7 and VIPERS data. When looking at the VIPERS data, we see that, as expected from the Fisher training, the Fisher_GRIW1 selection is more [OII]-emitting than the Fisher_GRZW1 selection. The Fisher_GRZW1 selection is intermediate, and the [OII] emission is similar for both tested densities (180 and 300 deg$^{-2}$). The VIPERS data also show that the colour–colour selection has slightly less [OII] emission than the Fisher_UGRIZW1 selection. Noticeably, the CC_UGRI selection is significantly less [OII]-emitting than the other selections.

Finally, we see the trend for all selections and eboss6-7 and VIPERS data towards galaxies that are fainter in the $g$-band to have less [OII] emission on average. This result agrees with those from the Comparat et al. (2015b) study of the [OII] luminosity function.

5.4.4. Statistics and summary

We give details on the properties of our tested Fisher selections in Table 3 and of the colour–colour selections in Table 4. We present the statistics for redshift, [OII] flux, and overall efficiency. More precisely, lines (L1–L6) present information computed with the photometric data over a ~50 deg$^2$ area within the CFHTLS/W1 field (density, overlap with LRGs, photometric redshifts statistics); lines (L7–L8) report the numbers of $0.6 < z_{\text{spec}} < 1.0$ VIPERS galaxies passing the selection, along with the percentage of those having $f_{\text{tot}}^{\text{[OII]}} > 10^{-16}$ erg cm$^{-2}$ s$^{-1}$. Lines (L9–L14) present spectroscopic information for the eboss6-7 plates observations covering an area of 8.82 deg$^2$ (number of galaxies, percentage of observed galaxies, percentage of galaxies with non reliable $z_{\text{spec}}$ measurement, $z_{\text{spec}}$ statistics). Finally, lines (L15–L16) present spectroscopic information for the eboss6-7 galaxies with a reliable $z_{\text{spec}}$ that would be used for a BAO measurement (mean $z_{\text{spec}}$, percentage of galaxies with $f_{\text{tot}}^{\text{[OII]}} > 10^{-16}$ erg cm$^{-2}$ s$^{-1}$, expected percentage of galaxies with catastrophic $z_{\text{spec}}$ estimation). We now summarise the selection properties based on the above analysis of Figs. 6–11 and statistics from Tables 3, 4.

**Fisher_UGRIZW1 selection.** This selection meets the initial eBOSS/ELG target selection redshift criteria. It has an efficiency of 71% and an expected $z_{\text{spec}}$ failure rate of 0.5%. We observe that it has a narrow $z_{\text{spec}}$ distribution with a typical width of 0.12. The $z_{\text{phot}}$ distribution is very similar. The median $z_{\text{spec}}$ of the selection is 0.78. As expected from the preliminary study (Fig. 5), the Fisher_UGRIZW1 selection is efficient in selecting [OII] emitters, and this can be seen in particular in Fig. 11 and also in the lower value of objects with an unreliable $z_{\text{spec}}$ or with the small overlap with LRGs (12% and 2.0 deg$^{-2}$, respectively; see Table 3).

**Fisher_GRIW1 and Fisher_GRIW1OII selections.** The Fisher_GRIW1 selection also meets the initial eBOSS/ELG target selection redshift criteria, the efficiency and expected $z_{\text{spec}}$ failure rate in $0.6 < z_{\text{spec}} < 1.0$ being close to the requirements (71% and 0.9%, respectively). The shape of the redshift distribution is close to the one of the Fisher_UGRIZW1 selection, but shifted to a slightly lower value (0.76 vs. 0.78 for $z_{\text{spec}}$). The Fisher_GRIW1 selection is also a little more efficient at removing low-redshift objects, as expected from Fig. 5, where we see a strong correlation between $z_{\text{spec}}$ and the Fisher discriminant. These features are also visible in the $z_{\text{phot}}$ distribution. An important characteristic of the Fisher_GRIW1 selection is that it tends to select fewer [OII] emitters than the Fisher_UGRIZW1 selection. Figure 11 consistently supports...
this observation, using both the eBOSS and the VIPERS measurements; in addition, this can also be seen in Table 3, where the number of LRGs per square degree is almost twice higher than for the Fisher_UGRIZW1 selection, or in Fig. 7, where the selected objects have redder $u-r$ colours. The Fisher_0I selection succeeds to select more [OII] emitters (middle panels of Figs. 10 and 11), and overlap with LRs in Table 3), but at the cost of being less efficient at removing low-redshift objects (middle panel of Fig. 9). For example, it can be seen in Figs. 7 and 8 that the Fisher_0I selection has colours bluer than in the Fisher_0I selection. Unfortunately, even if we probe 89% of the Fisher_0I selection with the eboss6–7 test plates, we cannot infer robust statistics with them because ~5% of the untargeted objects are a biased subsample. Typically, low-redshift objects belonging to the Fisher_0I selection but not to the Fisher_UGRIZW1 and Fisher_0I selections will not be targeted.

**Table 3. Summary of the Fisher selection properties.**

<table>
<thead>
<tr>
<th>Photometric data (−50 deg²)</th>
<th>Fisher_UGRIZW1</th>
<th>Fisher_GRIW1</th>
<th>Fisher_GRIW1OI</th>
<th>Fisher_GRZW1180</th>
<th>Fisher_GRZW1300</th>
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</thead>
<tbody>
<tr>
<td>(L1) Density (deg⁻²)</td>
<td>180</td>
<td>182</td>
<td>181</td>
<td>183</td>
<td>301</td>
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<tr>
<td>(L2) eBOSS/LRG overlap (deg⁻²)</td>
<td>2.0</td>
<td>3.5</td>
<td>2.4</td>
<td>2.7</td>
<td>3.4</td>
</tr>
<tr>
<td>(L3) median(peak width)</td>
<td>0.78</td>
<td>0.77</td>
<td>0.78</td>
<td>0.78</td>
<td>0.74</td>
</tr>
<tr>
<td>(L4) [OII] peak width</td>
<td>0.12</td>
<td>0.13</td>
<td>0.12</td>
<td>0.13</td>
<td>0.14</td>
</tr>
<tr>
<td>(L5) % with $0.6 \leq \zspec \leq 1.0$</td>
<td>79%</td>
<td>80%</td>
<td>75%</td>
<td>73%</td>
<td>71%</td>
</tr>
<tr>
<td>(L6) mean(peak width)</td>
<td>0.79</td>
<td>0.78</td>
<td>0.79</td>
<td>0.79</td>
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**VIPERS (0.6 \leq \zspec \leq 1.0)**

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<thead>
<tr>
<th>Plates eboss6–7 (8.82 deg²)</th>
<th>Fisher_UGRIZW1</th>
<th>Fisher_GRIW1</th>
<th>Fisher_GRIW1OI</th>
<th>Fisher_GRZW1180</th>
<th>Fisher_GRZW1300</th>
</tr>
</thead>
<tbody>
<tr>
<td>(L7) N selected galaxies</td>
<td>555</td>
<td>552</td>
<td>512</td>
<td>513</td>
<td>874</td>
</tr>
<tr>
<td>(L8) $f_{\text{tot}}^{\text{phot}} &gt; 10^{45}$ erg cm⁻² s⁻²</td>
<td>78%</td>
<td>69%</td>
<td>76%</td>
<td>74%</td>
<td>75%</td>
</tr>
</tbody>
</table>

**Plates eboss6–7.**

<table>
<thead>
<tr>
<th>Plates eboss6–7.</th>
<th>Fisher_UGRIZW1</th>
<th>Fisher_GRIW1</th>
<th>Fisher_GRIW1OI</th>
<th>Fisher_GRZW1180</th>
<th>Fisher_GRZW1300</th>
</tr>
</thead>
<tbody>
<tr>
<td>(L15) Mean($z_{\text{spec}}$)</td>
<td>0.79</td>
<td>0.77</td>
<td>(0.79)</td>
<td>(0.78)</td>
<td>(0.77)</td>
</tr>
<tr>
<td>(L16) $f_{\text{tot}}^{\text{phot}} &gt; 10^{45}$ erg cm⁻² s⁻²</td>
<td>85%</td>
<td>81%</td>
<td>(84%)</td>
<td>(81%)</td>
<td>(82%)</td>
</tr>
<tr>
<td>(L17) Expected $z_{\text{spec}}$ failure</td>
<td>0.5%</td>
<td>0.9%</td>
<td>(0.7%)</td>
<td>(0.8%)</td>
<td>(0.8%)</td>
</tr>
</tbody>
</table>

**Notes.** Lines (L1–L6): information computed with the photometric data over a ~50 deg² area within the CFHTLS/W1 field (density, overlap with LRs identified using the cuts defined in Prakash et al. (2015), photometric redshifts statistics). Lines (L7–L8): number of 0.6 \leq \zspec \leq 1.0 VIPERS galaxies passing the selection, and percentage of those having $f_{\text{tot}}^{\text{phot}} > 10^{45}$ erg cm⁻² s⁻². Lines (L9–L14): spectroscopic information for the eboss6–7 plates observing a area of 8.82 deg² (number of galaxies, percentage of observed galaxies, percentage of galaxies with unreliable $z_{\text{spec}}$ measurement, $z_{\text{spec}}$ statistics). Lines (L15–L16) present spectroscopic information for the eboss6–7 plates with a reliable $z_{\text{spec}}$ measurement with 0.6 \leq \zspec \leq 1.0 (mean $z_{\text{spec}}$, percentage of galaxies with $f_{\text{tot}}^{\text{phot}} > 10^{45}$ erg cm⁻² s⁻², expected percentage of galaxies with catastrophic $z_{\text{spec}}$ estimation). For lines (L10–L16), we report in brackets the quantities derived from our spectroscopic observations for the Fisher_GRIW1OI and Fisher_GRZW1 selections; those quantities are biased because they are obtained from a non-random subsample constituted of objects passing the Fisher_UGRIZW1 or Fisher_GRIW1 selections. (1) The width is estimated through the fitting of Gaussian.
Table 4. Summary of the colour–colour selections properties.

<table>
<thead>
<tr>
<th>Photometric data (-50 deg2)</th>
<th>CC_UGRI</th>
<th>CC_UGRIZW1</th>
<th>CC_GRIW1</th>
</tr>
</thead>
<tbody>
<tr>
<td>(L1) Density (deg⁻²)</td>
<td>183</td>
<td>179</td>
<td>183</td>
</tr>
<tr>
<td>(L2) eBOSS/ELG overlap (deg⁻²)</td>
<td>2.4</td>
<td>1.8</td>
<td>2.6</td>
</tr>
<tr>
<td>(L3) median((z_{\text{spec}}))</td>
<td>0.75</td>
<td>0.77</td>
<td>0.77</td>
</tr>
<tr>
<td>(L4) (z_{\text{peak}}) width</td>
<td>0.13</td>
<td>0.12</td>
<td>0.12</td>
</tr>
<tr>
<td>(L5) % with 0.6 ≤ (z_{\text{phot}}) ≤ 1.0</td>
<td>76%</td>
<td>81%</td>
<td>83%</td>
</tr>
<tr>
<td>(L6) mean((z_{\text{phot}})) (0.6 ≤ (z_{\text{phot}}) ≤ 1.0)</td>
<td>0.78</td>
<td>0.78</td>
<td>0.78</td>
</tr>
<tr>
<td>VIPERS (0.6 ≤ (z_{\text{spec}}) ≤ 1.0)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>(L7) (N) selected galaxies</td>
<td>536</td>
<td>666</td>
<td>668</td>
</tr>
<tr>
<td>(L8) (f^{\text{spec}}_{\text{OII}}) &gt; 10⁻¹⁶ erg cm⁻¹ s⁻²</td>
<td>64%</td>
<td>76%</td>
<td>73%</td>
</tr>
<tr>
<td>Plates eboss6-7 (8.82 deg²)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>(L9) (N) selected galaxies</td>
<td>1604</td>
<td>1670</td>
<td>1692</td>
</tr>
<tr>
<td>(L10) Targeted</td>
<td>96%</td>
<td>(81%)</td>
<td>(87%)</td>
</tr>
<tr>
<td>(L11) Unreliable (z_{\text{spec}})</td>
<td>26%</td>
<td>(10%)</td>
<td>(13%)</td>
</tr>
<tr>
<td>(L12) Median((z_{\text{spec}})) reliable</td>
<td>0.74</td>
<td>(0.77)</td>
<td>(0.76)</td>
</tr>
<tr>
<td>(L13) (z_{\text{spec}}) peak width reliable</td>
<td>0.12</td>
<td>(0.12)</td>
<td>(0.12)</td>
</tr>
<tr>
<td>(L14) Efficiency (0.6 &lt; (z_{\text{spec}}) &lt; 1.0)</td>
<td>59%</td>
<td>(76%)</td>
<td>(73%)</td>
</tr>
<tr>
<td>Plates eboss6-7</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>0.6 &lt; (z_{\text{spec}}) ≤ 1.0 only</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>(L15) Mean((z_{\text{spec}})) reliable</td>
<td>0.77</td>
<td>(0.78)</td>
<td>(0.78)</td>
</tr>
<tr>
<td>(L16) (f^{\text{spec}}_{\text{OII}}) &gt; 10⁻¹⁶ erg cm⁻¹ s⁻²</td>
<td>78%</td>
<td>(86%)</td>
<td>(85%)</td>
</tr>
<tr>
<td>(L17) Expected (z_{\text{spec}}) failure</td>
<td>1.1%</td>
<td>(0.5%)</td>
<td>(0.7%)</td>
</tr>
</tbody>
</table>

Notes. Lines are similar to Table 3.

More precisely, on the one hand, they have slightly more objects with 0.6 ≤ \(z_{\text{phot}}\) ≤ 1.0, but on the other, their median redshift is slightly lower, and they have slightly less \([\text{OII}]\) emission.

5.5. Adjusting the selection density

Our tests in Sect. 5.4 were done on a single location in a rather small area compared to the aim of 1500 deg² of the eBOSS/ELG survey. Here we investigate 1) the mean object density over large SGC areas and 2) the way the selection efficiency varies if we change the selection density. We refer to Paper III for a complete analysis over the full SGC.

The lower cut on the Fisher discriminant, \(X_{\text{Fisher min}}\), is set so that our selections have an object density of 180 deg⁻² over a ~50 deg² area included in the CFHTLS-Wide W1 field, approximately centred at RA = 34 and Dec = -6.5. Thanks to the recent development of catalogue tools for the Paper III analysis, it is now feasible to apply our selections using SDSS, WISE, and SCUSS photometry over larger SDSS footprints. We computed the object density for two typical SGC areas of ~700 deg² each: one that we label LowDec (−35 < RA < 40 and −5 < Dec < 5) and one labelled HiDec (0 < RA < 30 and 5 < Dec < 30).

The Fisher_UGRIZW1 selection has a mean object density of 183 deg⁻² (166 deg⁻², respectively) over the LowDec (HiDec, respectively) area, whereas the Fisher_GRIW1 and the Fisher_GRIW1OII selections have a mean object density of 183–187 deg⁻² over both areas. The Fisher_UGRIZW1 thus seems to have a less homogeneous density over the SGC than the Fisher_GRIW1 and Fisher_GRIW1OII selections.

We note that the Fisher_UGRIZW1 selection object density can be increased by lowering \(X_{\text{Fisher min}}\), the threshold cut on the Fisher discriminant. To illustrate this flexibility in our method, we do the following exercise using the CFHTLS \(z_{\text{phot}}\) for our ~50 deg² test area. We look at the variations of the mean \(z_{\text{spec}}\) and of the percentage of galaxies with 0.6 ≤ \(z_{\text{phot}}\) ≤ 1.0 as a function of the selection density, when varying the Fisher discriminant threshold cut \(X_{\text{Fisher min}}\) from 2.0 to 1.0 in steps of 0.1. We note that the efficiencies computed with the \(z_{\text{phot}}\) are higher than the ones computed with the \(z_{\text{spec}}\), because there is no requirement to have a measurable redshift from the spectrum; however, we are here interested in the relative variation with the threshold cut on the Fisher discriminant. The results are displayed in Fig. 12, where we see that the four Fisher discriminants have similar behaviours. If we decrease the threshold cut on the Fisher discriminant (from left to right), the density increases and the mean \(z_{\text{phot}}\) decreases, meaning that we select more galaxies but they have a lower redshift. The percentage of galaxies with 0.6 ≤ \(z_{\text{phot}}\) ≤ 1.0 decreases when the density increases, because there are more selected galaxies at \(z_{\text{phot}} < 0.6\). When the density decreases, we see two different types of behaviour. For the Fisher_GRIW1 selection, the percentage increases: this is because the mean redshift also increases, but staying at ≤0.8 implies that more galaxies are included in the 0.6 ≤ \(z_{\text{phot}}\) ≤ 1.0 range. However, we see a different behaviour for the three
other selections, where the percentage flattens or starts to reverse when going to low densities. This is explained by the fact that the selections start to include galaxies at $z > 0.6$ with $z_{\text{phot}}$ peak width slightly lower redshift than the Fisher_UGRIZW1 selection and a slightly narrower distribution than the Fisher_GRZW1 selection. For low densities, the Fisher_UGRIZW1 selection has a slightly lower redshift of the selection and, for the Fisher_GRZW1 selection, is due to a higher redshift and a broader redshift distribution. For low densities, the Fisher_GRIZW1 selection has a slightly lower redshift than the Fisher_UGRIZW1 selection and a slightly narrower distribution than the Fisher_GRZW1 selection, which explains that we only observe a flattening and not a reversal.

Additionally, for the four Fisher discriminant selections, this percentage is fairly constant, within a few percentage points, for densities between $\sim 150$ deg$^{-2}$ and $\sim 250$ deg$^{-2}$. Overall, this means that increasing the selection density while lowering the threshold cut on the Fisher discriminant should still provide satisfactory results. We note that the percentage of galaxies with $0.6 \leq z_{\text{phot}} \leq 1.0$ is higher than our computed efficiency with $z_{\text{spec}}$ because it does not require the additional criterion to have a reliable $z_{\text{spec}}$ measurement. To quantitatively illustrate the impact of increasing the target density, we report in Table 5 the properties for the Fisher_UGRIZW1 selection when the cut on the Fisher discriminant is set to have a target density of 210 deg$^{-2}$ (1.209 $< X_{\text{F1}}$) over our $\sim 50$ deg$^2$ test area.

### 6. Fisher_UGRIZW1 and Fisher_GRIW1 selection stacked properties

We have shown in the previous section that the Fisher_UGRIZW1 and Fisher_GRZW1 selections successfully select galaxies in the $0.6 \leq z_{\text{spec}} \leq 1.0$ range with [OII] emission, thus permitting ~70% of the selection to be in the desired redshift range with a reliable $z_{\text{spec}}$ measurement in the 1h observation with the BOSS spectrograph. Although allowing a reliable redshift measurement, the typical individual spectra are noisy (see Fig. 3), which prevents us from visualising or measuring the typical features of the selected galaxies. Stacking the data allows us to significantly increase the signal-to-noise ratio in the data, thereby enabling this visualisation or measurement of typical features of the selections that would not be visible or measurable in the individual data.

In this section, we take advantage of the unbiased, almost complete coverage of the Fisher_UGRIZW1 and Fisher_GRZW1 selections with the ten $\text{eboss}^6$–7 test plates to study some global physical properties of those two selections through the use of stacked data. We stack the $\text{eboss}^6$–7 spectra in Sect. 6.1 and the CFHTLS-Wide images in Sect. 6.2.

---

**Table 5.** Fisher_UGRIZW1 selection properties for a target density of 210 deg$^{-2}$ (1.209 $< X_{\text{F1}}$) over our $\sim 50$ deg$^2$ test area.

<table>
<thead>
<tr>
<th>Photometric data ($\sim 50$ deg$^2$)</th>
<th></th>
<th>Fisher_UGRIZW1</th>
</tr>
</thead>
<tbody>
<tr>
<td>Density (deg$^{-2}$)</td>
<td>212</td>
<td></td>
</tr>
<tr>
<td>eBOSS/LRG overlap (deg$^{-2}$)</td>
<td>2.1</td>
<td></td>
</tr>
<tr>
<td>median($z_{\text{phot}}$)</td>
<td>0.77</td>
<td></td>
</tr>
<tr>
<td>$z_{\text{phot}}$ peak width</td>
<td>0.12</td>
<td></td>
</tr>
<tr>
<td>Percentage with $0.6 \leq z_{\text{phot}} \leq 1.0$</td>
<td>78%</td>
<td></td>
</tr>
<tr>
<td>mean($z_{\text{phot}}$) ($0.6 \leq z_{\text{phot}} \leq 1.0$)</td>
<td>0.78</td>
<td></td>
</tr>
<tr>
<td>VIPERS ($0.6 \leq z_{\text{spec}} \leq 1.0$)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$N$ selected galaxies</td>
<td>671</td>
<td></td>
</tr>
<tr>
<td>log$<em>{10}(f</em>{\text{tot}})$($z_{\text{spec}}$) $&gt;-16.0$</td>
<td>78%</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Plates eboss6–7 (8.82 deg$^2$)</th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>$N$ selected galaxies</td>
<td>1902</td>
<td></td>
</tr>
<tr>
<td>Targeted</td>
<td>86%</td>
<td></td>
</tr>
<tr>
<td>Non-reliable $z_{\text{spec}}$</td>
<td>(12%)</td>
<td></td>
</tr>
<tr>
<td>median($z_{\text{spec}}^{\text{reliable}}$)</td>
<td>(0.77)</td>
<td></td>
</tr>
<tr>
<td>$z_{\text{spec}}$ peak width††</td>
<td>(0.12)</td>
<td></td>
</tr>
<tr>
<td>Efficiency ($0.6 \leq z_{\text{spec}}^{\text{reliable}} \leq 1.0$)</td>
<td>(69%)</td>
<td></td>
</tr>
</tbody>
</table>

Notes. Reported quantities are similar to those in Table 3.
analysis for the two Fisher_UGRIZW1 and Fisher_GRIW1 selections. The CFHTLS-Wide images are about three magnitudes deeper than the SDSS and have better resolution and seeing (pixel scale of 0.187” pix⁻¹ and seeing of 0.7”~0.8”). Galaxy surface brightness distribution can be modelled with a Sérsic (1968) profile \( I(r) = I_e \times \exp[-\left(\frac{r}{r_e}\right)^{1/n_s} - 1] \), where \( I(r) \) is the surface brightness at \( r \), and \( I_e \) is the surface brightness at the effective radius \( r_e \), which is the radius which encloses half of the emitted light. The Sérsic index \( n_s \) translates the shape of the profile, with a higher value corresponding to a profile more peaked at the centre and with larger wings; \( n_s = 4 \) corresponds to a de Vaucouleurs (1948) profile, which is typical of early-type galaxies, while \( n_s = 1 \) corresponds to an exponential profile, typical of late-type galaxies. Wuyts et al. (2011) have shown that, for \( 0.1 < z_{\text{spec}} < 2.5 \), typical passive galaxies have \( n_s \approx 4 \), while typical star-forming galaxies have \( n_s \approx 1-2 \).

We used the CFHTLS \( i \)-band images and restricted ourselves to the eboss–7 plates passing the Fisher_UGRIZW1 and Fisher_GRIW1 selections with \( 0.7 \leq z_{\text{spec}} \leq 0.8 \) to mitigate the effect of redshift on the angular size of the galaxies. In this redshift range, which corresponds to the peak of the \( z_{\text{spec}} \) distribution for the two considered selections, the \( i \)-band probes the rest frame 4100–4400 Å. We obtain similar results if we use the CFHTLS \( r \)-band images, which probe the 3400–3700 Å rest-frame at \( 0.7 \leq z_{\text{spec}} \leq 0.8 \). For each stamp used in the median stacked image, we masked neighbouring objects beforehand, subtracted the sky, and scaled the galaxy fluxes to a normalised absolute magnitude. For both selections, we created two median stacked images, using the eboss–7 galaxies with \( 0.7 \leq z_{\text{spec}} \leq 0.8 \): 1) we used all the observed objects passing the selection \( \sim370 \) galaxies; 2) we used only objects passing one selection but not the other \( \sim90 \) galaxies. We fitted the surface brightness distribution with the GALFIT software (v3.0.5: Peng et al. 2010). During the fit, we set the axis ratio to 1 and the position angle to 0; besides this, we used spectroscopic stars (\( 18 \leq i_{\text{AB}} \leq 21 \)) in the eboss–7 plates area to create a point-spread function (PSF) stamp.

We present the stacked images and their radial profile in the Fig. 14. We also report in this figure the estimated \( r_e \) and \( n_s \), along with their uncertainty computed via a thousand bootstrap realisations for each case. The stacked galaxies are relatively small sizes, though clearly resolved: the surface brightness profile extends significantly farther than the PSF full-width-half-maximum. Regarding the surface brightness profile shape, we observe that both selections have a Sérsic index of \( \sim1.3–1.4 \), typical of star-forming galaxies (top panel). Interestingly, we see that the Fisher_GRIW1 selection galaxies have a slightly higher Sérsic index, which is consistent with the trend seen in previous sections toward the Fisher_GRIW1 selection forming fewer stars than the Fisher_UGRIZW1 selection. This trend is more significant on the stacked images using galaxies belonging to only one of the selections (bottom panel). In addition, the Fisher_GRIW1 selection galaxies also have sizes slightly larger than the Fisher_UGRIZW1 selection galaxies ones. Finally, we note that the Fisher_UGRIZW1 selection galaxies tend to have relatively more flux in a 2” aperture – corresponding to the BOSS spectrograph fibre diameter – than the Fisher_GRIW1 selection, though this effect is minor. For the fitted parameters corresponding to the bottom panel of Fig. 14, 90% of the total flux is included in a 2” aperture for the Fisher_UGRIZW1 selection galaxies, versus 84% for the Fisher_GRIW1 selection galaxies.

![Fig. 13. Stacked spectra from the eboss–7 plates galaxies with 0.6 ≤ z_{\text{spec}} ≤ 1.0 passing the Fisher_UGRIZW1 and Fisher_GRIW1 selections. Top panel: the stacking (average S/N of ~5) is done using all galaxies passing the selections (~1100 galaxies per stack). Bottom panel: the stacking (average S/N of ~3) is done using only galaxies not belonging to the intersection between Fisher_UGRIZW1 and Fisher_GRIW1 selections (~300 galaxies per stack), to enhance the differences.](image-url)
7. Conclusions

We have studied possible $z \sim 0.8$ ELG selection schemes in preparation of the eBOSS/ELG survey. The initial eBOSS/ELG requirements are to select 180 deg $^{-2}$ SDSS galaxies, 70% of which have a reliable $z_{\text{spec}}$ measurement in a $\sim$1h exposure observation with the BOSS spectrograph, 0.6 $\leq z_{\text{spec}}$ $\leq$ 1.0, and a catastrophic failure rate $\leq$1% in this redshift range. Our selection schemes are based on the Fisher discriminant approach, which consists in computing the Fisher discriminant, a linear combination of colours defined from a spectroscopic training sample, and a simple selection with cuts on magnitudes and on this Fisher discriminant. This type of selection is simple and has the advantage of being flexible, since the density can be adjusted by modifying the Fisher discriminant threshold.

We studied the use of different photometric surveys: SCUSS/µ+SDSS/2g, WISE/W1, SDSS/2+WISE/W1, and SDSS/2+WISE/W1. We quantified the properties of our selections in terms of redshift, [OII] emission, and efficiency, using dedicated eBOSS/ELG test plates and public photometric and spectroscopic data. We did a parallel analysis of colour–colour selections and showed, on the one hand, that the W1-band is crucial in improving the efficiency and, on the other hand, that the Fisher selections are competitive with colour–colour selections.

The Fisher_UGRIZ1 selection meets the eBOSS/ELG redshift requirements. It has a median redshift of 0.78, and 71% of the selection has $0.6 \leq z_{\text{spec}}$ $\leq$ 1.0; among those 71% galaxies, $\sim$80% have a significant [OII] emission ($f_{\text{[OII]}}$ $\geq$ 10$^{-16}$ erg cm$^{-2}$ s$^{-1}$ Å$^{-1}$), and the catastrophic $z_{\text{spec}}$ measurement is expected to be 0.5% with the current instrumental setup and pipeline. The Fisher_GRIW1 selection also meets the eBOSS/ELG redshift requirements with a 71% efficiency in the $0.6 \leq z_{\text{spec}}$ $\leq$ 1.0 range and an expected catastrophic $z_{\text{spec}}$ measurement of 0.9% in this redshift range. This selection has, on average, less [OII] emission than the Fisher_UGRIZ1 selection. Training the Fisher method with $z_{\text{spec}}$ and [OII] flux (Fisher_UGRIZ1 selection) allows us to increase the [OII] emission of the selection, but at the cost of a slightly lower mean redshift. The Fisher_GRIW1 selection using the DECaLS/2-band seems to provide an acceptable alternative if set to a 180 deg $^{-2}$ target density. Finally, we show that the density can be increased while keeping a reasonably high number of galaxies with $0.6 \leq z_{\text{phot}}$ $\leq$ 1.0.

In addition, we also studied the properties of the stacked spectra and stacked CFHTLS-wide images for the Fisher_UGRIZ1 selection. Those stacked data present typical features of star-forming galaxies and also indicate that the Fisher_UGRIZ1 selection tends to favour more star-forming galaxies than the Fisher_GRIW1 selection.

For the two most efficient selections, the Fisher_UGRIZ1 and Fisher_GRIW1 selections, the homogeneity over the SGC along with the possible systematic dependence on various quantities, is studied in Paper III. Paper III also presents the catalogue release over the SGC for those two selections.

To conclude, this Fisher discriminant approach can be used more generally if one desires to select a galaxy population with desired properties with multi-band photometry. The method is simple and offers flexibility, the only requirement being the use of a spectroscopic training sample. Future massive spectroscopic surveys, such as DESI, 4MOST12, or the Prime Focus Spectrograph (PFS; Sugai et al. 2012), will provide large samples that are particularly well-suited to the Fisher discriminant approach.

12 https://www.4most.eu/
Acknowledgements. A.R. acknowledges funding from the P2IO LabEx (ANR-10-LABX-0038) in the framework “Investissements d’Avenir” (ANR-11-IDEX-0003-01) managed by the French National Research Agency (ANR). J.C. acknowledges financial support from MINECO (Spain) under project number AYA2012-31101. J.P.K. and T.D. acknowledge support from the ERC advanced grant LIDA. This study is based on data from SDSS-III (full text acknowledgement: http://www.sdss3.org/collaboration/boiler-plate.php) and is done in the context of SDSS-IV (full text acknowledgement: http://www.sdss.org/collaboration/0fficialSDSSAcknowledgment). The SCUSS is funded by the Main Direction Program of Knowledge Innovation of Chinese Academy of Sciences (No. KJCX2-EW-06). It is also an international cooperative project between National Astronomical Observatories, Chinese Academy of Sciences and Steward Observatory, University of Arizona, USA. Technical support and observational assistance of the Bok telescope are provided by Steward Observatory. The project is managed by the National Astronomical Observatory of China and Shanghai Astronomical Observatory. This publication makes use of data products from the Wide-field Infrared Survey Explorer, which is a joint project of the University of California, Los Angeles, the Jet Propulsion Laboratory/California Institute of Technology, and NEOWISE, which is a project of the Jet Propulsion Laboratory/California Institute of Technology. WISE and NEOWISE are funded by the National Aeronautics and Space Administration. This work is based on observations obtained with MegaPrime/MegaCam, a joint project of CFHT and CEA/DAPNIA, at the Canada–France–Hawaii Telescope (CFHT), which is operated by the National Research Council (NRC) of Canada, the Institut National des Sciences de l’Univers of the Centre National de la Recherche Scientifique (CNRS) of France, and the University of Hawaii. This research used the facilities of the Canadian Astronomy Data Centre operated by the National Research Council of Canada, the Institut National des Sciences de France, the Canada–France–Hawaii Telescope (CFHT), which is operated by the National Research Council of Canada, the Institut National des Sciences de l’Univers of the Centre National de la Recherche Scientifique (CNRS) of France, and the University of Hawaii. This research used the facilities of the Canadian Astronomy Data Centre operated by the National Research Council of Canada with the support of the Canadian Space Agency. This research uses data from the VIMOS VLT Deep Survey, obtained from the VVDS database operated by Ceson, Laboratoire d’Astrophysique de Marseille, France. This paper uses data from the VIMOS Public Extragalactic Redshift Survey (VIPERS). VIPERS was performed with the ESO Very Large Telescope under the “Large Programme” 182.A-0886. The participating institutions and funding agencies are listed at http://vipers.inaf.it. We thank the anonymous referee for his report, which helped us improve the clarity of the paper.

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Appendix A: CFHTLS photometric redshift reliability

In Sect. 5.4, we make use of the CFHTLS-Wide photometric redshifts (T0007 release\textsuperscript{13}; Ilbert et al. 2006; Coupon et al. 2009) to estimate the redshift distribution of our selection schemes. Those photometric redshifts have been proven to be of very good quality up to \( i < 22.5 \) (bias below 1\%, scatter of \( \sim 0.04 \), and less than 4\% outliers). Nevertheless, those statistics have been computed for magnitude-limited samples, whereas the galaxies under study in this paper are mainly star-forming galaxies. Owing to the lack of features (weak 4000 Å break, power law spectrum), this class of galaxies is well-known for having slightly less accurate photometric redshift, which results in a higher outlier rate (e.g. Ilbert et al. 2006; Hildebrandt et al. 2012).

Using the eboss6-7 test plates, we demonstrate in Fig. A.1 the reliability of those photometric redshifts for ELGs up to redshift \( \sim 1 \). We selected eboss6-7 galaxies with a secure spectroscopic redshift and a [OII] total luminosity \( L_{\text{[OII]}} \) greater than \( 10^{41} \) erg s\(^{-1} \) (3712 galaxies with \( z_{\text{spec}} = 0.80 \pm 0.17 \)). For each object in our spectroscopic sample, we calculated \( \Delta z = \frac{z_{\text{phot}} - z_{\text{spec}}}{1+z_{\text{spec}}} \) and classify it as an outlier if \( |\Delta z| > 0.15 \). For each binned subsample, we report bias: the median value of \( \Delta z \); outl.: the percentage of outliers; and \( \sigma_{\text{outl rej.}} \): the standard deviation of \( \Delta z \) when outliers have been excluded. These quantities are used to facilitate comparison with other works. As mentioned in Hildebrandt et al. (2012), the outlier definition is arbitrary. We observe that the photometric redshifts are slightly biased high (bias \( \sim +0.01 \), for all magnitudes), the bias becoming significant for \( z_{\text{phot}} \gtrsim 1.1 \). The scatter is reasonable (\( \sigma_{\text{outl rej.}} \sim 0.04 \)), as is the outlier rate (5–10\%). Those results qualitatively agree with previous studies (Ilbert et al. 2006; Hildebrandt et al. 2012).

\textsuperscript{13} http://terapix.iap.fr/rubrique.php?id_rubrique=267